

NHI Course No. 13063

Seismic Bridge Design Applications

25 July 1996

Part Two

Publication No. FHWA-SA-97-018

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16. Abstract Seismic Bridge Design Applications, Parts One and Two, contains the material used in two one-day national satellite seminars broadcast from the University of Maryland to provide seismic design application instruction. Mr. Robert Mast and Dr. Lee Marsh of BERGER/ABAM Engineers, Inc., were the instructors and developed the course materials. Part One includes seven sessions covering basic seismic principles, one complete seismic analysis and design example, modeling guidelines, multimodal analysis, and column design features. Part Two includes "homework problems" assigned after the first seminar as well as specific topics requested by participants of the first seminar.					
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Seismic Design of Bridges

Seminar No. 2 – Outline

Session No.	Topic	Reference Example
1	Practice Problem No. 1 Spread Footings	Concrete Box Girder Bridge (Design Example No. 1)
2	Abutments	
3	Practice Problem No. 2 Conceptual Design Steel Superstructure Issues	Steel Plate Girder Bridge (Design Example No. 2)
4	Skew Structure Issues Elastomeric Bearings	
5	Curved Structure Issues Piles	Curved Box Girder Bridge (Design Example No. 6)

Seismic Design of Bridges

Seminar No. 2 – Outline (continued)

Session No.	Topic	Reference Example
6	Drilled Shafts	Curved Box Girder Bridge (Design Example No. 6)
	Pile Bents	Pile Bent Bridge (Design Example No. 7)
	Joint Design	Other Topics
7	Existing Bridge Assessment and Retrofit	
	Questions and Answers	

Session 1

Concrete Box Girder Bridge Example

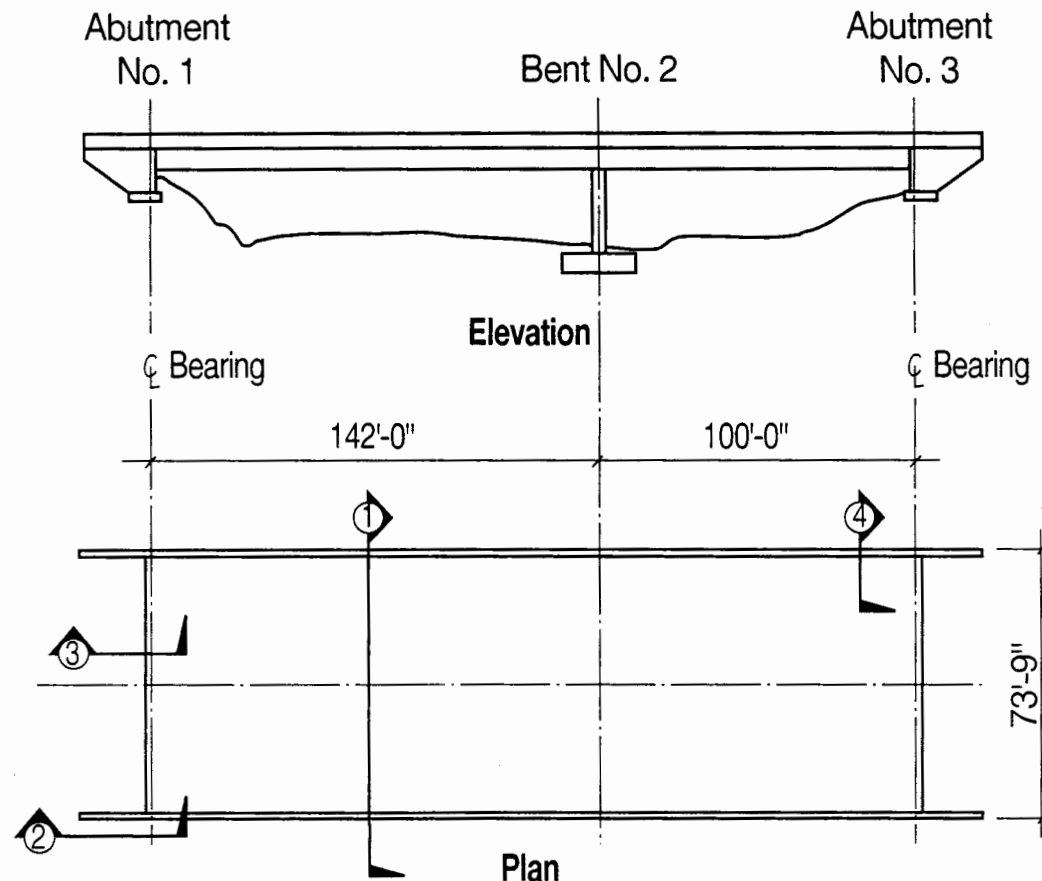
Session 1

- **Practice Problem No. 1**
- **Spread Footings**

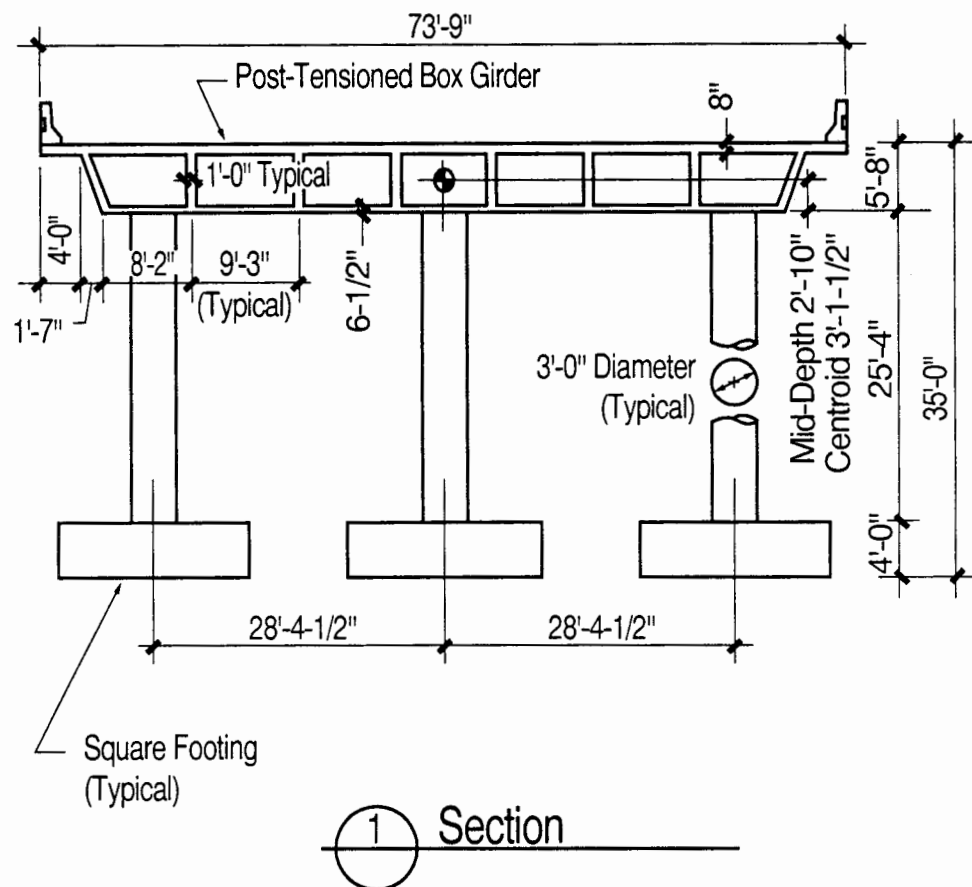
Session 2

- **Abutments**

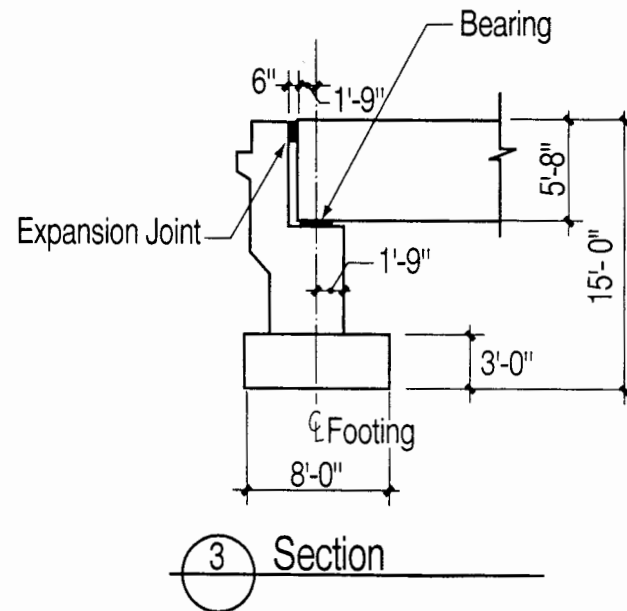
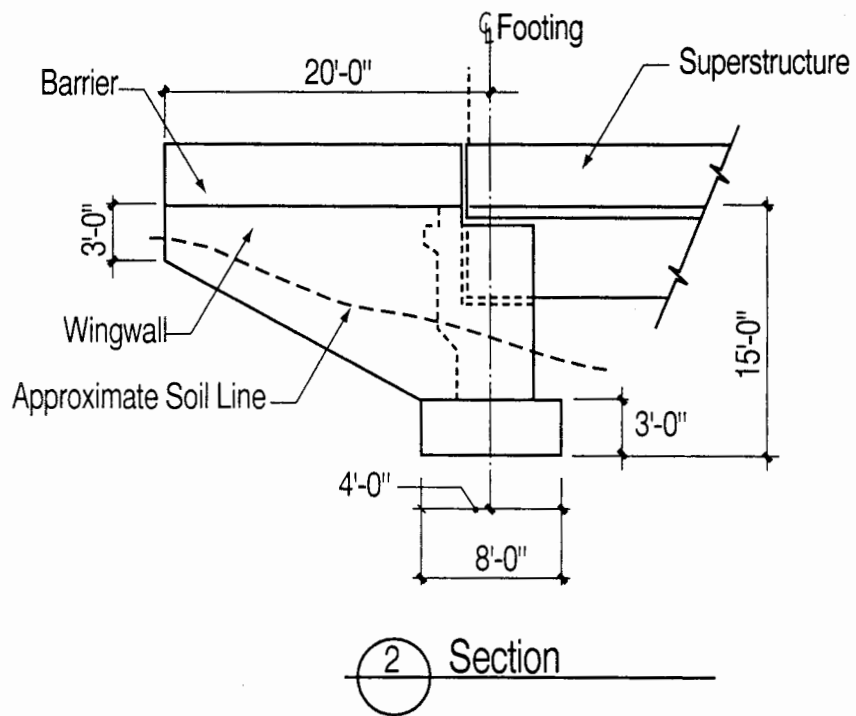
Bridge Layout / Plan and Elevation



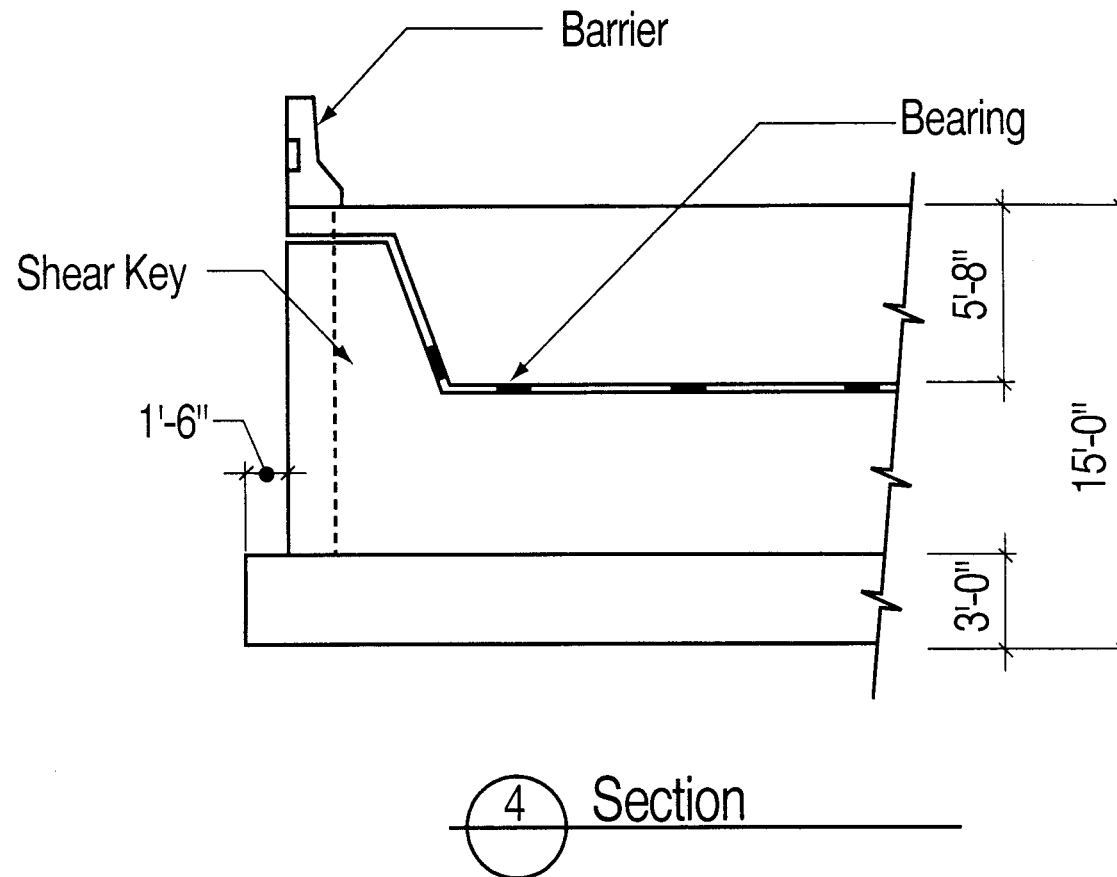
Layout / Preliminary Bent Details



Bridge Layout / Abutment Details



Layout / Shear Key at Abutments



Session 1

Required / Practice Problem No. 1

- **Calculate the Longitudinal Period**
- **Calculate the Longitudinal Forces and Displacements**
- **Design the Column Reinforcement**
- **Size Column Footing**
- **Assess the Effects of Plastic Hinging**

Basic Data for Bridge

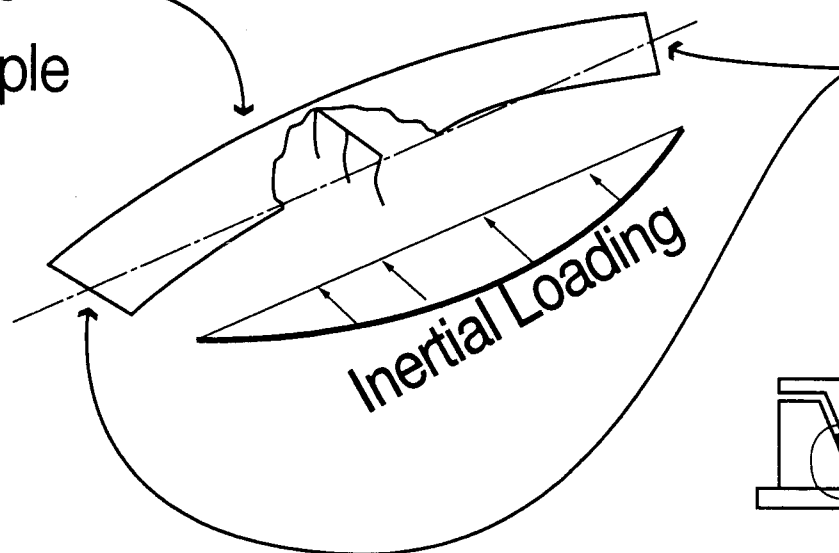
- Acceleration Coefficient, $A = 0.15g$
- Seismic Performance Category, $SPC = B$
- Soil — 250 ft Deep Glacial Sand and Gravel

$$S = 1.2$$

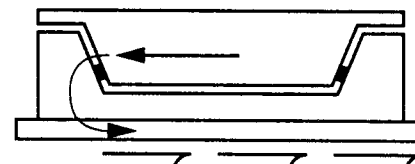
$$f_{ult} = 24 \text{ ksf}$$

Transverse Lateral Load Behavior

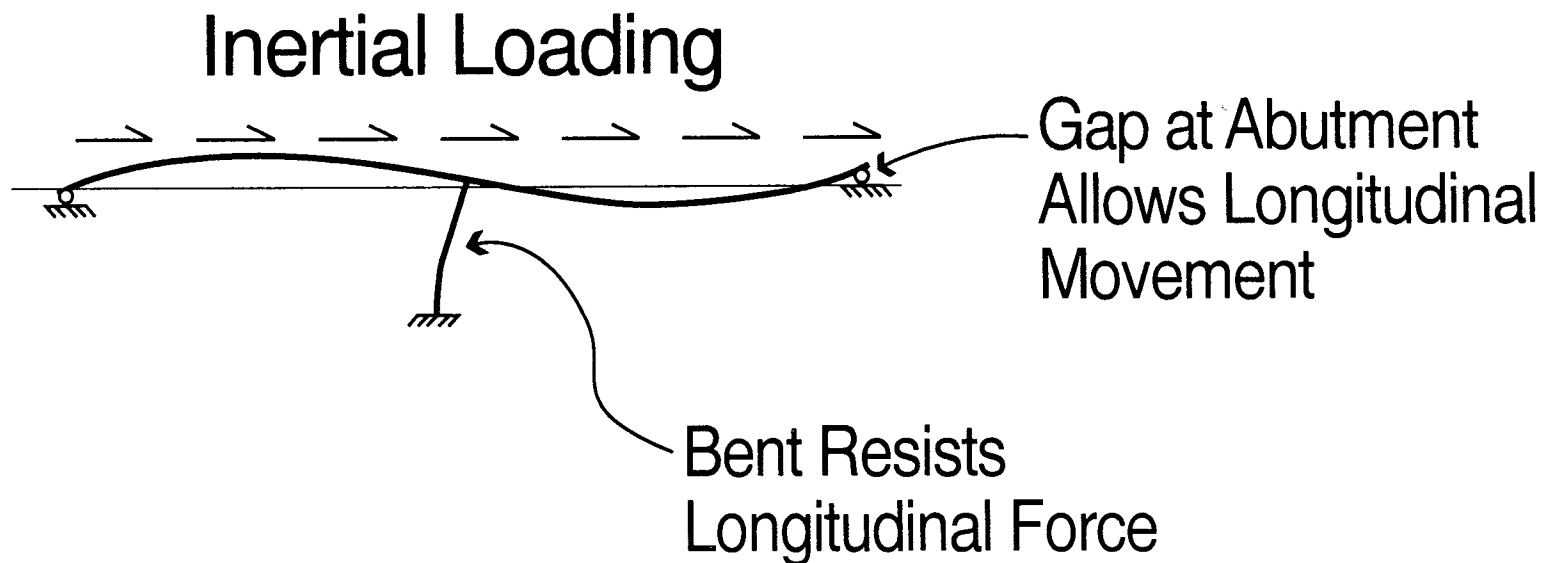
Superstructure
Acts as a Simple
Beam in Plan



Abutments
Resist Most
of the Force

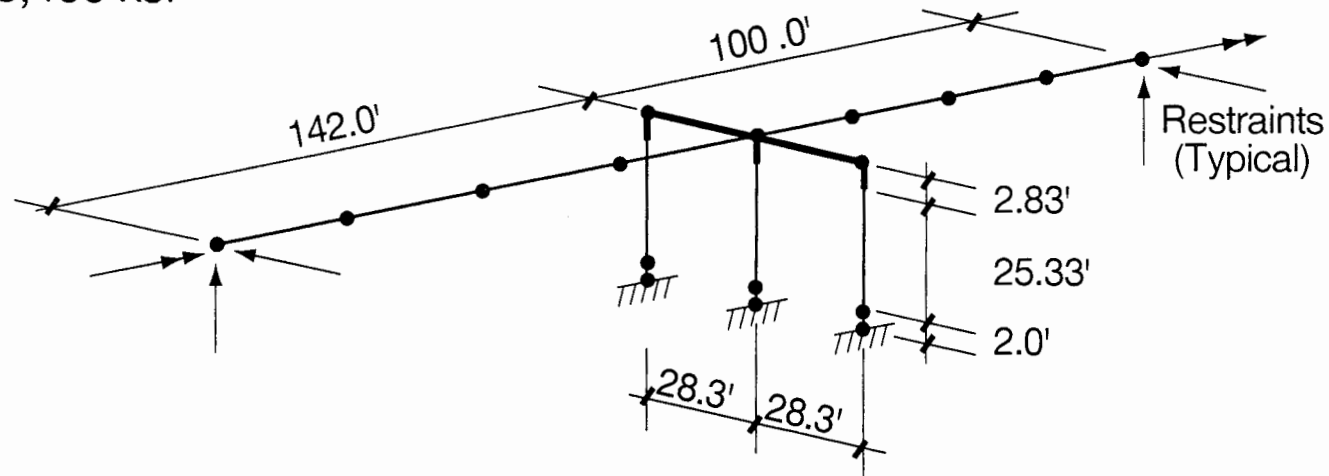


Longitudinal Lateral Load Behavior



Analytical Model and Properties

$E = 518,400 \text{ ksf}$



Superstructure

$$A = 120 \text{ ft}^2$$

$$I_{\text{str}} = 51,000 \text{ ft}^4$$

$$I_{\text{weak}} = 575 \text{ ft}^4$$

Capbeam

$$A = 25 \text{ ft}^2$$

$$I_{\text{str}} = I_{\text{weak}} = 10^7 \text{ ft}^4$$

Column

$$A = 7.07 \text{ ft}^2$$

$$I = 3.98 \text{ ft}^4$$

Longitudinal Period

Stiffness
(Bent Only)

$$K = 3 \left(\frac{12EI}{H^3} \right) = 3 \left(\frac{12(518,400)3.98}{(25.33 + 2.0)^3} \right)$$

$$K = 3639 \text{ kip/ft}$$

Weight

$$W = 4842 \text{ kip}$$

Period

$$T = 2\pi \sqrt{\frac{4842}{32.2 (3639)}} = 1.28 \text{ sec}$$

$$T_{\text{modal}} = 1.32 \text{ sec (3\% Difference)}$$

Longitudinal Shear and Moment

- **Total Base Shear**

$$C_s = \frac{1.2AS}{T^{2/3}} = \frac{1.2(0.15)(1.2)}{(1.28)^{2/3}} = 0.183 < 0.375 = 2.5A$$

$$V_{\text{base}} = C_s W = 0.183 (4842) = 886 \text{ kip}$$

Assumes All Mass Moves Equally

- **Column Forces**

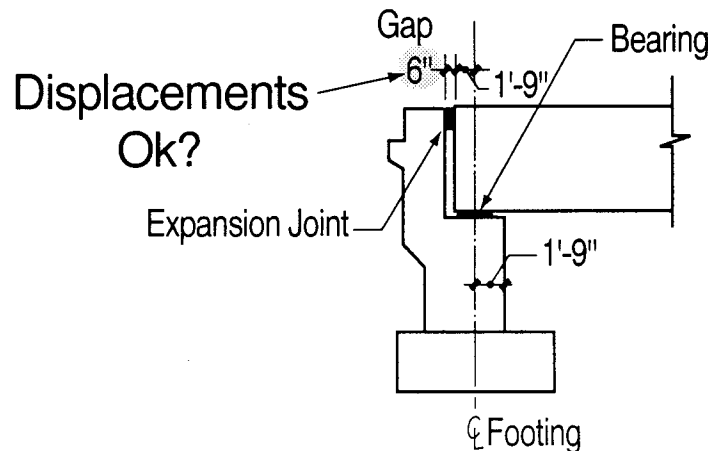
$$V_{\text{col}} = \frac{V_{\text{base}}}{3} = \frac{886}{3} = 295 \text{ kip vs. } V_{\text{modal}} = 288 \text{ kip}$$

$$M_{\text{col}} = V_{\text{col}} \left(\frac{H}{2} \right) = 295 \left(\frac{27.33}{2} \right) = 4031 \text{ kip ft vs. } M_{\text{modal}} = 3856 \text{ kip ft}$$

Displacement Calculations

$$\Delta = \frac{V_{\text{base}}}{K} = \frac{886}{3639} = 0.24 \text{ ft (2.9 in.) Gross Properties}$$

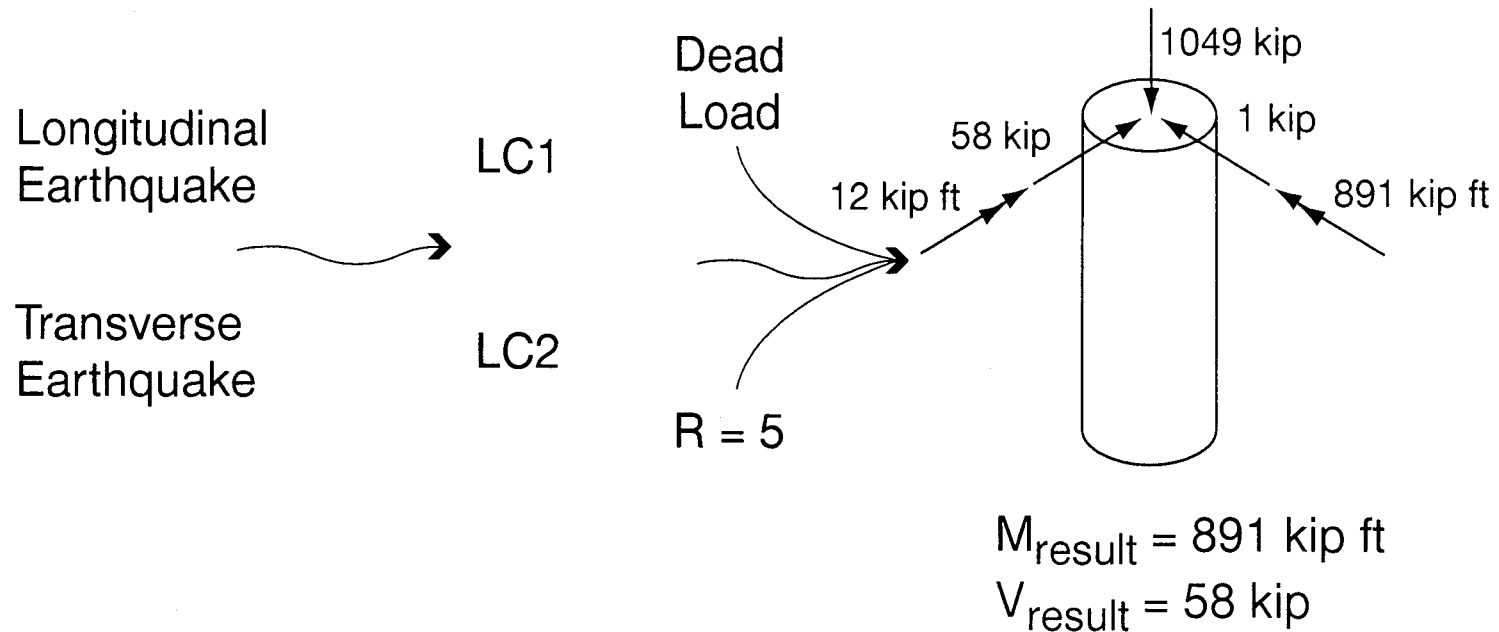
$$\Delta_{1/2} = \frac{0.145(4842)}{1820} = 0.39 \text{ ft (4.6 in.) Effective / Fixed Base}$$



- Potential for Joint Damage
- Add Footing Flexibility
- More Later

Column Design Forces

- **Outboard Column**



Column Flexural Design

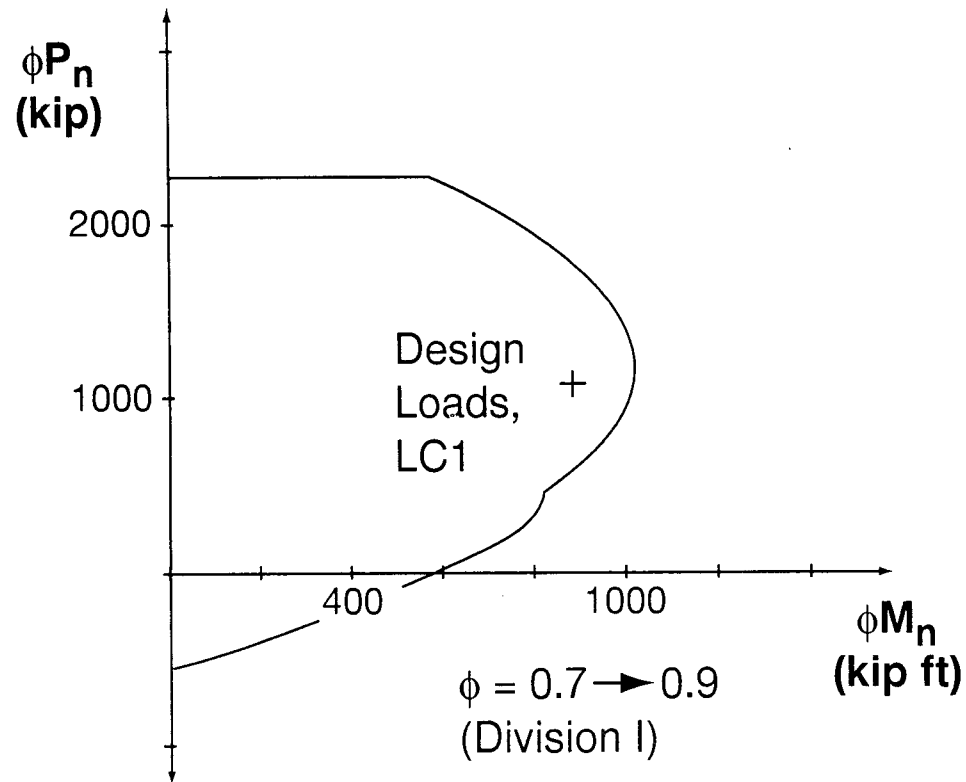
Try:

8 #10 Bars

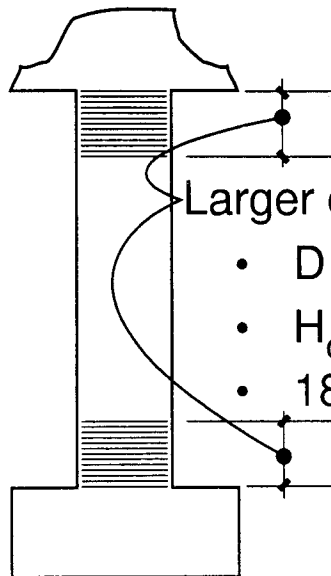
$\rho_g = 1.00\%$

$f_y = 60 \text{ ksi}$

$f'_c = 4 \text{ ksi}$



Hinge Zone Confinement



Larger of:

- D = 36"
- $H_{clr}/6 = 51"$
- 18"

$$\rho_s = 0.45 \left(\frac{A_g}{A_{core}} - 1 \right) \frac{f'_c}{f_{yh}} = 0.008$$

Minimum:

$$\rho_s \geq 0.12 \frac{f'_c}{f_{yh}} = 0.008$$

$$\text{Try } A_{sp} = 0.31 \text{ in}^2 \text{ (#5)}$$

$$s = \frac{4 A_{sp} d_s}{\rho_s d_{core}^2} = \frac{4 (0.31)(32 - 0.625)}{0.008(32)^2} = 4.75"$$

Use #5 @ 4.5 in. for 60 in.

Shear Strength

SPC B — Shear Strength Same as Division I

$$V_u = 58 \text{ kip} \quad \phi V_c = (0.85) \frac{2\sqrt{4000}}{1000} 36(28) = 109 \text{ kip}$$

$$\text{Use } A_{v_{\min}} = \frac{50(36)12}{60,000} = 0.36 \text{ in}^2$$

$$\text{Use \#5 @ 12 in.} \quad V_s = 2(0.31) \frac{28}{12} 60 = 87 \text{ kip}$$

$$\phi V_n = 109 + 0.85(87) = 183 \text{ kip}$$

Footing Design Forces

- **Outboard Column**

Longitudinal
Earthquake

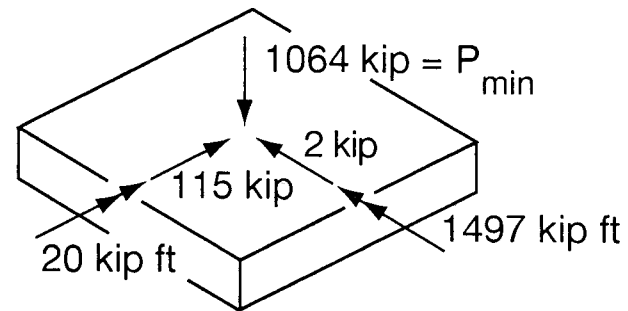
LC1

Transverse
Earthquake

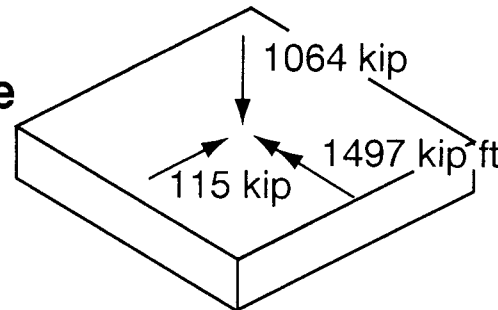
LC2

Dead
Load

$$R = \frac{5}{2} = 2.5$$

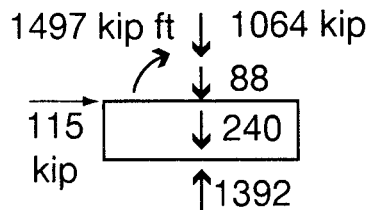


Resultant Forces Essentially Are



Footing Size

- If $B = L = 20$ ft



$$P = P_{D+LC1/R} + P_{\text{footing}} + P_{\text{soil}}$$

$$P = 1064 \text{ kip} + 240 \text{ kip} + 88 \text{ kip} = 1392 \text{ kip}$$

$$M = 1497 + 115(4) = 1957 \text{ kip ft}$$

$$e = \frac{M}{P} = \frac{1957}{1392} = 1.4 \text{ ft} \ll \frac{L}{3} = \frac{20}{3} = 6.7 \text{ ft}$$

- If $B = L = 15$ ft (Gravity Loads Control)

$$P = 1255 \text{ kip}$$

$$e = \frac{1957}{1255} = 1.6 \text{ ft} < \frac{15}{3} = 5 \text{ ft}$$

$$q = 9.5 \text{ ksf} < 24 \text{ ksf}$$

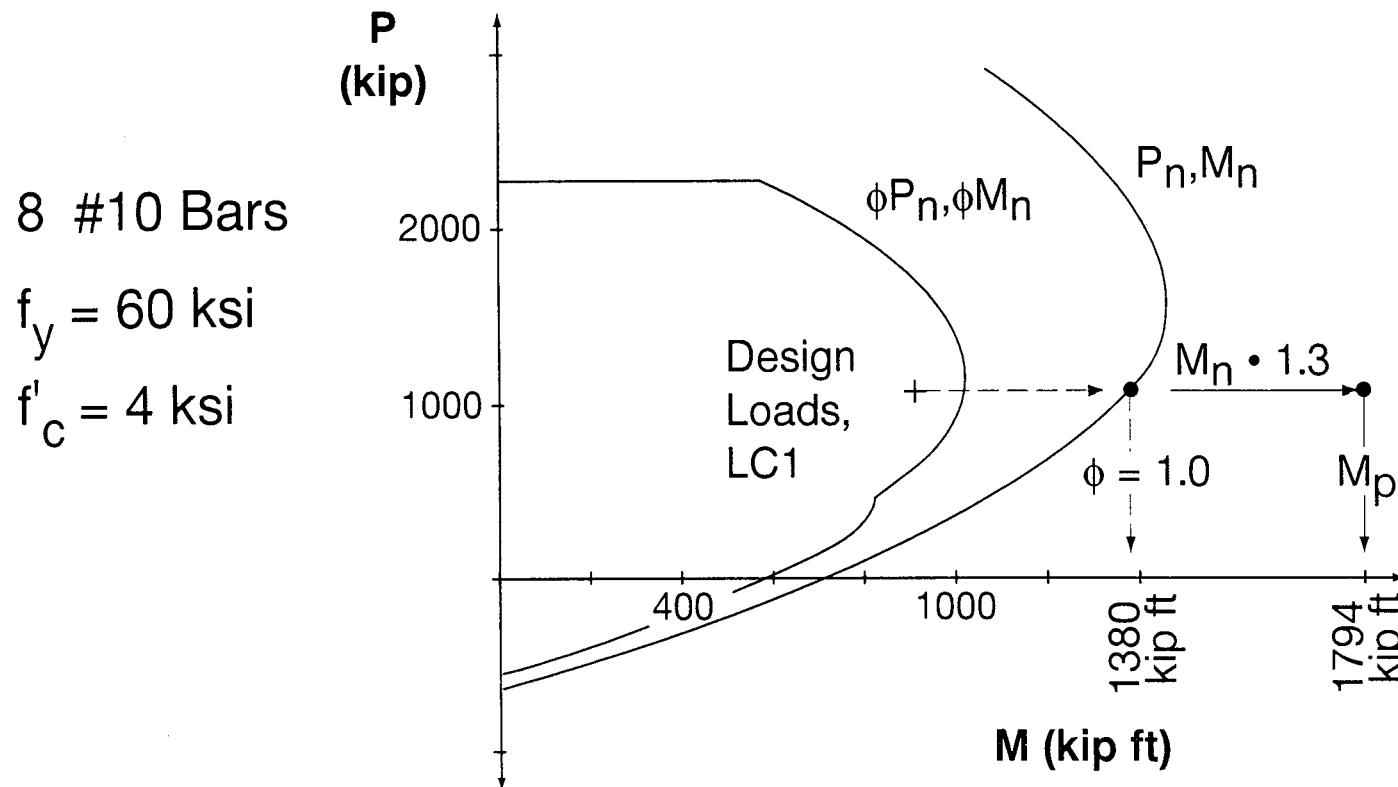
∴ 1/2 Uplift
Will Not
Control

Use 15 ft
Square Footing

Check the Effects of Plastic Hinging

Not Required in SPC B

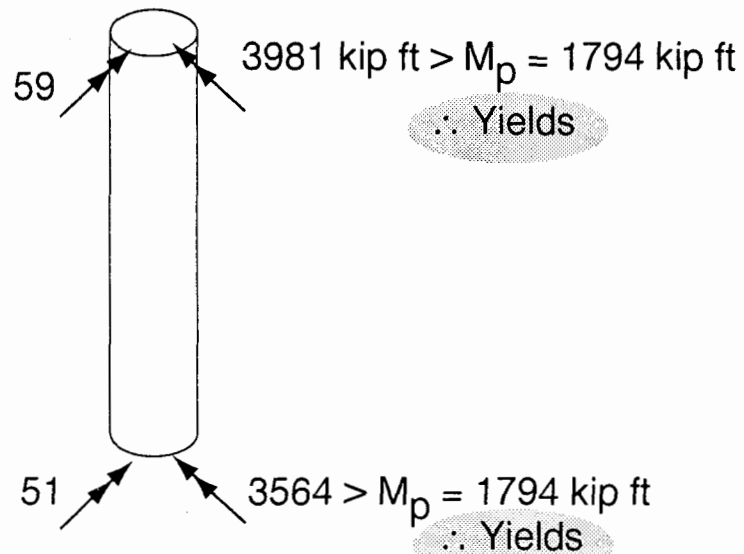
Column Nominal and Overstrength Properties



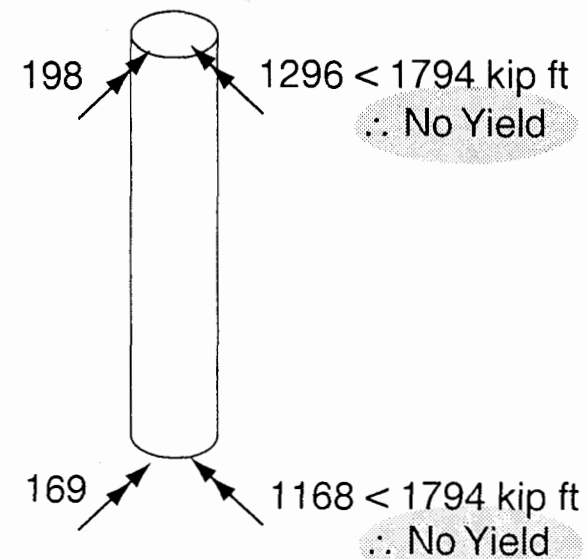
Will Column Develop Plastic Hinge?

Outboard Column

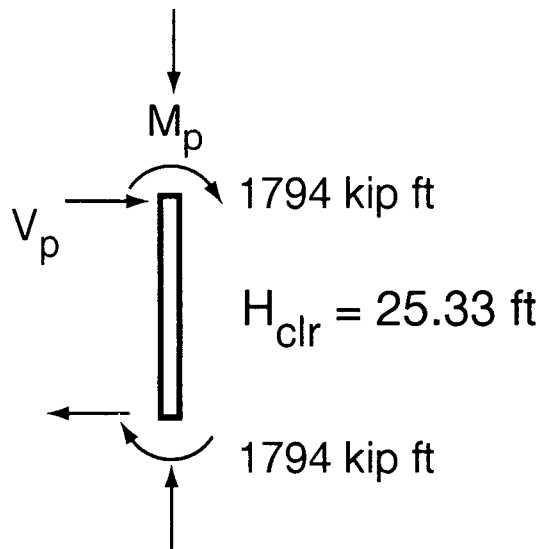
Elastic Forces LC1 + DL



Elastic Forces LC2 + DL



Maximum Column Shear



$$V_{\text{elastic}} = 288 \text{ kip}$$

$$V_p = \frac{2(1794)}{25.33} = 142 \text{ kip}$$

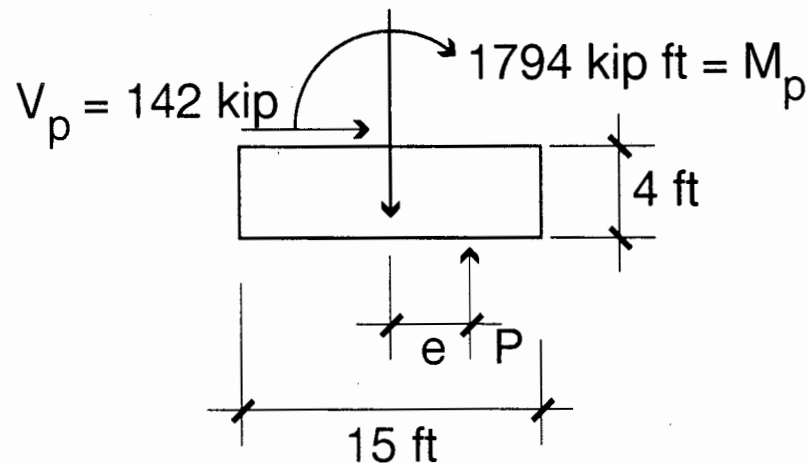
$$\phi V_n = 183 \text{ kip} \quad \therefore \text{OK}$$

Because We Provided
Minimum Steel

Plastic Hinging Effects on Footing

$$e = \frac{M}{P} = \frac{1794 + 142(4)}{1255} = 1.88 \text{ ft} < 5 \text{ ft}$$

and $q = 9.9 \text{ ksf} < 24 \text{ ksf}$



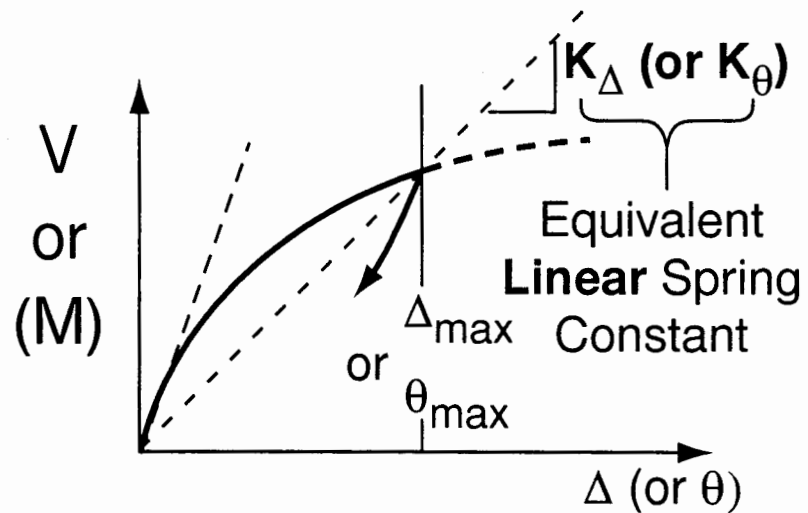
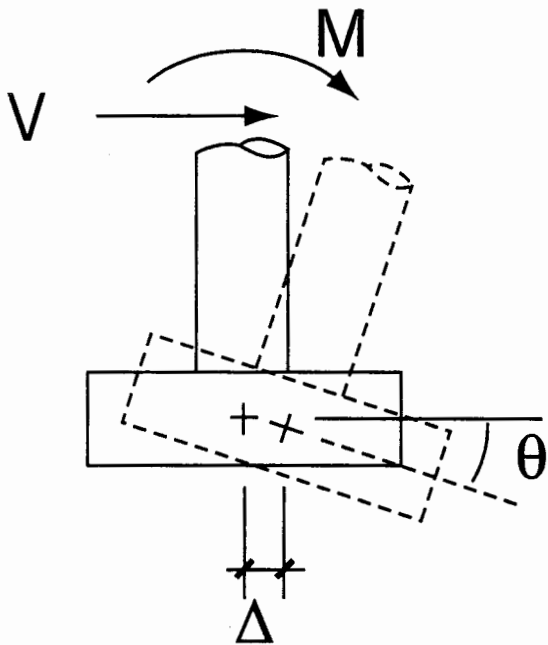
\therefore OK
for Plastic
Hinging

Session 1

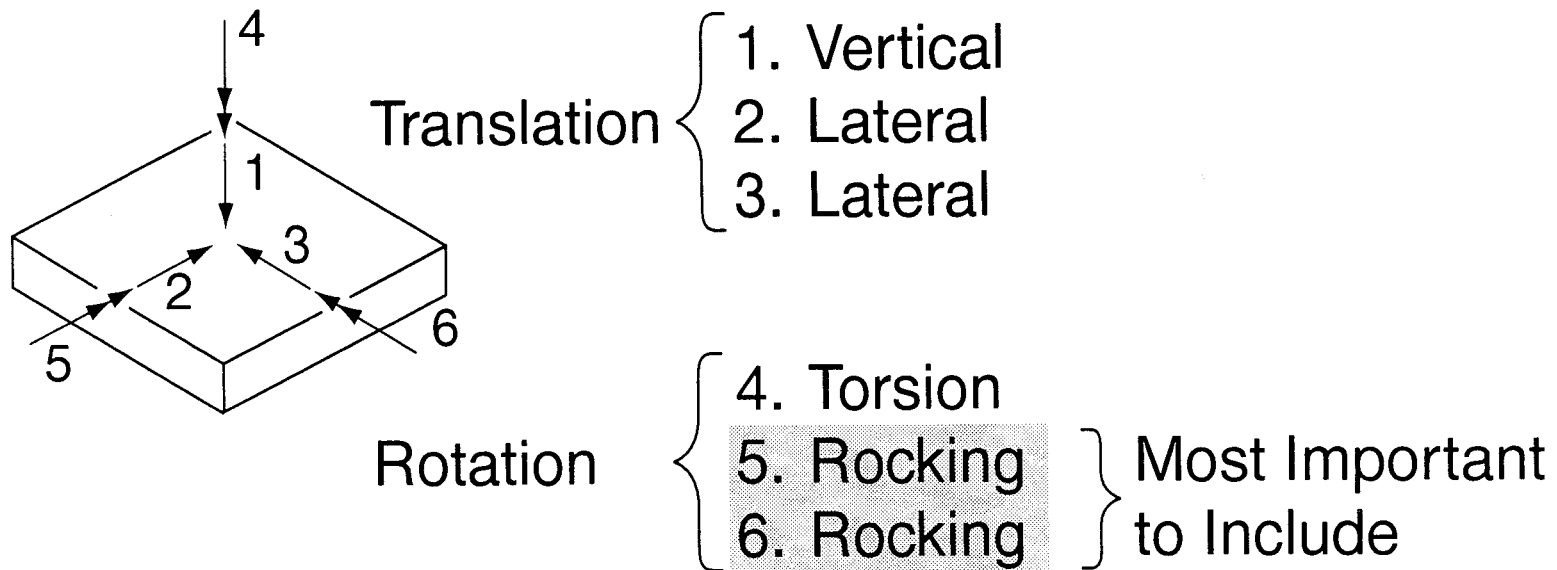
Spread Footings

- **Including Flexibility**
- Overturning and Sliding
- Pinned Base Columns

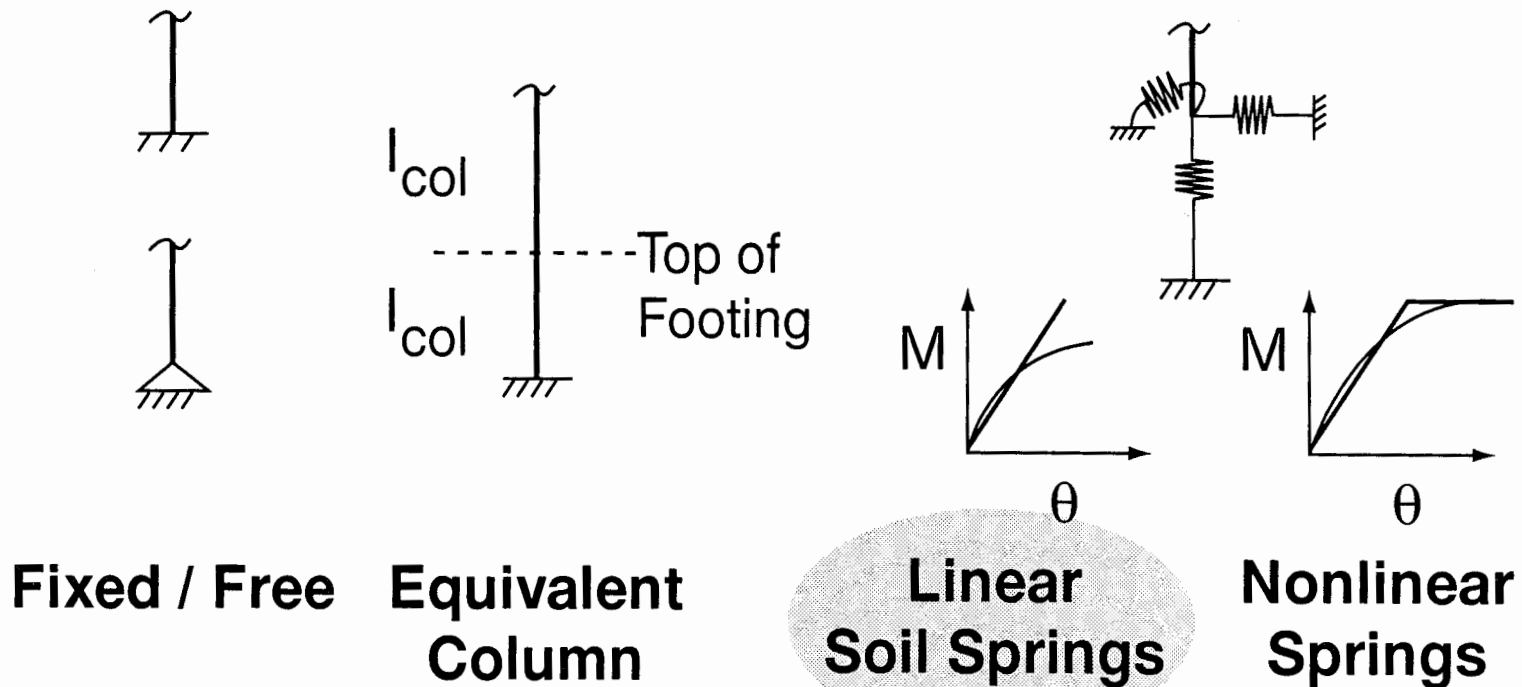
Conceptual Behavior



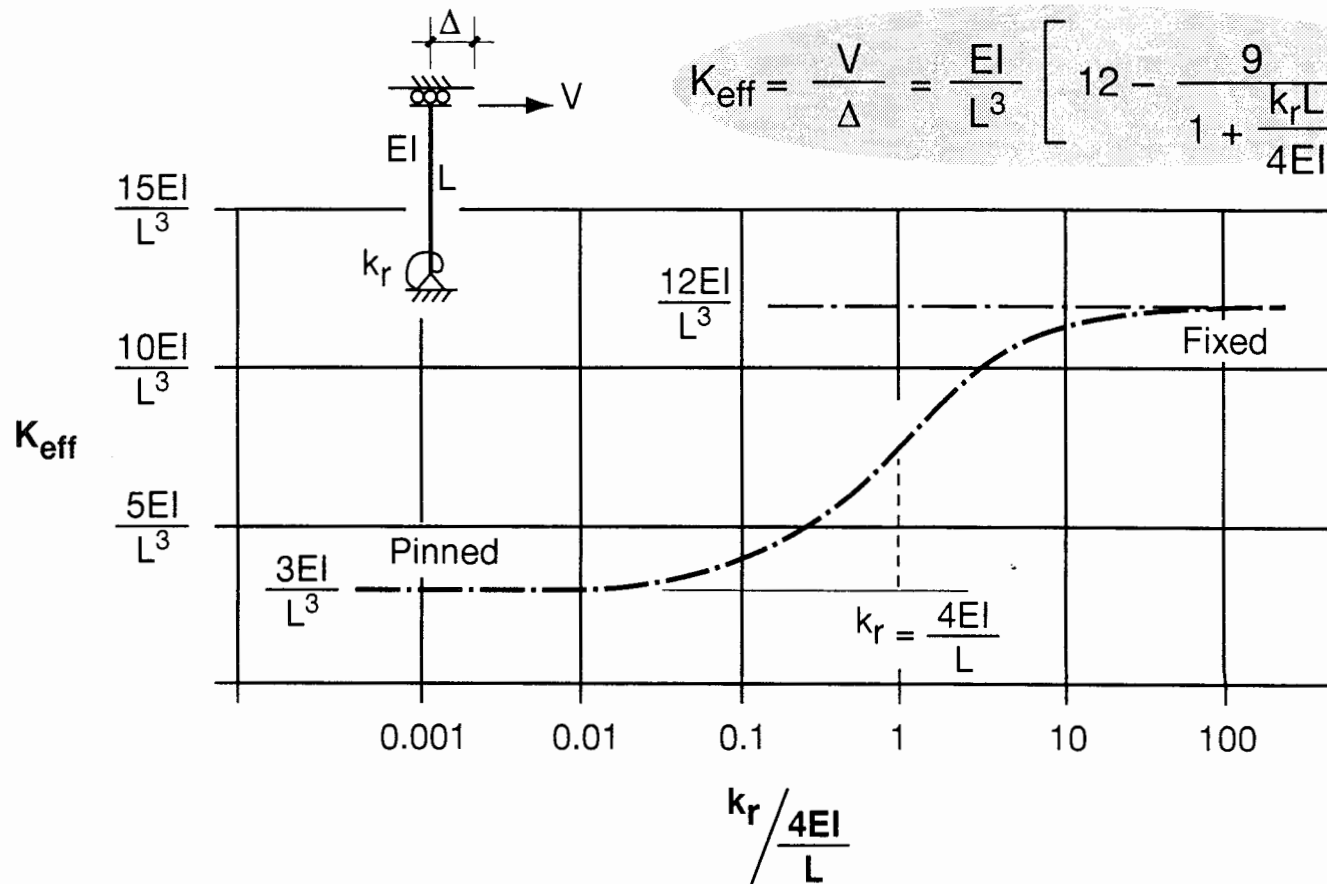
Degree-of-Freedom / Importance



Modeling Foundation Flexibility



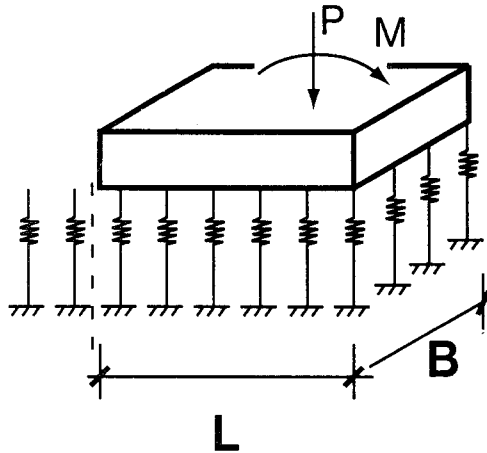
Rotational Flexibility / Fixed or Not?



Determining Foundation Stiffness

- **Elastic Foundation Methods**
- **'Elastic Half-Space' Methods**

Elastic Foundation Method

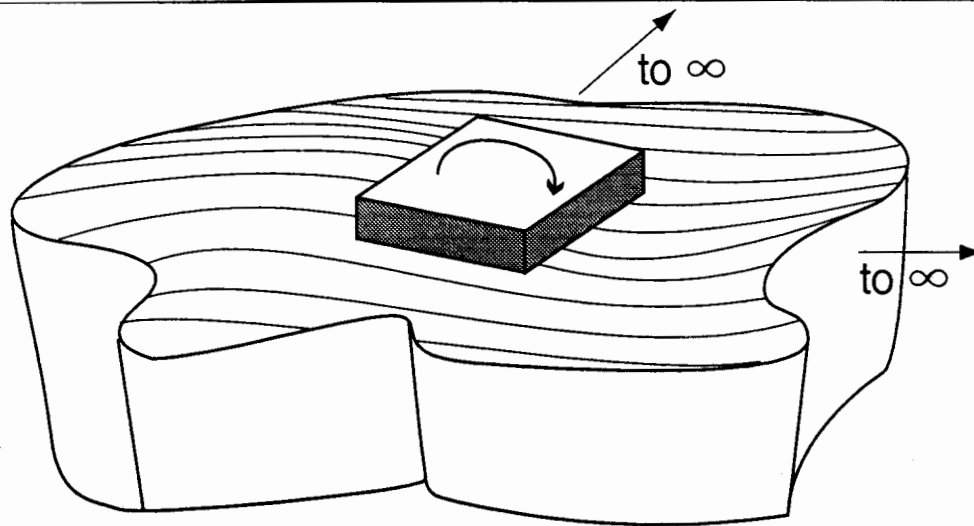


k_s , Subgrade Reaction Coefficient

$$\left(\frac{\text{kip}}{(\text{ft}^2 \text{ of Area})(\text{ft of Deflection})} = k_{cf} \right)$$

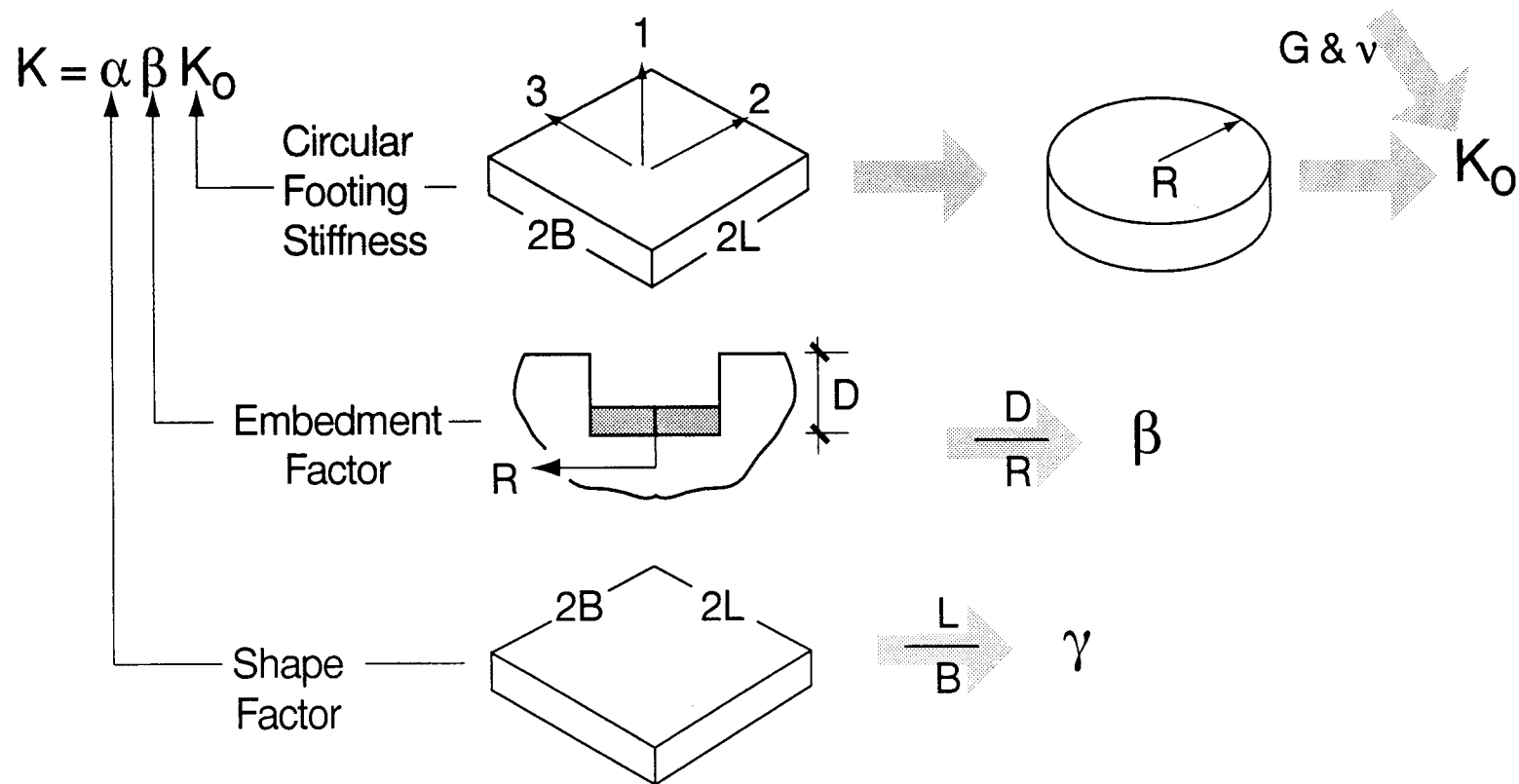
- 'Springs' Are Independent (Winkler Foundation)
- Footing Rigid Relative to Soil
- Rotational Stiffness, $k_r = k_s \frac{L^3 B}{12} \frac{\text{kip ft}}{\text{rad}}$

Half-Space Method



- Footing (Rigid) Bonded to Elastic Half-Space Medium
- Must Use Theory of Elasticity Methods to Determine K's
(Standard Non-Dimensional Solutions)

Half-Space Method for Spread Footings



Adapted from : FHWA-IP-87-6

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UMD-ITV

Seismic Bridge Design Applications
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Stiffness of Circular Surface Footing

Degree of Freedom	Equivalent Radius	Stiffness K_0
Vertical Translation	$R_0 = \sqrt{\frac{4BL}{\pi}}$	$4GR/1 - \nu$
Lateral Translation (Both)	"	$8GR/2 - \nu$
Torsion Rotation	$R_1 = \left[\frac{4BL (4B^2 + 4L^2)}{6\pi} \right]^{1/4}$	$16GR^3/3$
Rocking About 2	$R_2 = \left[\frac{(2B)^3 (2L)}{3\pi} \right]^{1/4}$	$8GR^3/3(1 - \nu)$
Rocking About 3	$R_3 = \left[\frac{(2B) (2L)^3}{3\pi} \right]^{1/4}$	"

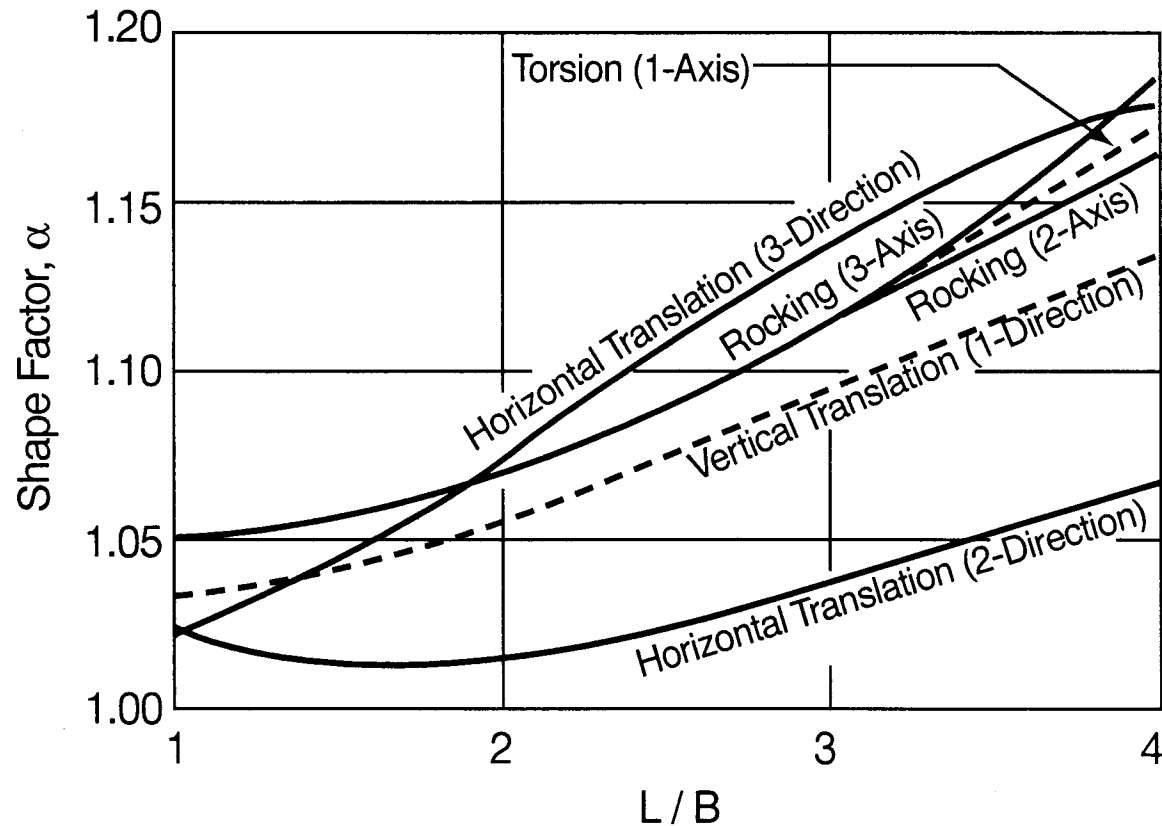
Adapted from: FHWA-IP-87-6

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UMD-ITV

Seismic Bridge Design Applications
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Shape Factor for Rectangular Footing



Adapted from : FHWA-IP-87-6

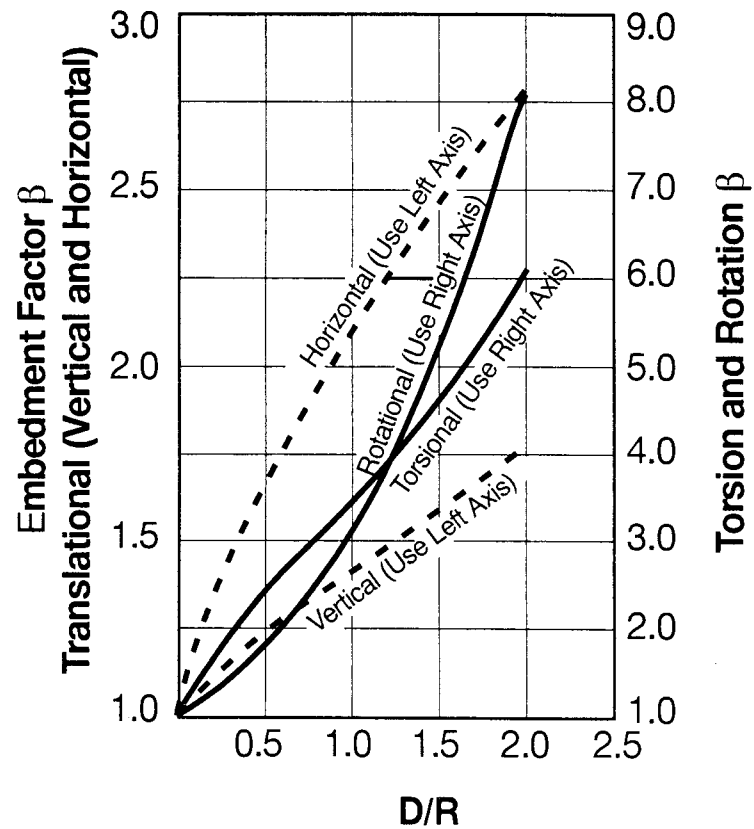
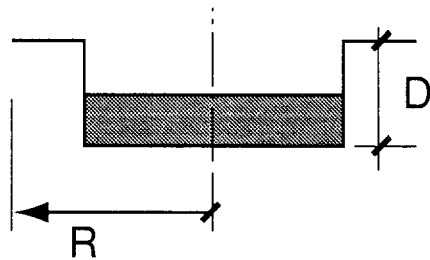
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UMD-ITV

Seismic Bridge Design Applications

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Embedment Factor



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UMD-ITV

Seismic Bridge Design Applications
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Representative* Soil Properties

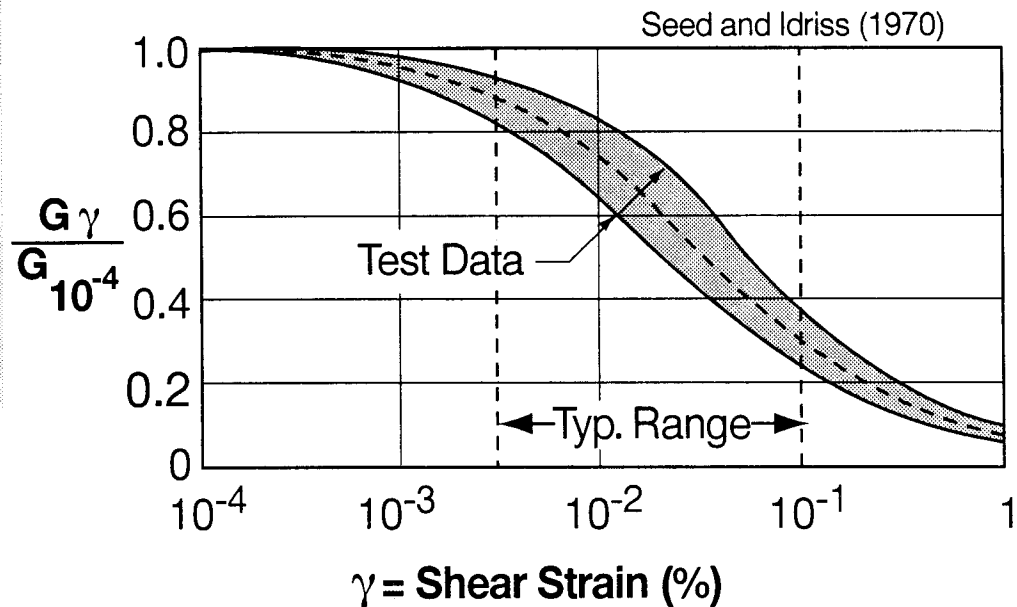
- **Shear Modulus, G**

Material	G(ksi)
Clean dense quartz sand	1.8-3 ⁺
Micaceous fine sand	2.3
Berlin sand (e=0.53)	2.5-3.5
Loamy sand	1.5
Dense sand-gravel	10 ⁺
Wet soft silty clay	1.3-2
Dry soft silty clay	2.5-3
Dry silty clay	5-5
Medium clay	2-4
Sandy clay	2-4

Bowles (1988)

- **Poisson's Ratio** $\nu = 0.3$ Cohesionless
 $\nu = 0.4 - 0.5$ Cohesive

- **Shear Modulus vs. Strain**



* Consult Your Geotech!

Example / Rocking Stiffness / Half-Space

- Consider Practice Problem No. 1

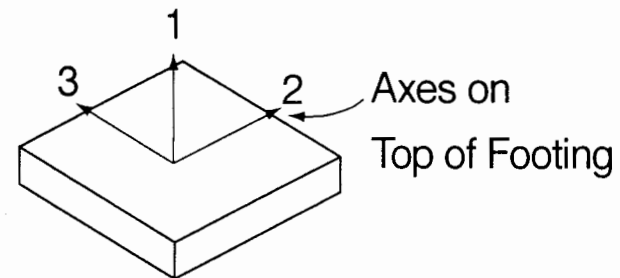
Footing: $2B = 2L = 15 \text{ ft}$ $D = 6 \text{ ft}$

Soil: From Geotechnical Engineer, $G = 400 \text{ ksf}$ $\nu = 0.3$

Rotational

Stiffness: $K_{r3} = \alpha \beta K_0$

(Rocking About Axis 3)



Example / Rocking Stiffness (continued)

- Equivalent Radius, $R_3 = \left[\frac{(15)(15)^3}{3\pi} \right]^{1/4} = 8.56 \text{ ft}$
- Rocking, $K_0 = \left[\frac{8(400)(8.56)^3}{3(1 - 0.3)} \right] = 955,600 \frac{\text{kip ft}}{\text{rad}}$
- Shape Factor, $\alpha \quad \frac{L}{B} = 1 \rightarrow \alpha = 1.05$
- Embedment Factor, $\beta \quad \frac{D}{R} = \frac{6}{8.56} = 0.70 \rightarrow \beta = 2.3$

Example / Rocking Stiffness (continued)

- $K_{r3} = \alpha\beta K_0 = 1.05(2.3) 955,600 = 2,308,000$
 $\frac{\text{kip ft}}{\text{rad}}$
- How Important Is This Stiffness on the Lateral Behavior of the Structure?

Column Properties

$$E = 518,400 \text{ ksf}$$

$$I = 3.98 \text{ ft}^4$$

$$H_{\text{clr}} = 25.33 \text{ ft}$$

$$K_{\text{eff}} = \frac{EI}{H^3} \left[12 - \frac{9}{1 + \frac{K_r L}{4EI}} \right]$$

$$\frac{K_{\theta 3} H}{4EI} = 7.08 \quad \Rightarrow \quad K_{\text{eff}} = 10.9 \frac{EI}{H^3}$$

vs. 12! \therefore Essentially Fixed

Example / Footing Rocking – Practice No. 1

- Effective Longitudinal Stiffness Including Rocking

$$K_{\text{eff}} = 3 \left(10.9 \frac{EI}{H^3} \right) = 4146 \text{ kip/ft}$$

- Previously in Practice No. 1 $K = 3639 \text{ kip/ft}$ (Top Half of Footing Included with I_{col} to Approximate Footing Flexibility)
- New Results

$$T = 1.20 \text{ sec (vs. 1.28 sec)}$$

$$C_s = 0.192$$

$$V = 928 \text{ kip}$$

$$\Delta_{\text{long}} = 2.7 \text{ in vs. } \begin{cases} 2.9 \text{ in with } I_g \\ 4.6 \text{ in with } I_g/2 \end{cases}$$

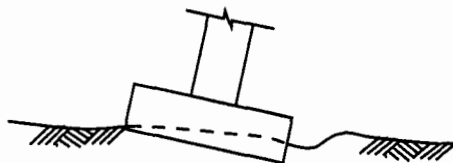
Session 1

Spread Footings

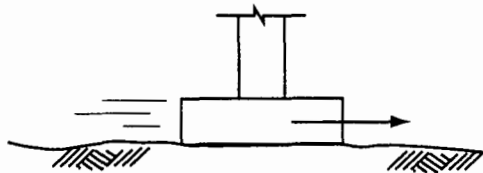
- **Including Flexibility**
- **Overturning and Sliding**
- **Pinned Base Columns**

Spread Footing Failure Modes

- **Soil Failure**



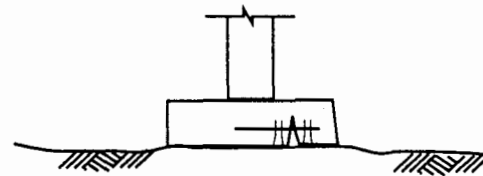
**Soil Bearing Failure
(Overturning)**



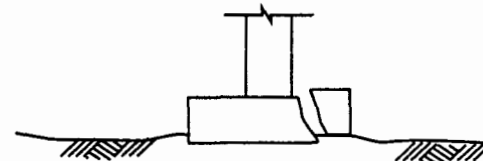
Sliding Failure

- **Footing Failure**

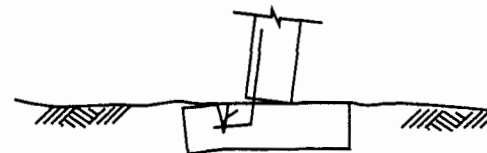
(All Types Aggravated by Large Overturning)



Flexural Yielding of Reinforcing



Concrete Shear Failure



Anchorage Failure

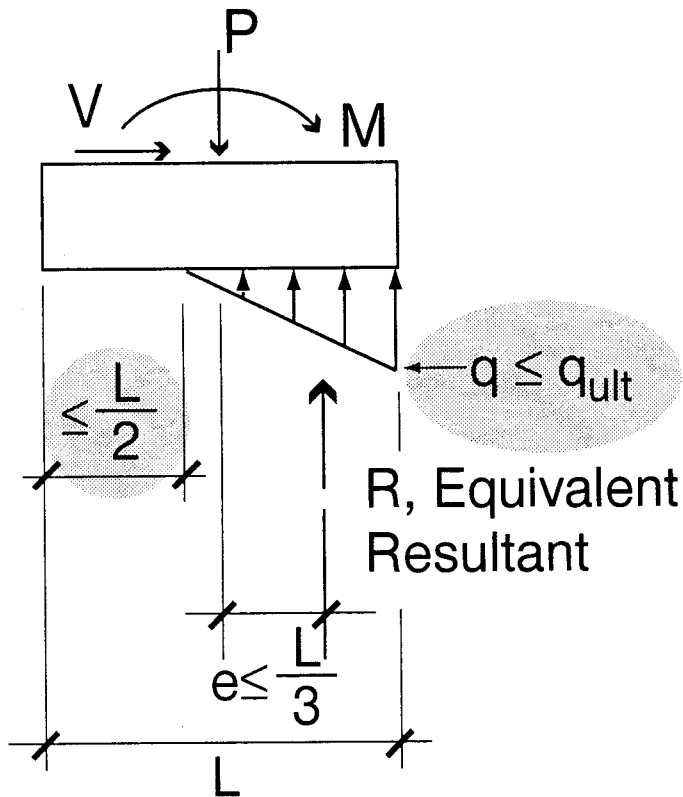
Overturning

Division I-A, Articles 6.4.2(B) and 7.4.2(B)

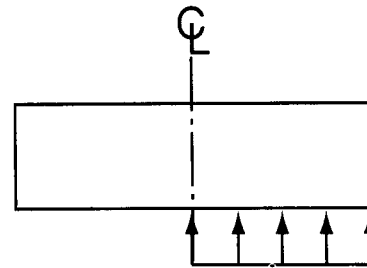
“Because of the dynamic cyclic nature of seismic loading, the ultimate capacity of the foundation medium should be used ...”

“Transient foundation uplift or rocking involving separation ... up to one-half of ... pile group or ... contact area is permitted ... provided that ... soils are not susceptible to loss of strength ...”

Overturning Comparisons



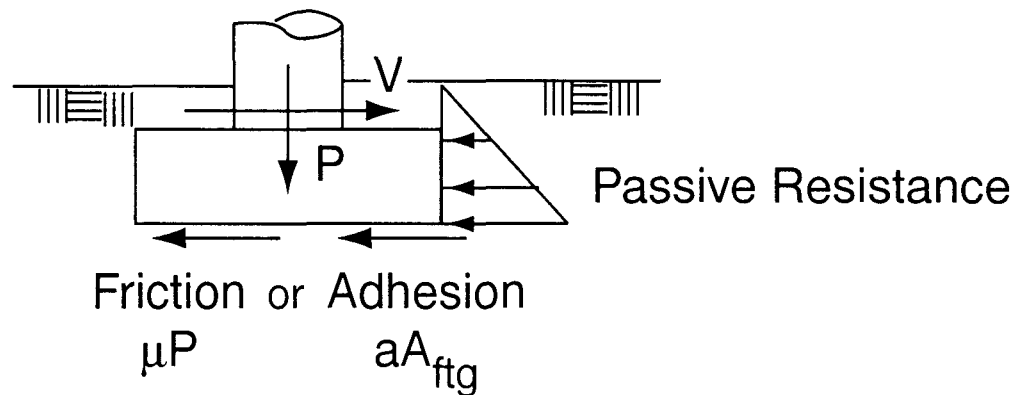
- Triangular Stress Distribution
Recommended for Now
- Rectangular Stress Distribution



Under Development,
Better Correlation with
Test Results?
Better for Soft Soils?

Sliding

- Make Comparisons at Impending Sliding Condition
- Neglect Passive Resistance? (Consult Your Geotech)
- If Soil Is Adhesive, Use Larger of Friction or Adhesion
- Consider Jointing Effect in Rock



Representative* Ultimate Values of Coefficient of Friction for Concrete Foundations on Rock / Soil

Material	Relative Density/ Consistency	Coefficient of Friction ¹	Adhesion ¹ (PSF) ²
Clean, Sound Rock ³	Not Applicable	0.70 - 0.80	—
Clean Gravel, Gravel-Sand Mixtures	Dense to Very Dense Medium Dense	0.55 - 0.70 0.55 - 0.65	—
Clean to Slightly Silty / Clayey Sand with or without Gravel	Dense to Very Dense Medium Dense	0.45 - 0.60 0.45 - 0.55	— —
Silty / Clayey Sand and Sandy Silt with or without Gravel	Dense to Very Dense Medium Dense	0.40 - 0.55 0.35 - 0.50	— —
Silty Clay and Clayey Silt with or without Sand and Gravel (low plasticity) ⁴	Very Stiff to Hard Medium Stiff to Stiff	0.40 - 0.50 0.30 - 0.45	1000 - 1500 500 - 1000

(After Potyondy, 1961; Goh and Donald, 1984; U.S. Department of the Navy, 1986) For Notes 1 through 4, See Design Example No. 3

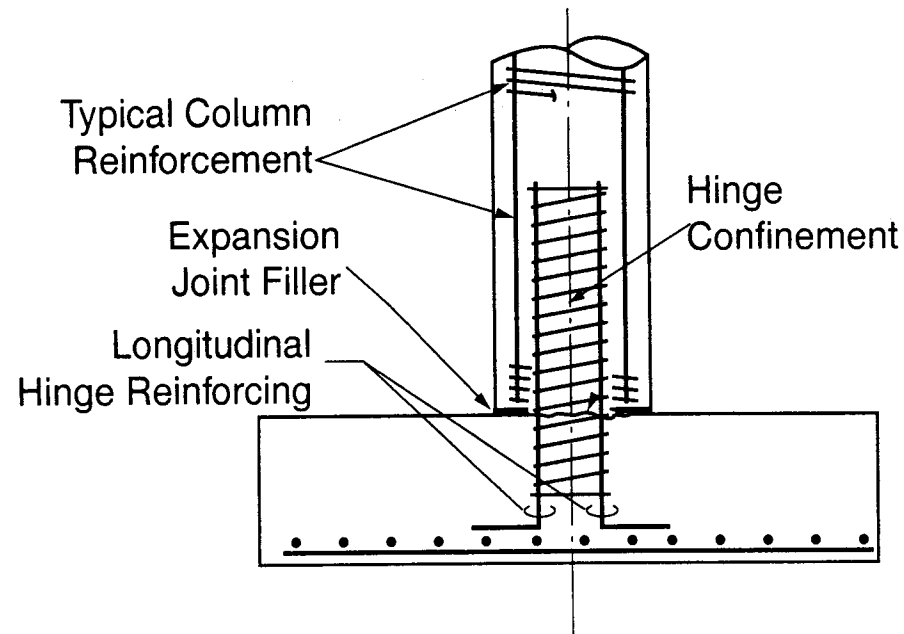
* Consult Your Geotechnical Engineer

Session 1

Spread Footings

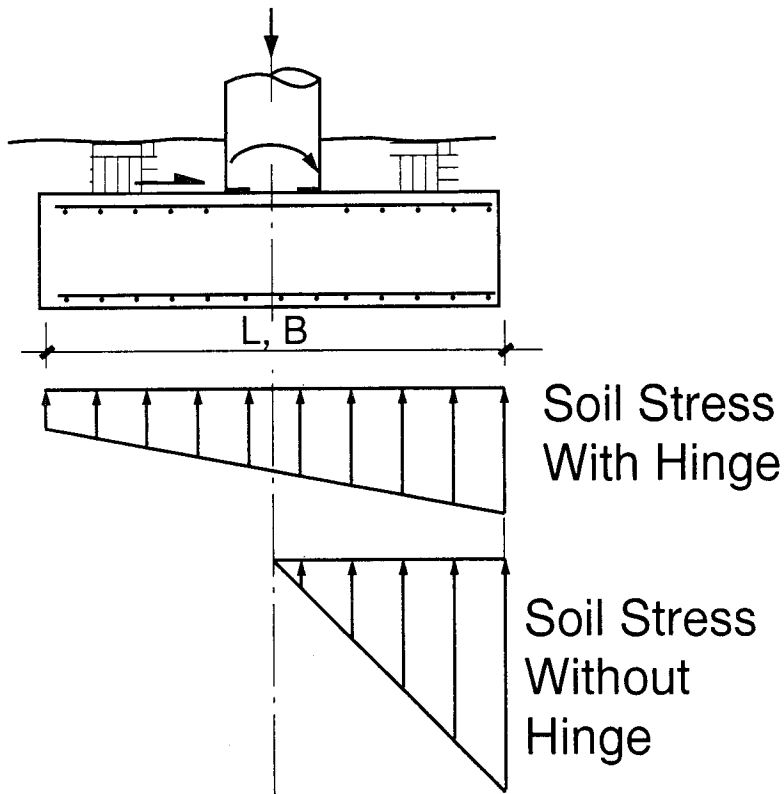
- **Including Flexibility**
- **Overturning and Sliding**
- **Pinned Base Columns**

Limiting the Moment Transferred to a Footing



**Seismic
Hinge Detail**

Effects of Limiting Foundation Moments



With a Hinge:

- Soil Contact Stress Lower
- Internal Forces Lower
- Structure More Flexible (Displacements Larger)
- Can Reduce Footing Size
- May Increase Column Size

Design of Pinned Bases

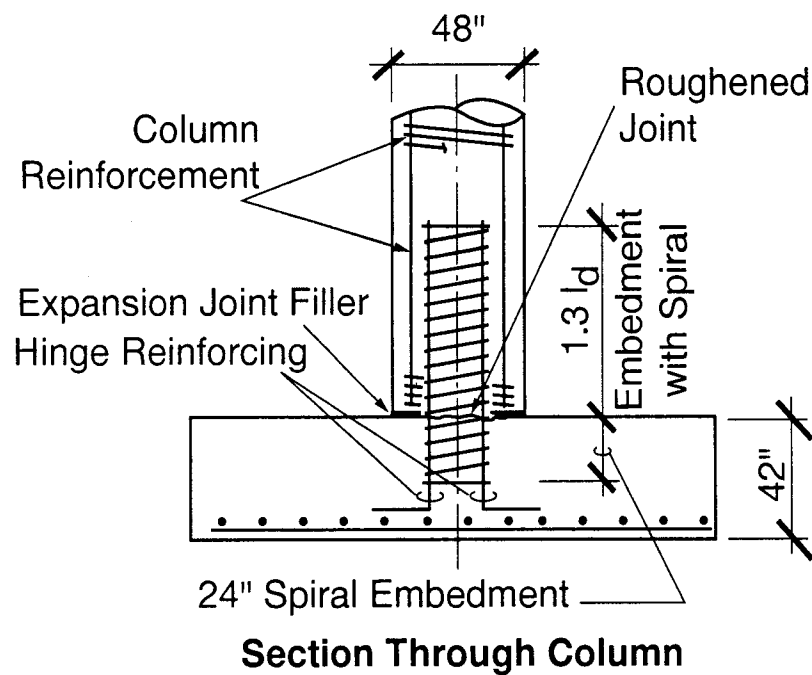
- Use 1/2 in. or More Expansion Joint Filler for Rotation Capacity
- Size Contact Area Using Shear Friction
- Ensure Area Can Carry Group VII Loads Based on

$$\phi P_o = 0.85\phi f'_c (A_g - A_{st}) + A_{st} f_y$$

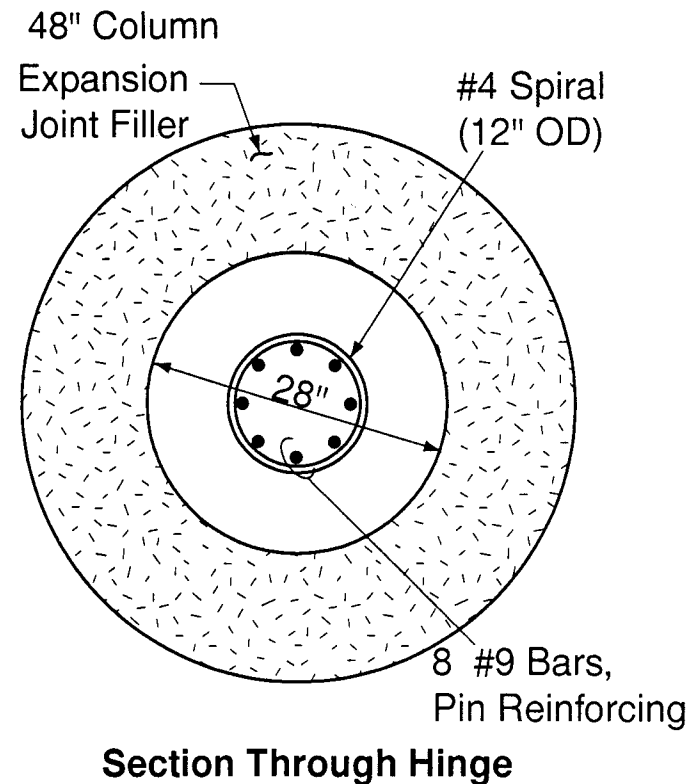
Caltrans (1995)

- Centralize Longitudinal Steel to Minimize Actual Moment
- Develop Longitudinal Steel on Both Sides of Hinge
- Use a Nominal Spiral Over Half the Column Dimension
Above and Below Hinge

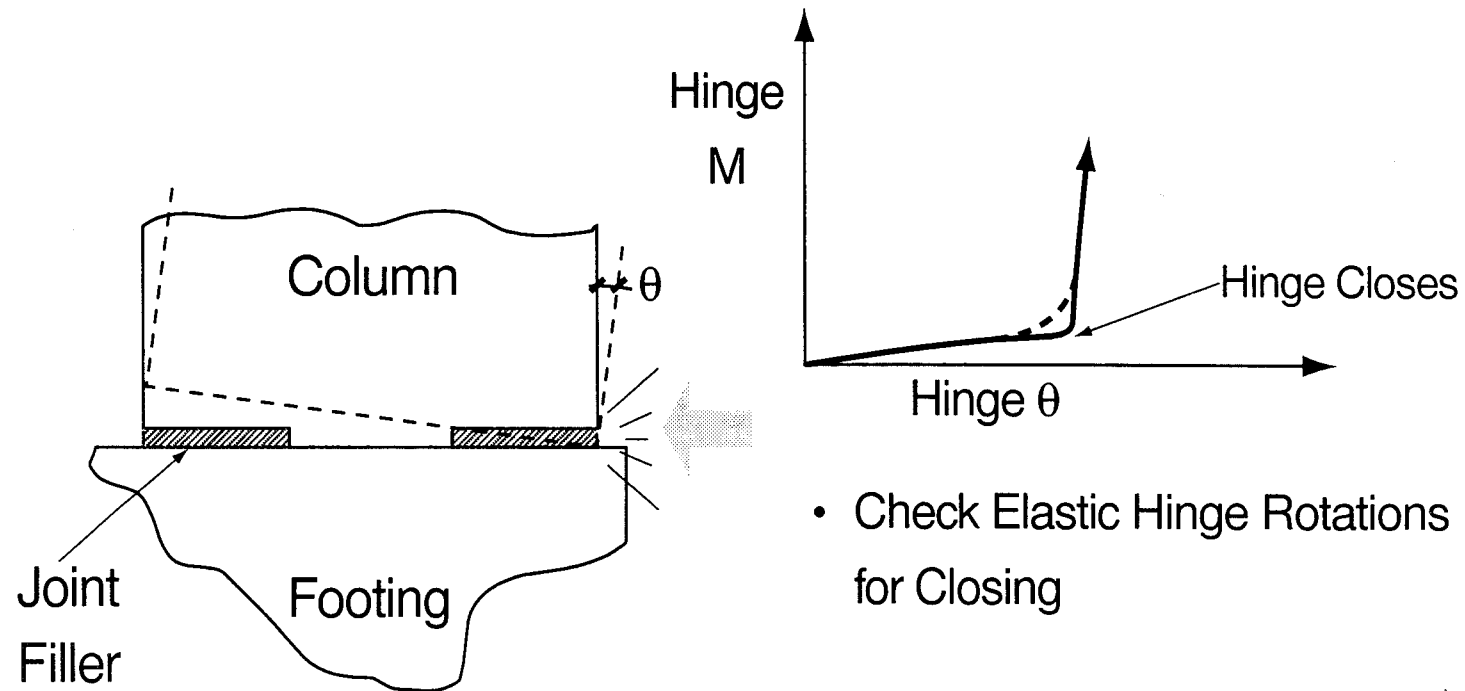
Example Detailing / 4 ft Diameter Column



Reference: Design Example No. 4



Limit Behavior / Pinned Base Columns

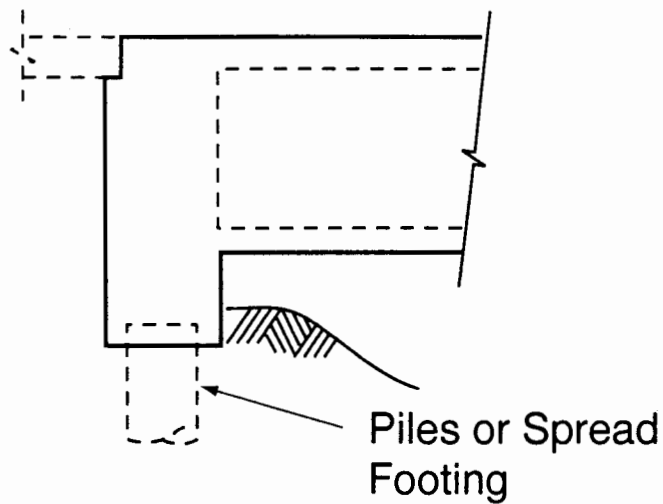


Session 2

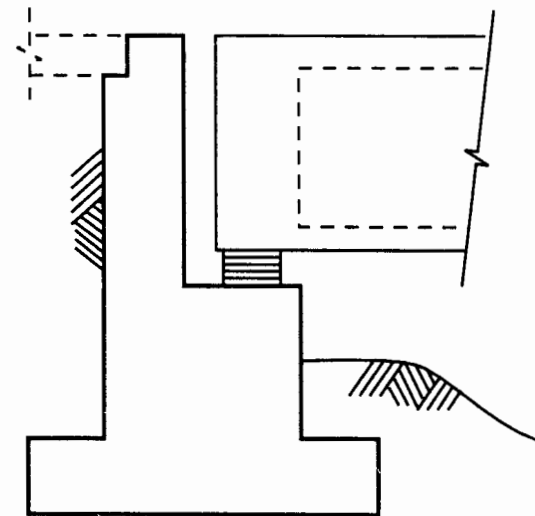
Concrete Box Girder Bridge Example Abutments

- **Conceptual Behavior**
- **Modeling Soil Flexibility**
- **Nonlinear Effects**
- **Mononobe-Okabe Analysis**
- **Design Issues, Force Transfer,
and Fuse Elements**

Types of Abutments

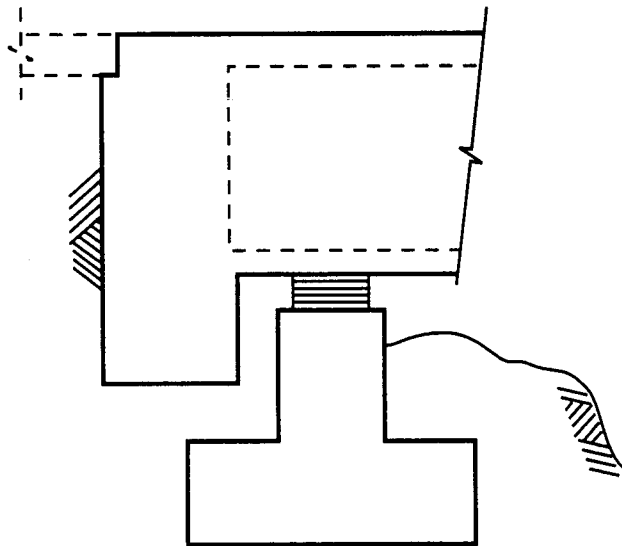


Integral Abutment
(Monolithic)

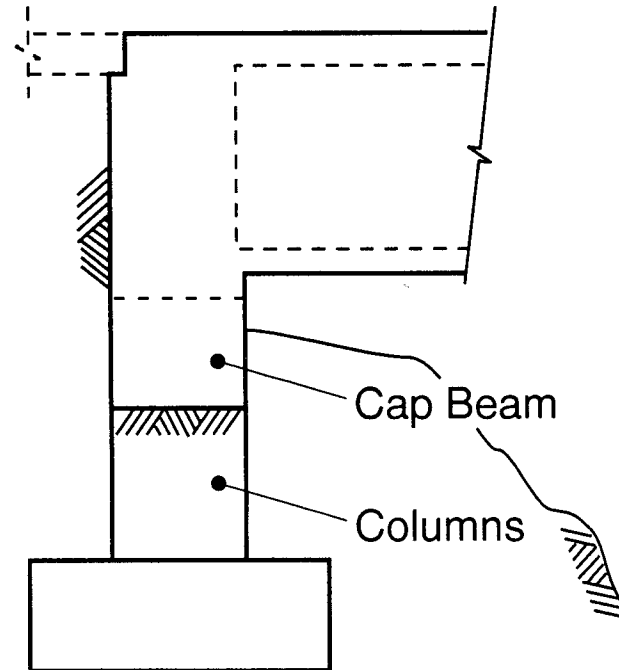


Seat Abutment
(Free-Standing)

Variations of the Integral Abutment



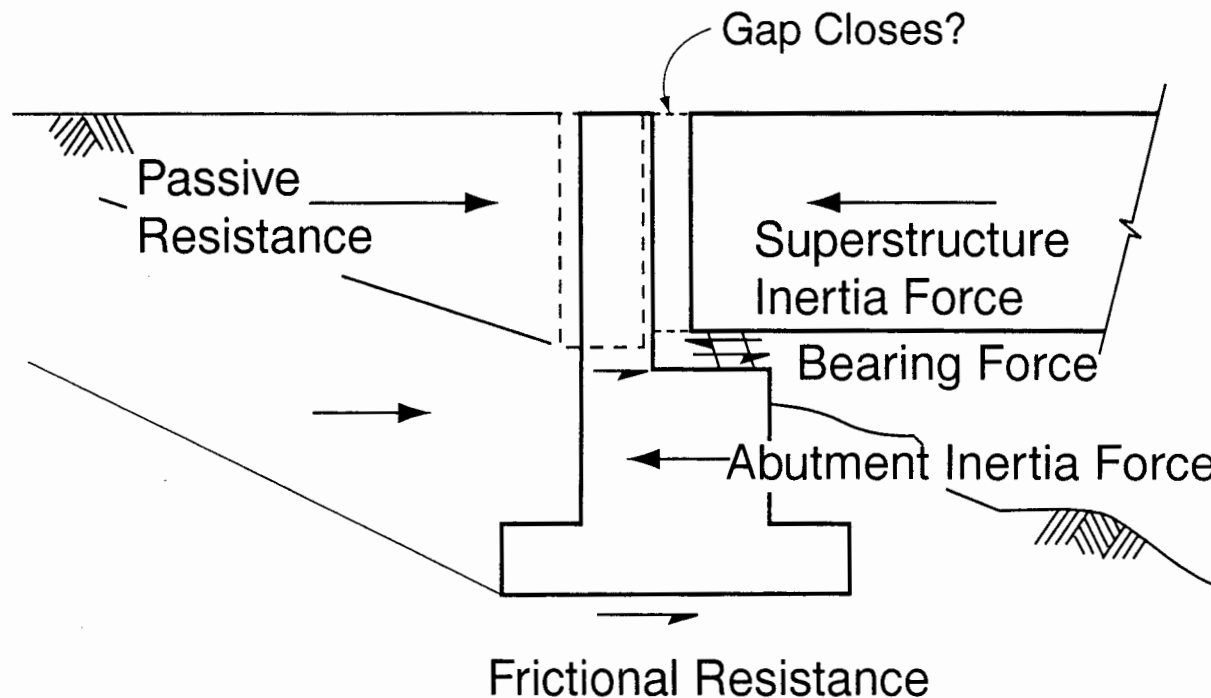
Stub Abutment
(Semi-Integral)



Spill-Through Abutment

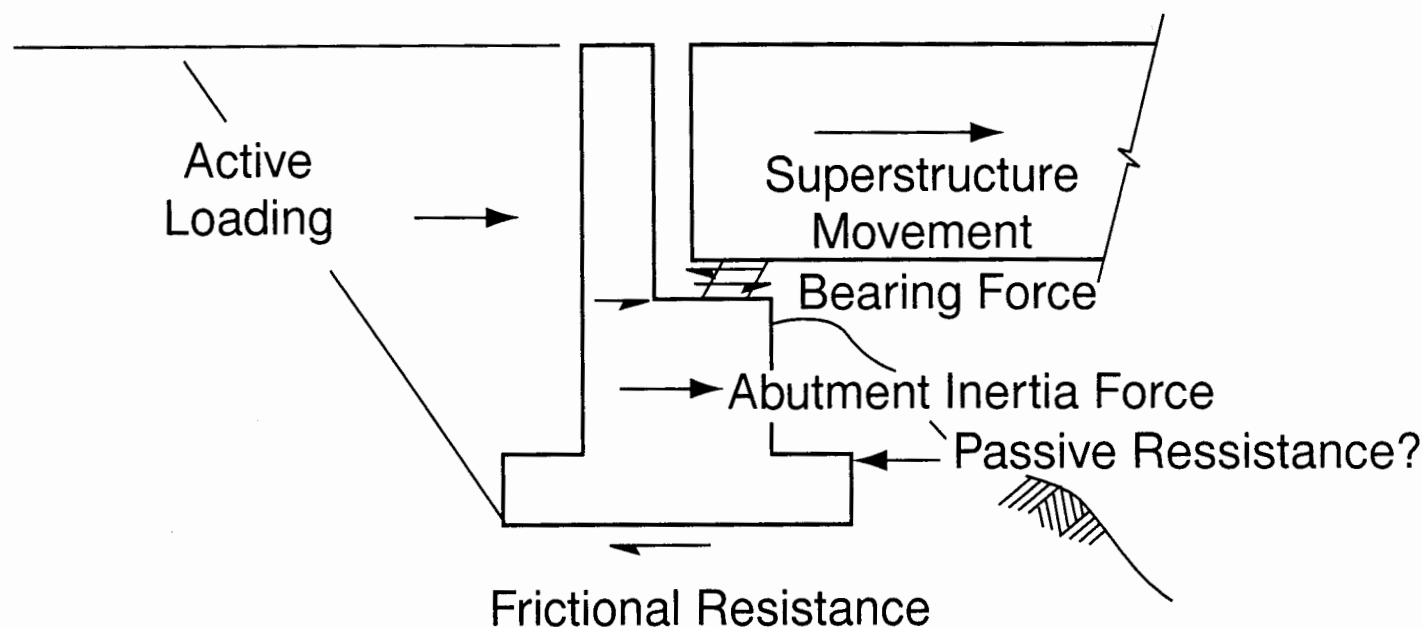
Seat Type / Longitudinal Behavior

Superstructure Moves **Toward** Backfill



Seat Type / Longitudinal Behavior (continued)

Superstructure Moves **Away** from Backfill

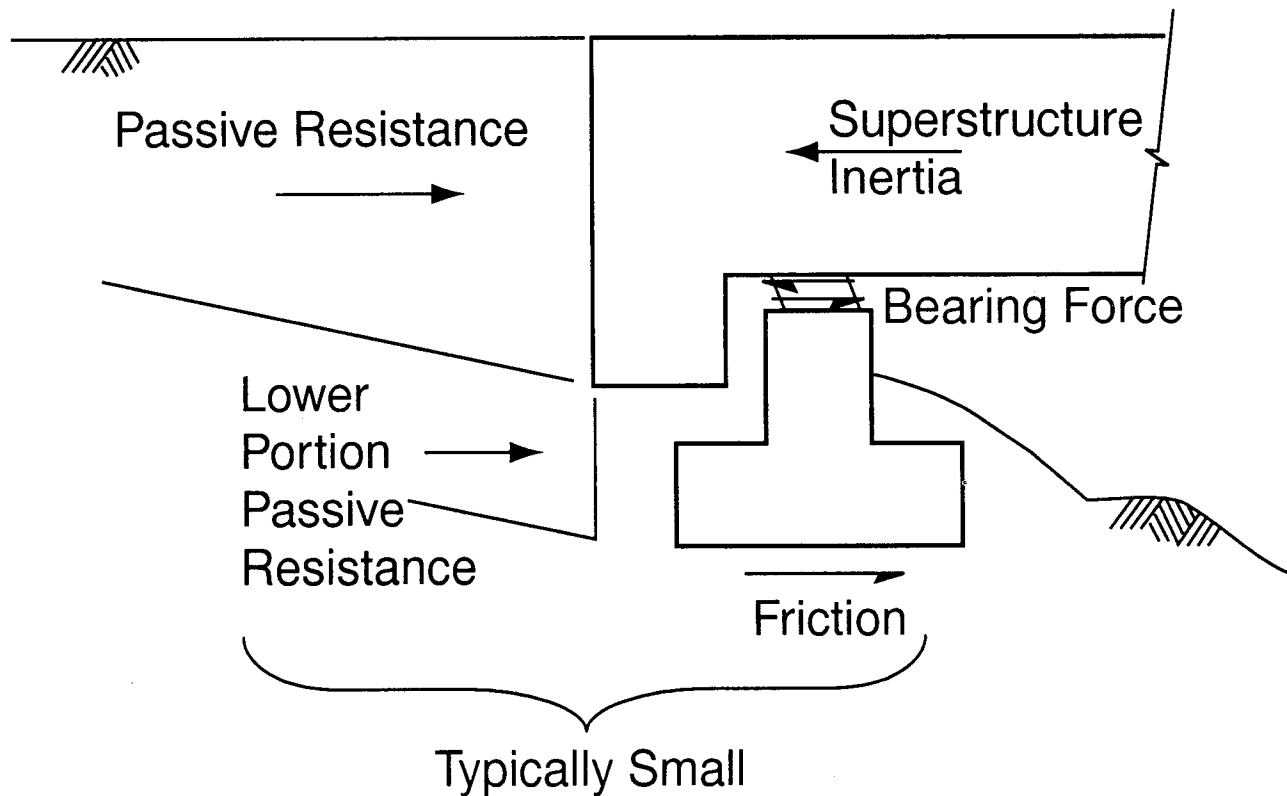


Cannot Mobilize Passive Resistance Until Batter Pile Softens or Backwall Fails (Yields)

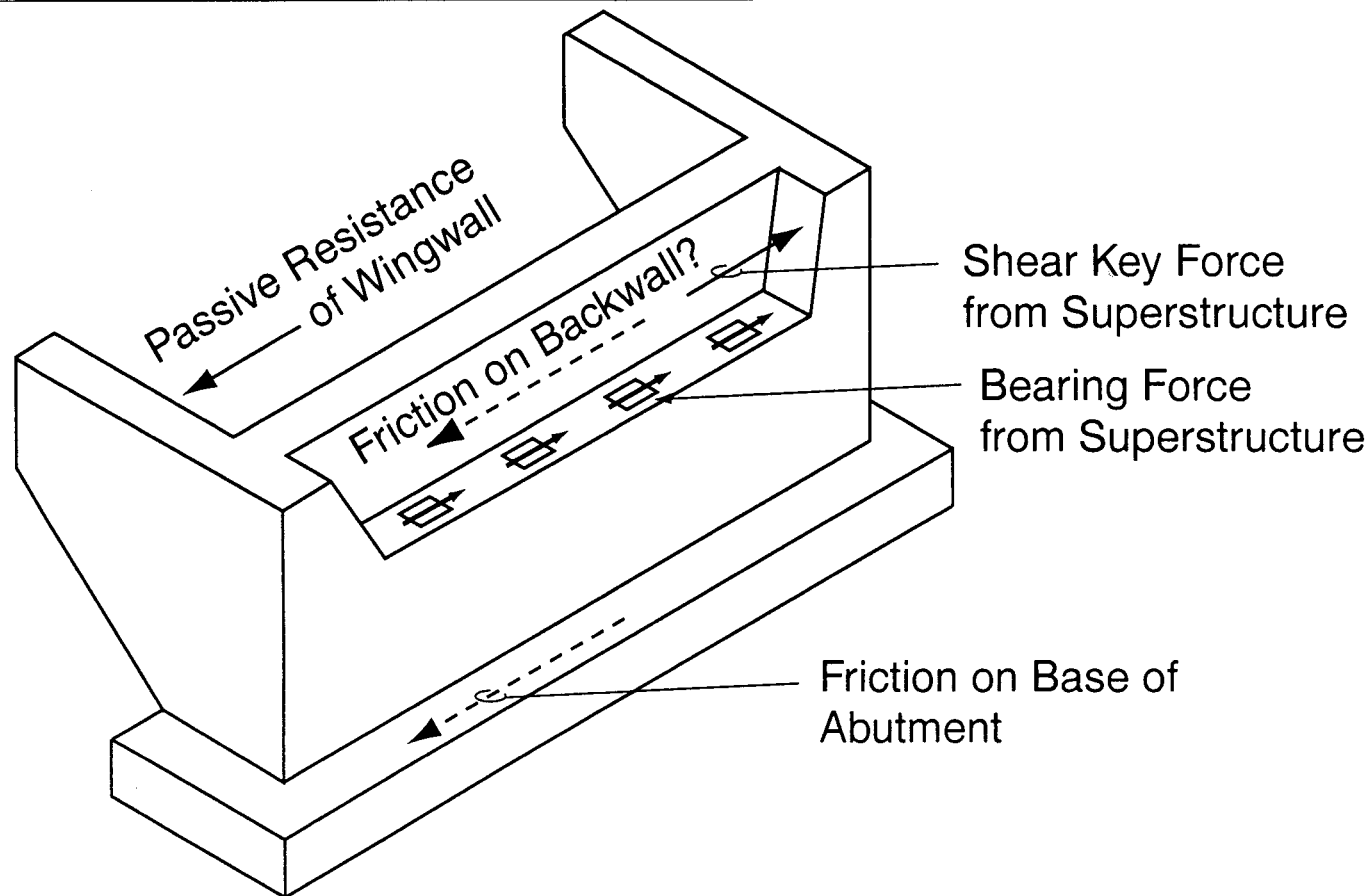
Axial Component Greatly Stiffens System

The diagram shows a cross-section of a structure with a batter pile. A horizontal arrow indicates a lateral load. A vertical line with a question mark represents the backwall. A dashed line indicates the failure mechanism. A horizontal arrow at the base of the pile indicates the axial component of the load. A diagonal arrow indicates the axial component of the load. A horizontal arrow at the base of the pile indicates the axial component of the load. A diagonal arrow indicates the axial component of the load.

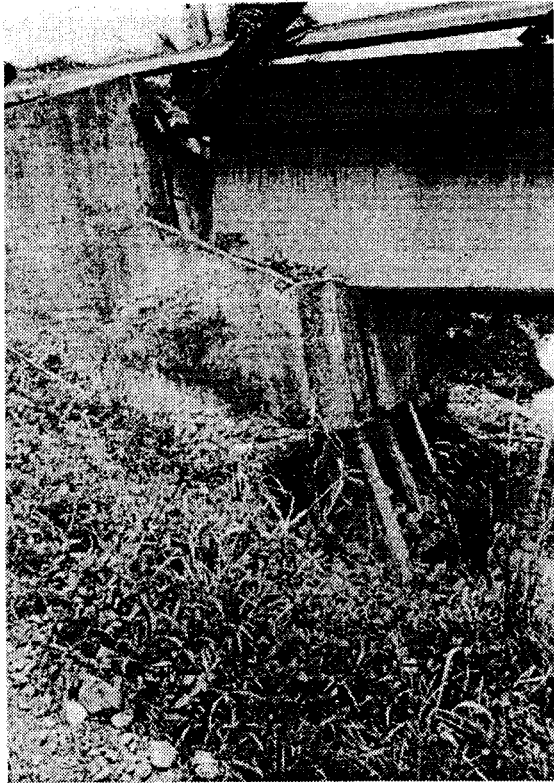
Integral Type / Longitudinal Behavior



Transverse Behavior

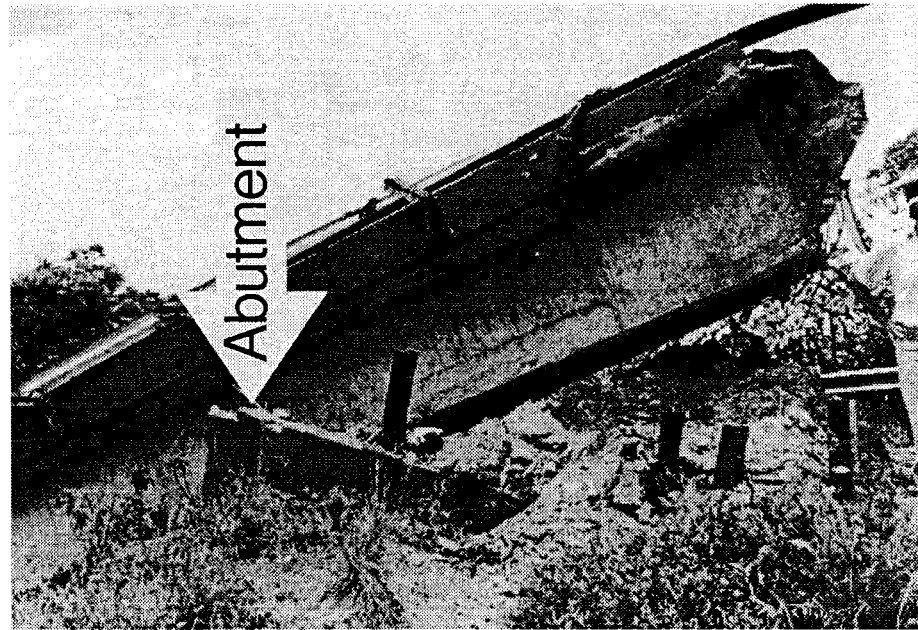


Abutment Damage



**Abutment Slumping
and Rotation**

Costa Rica, 1991



Passive Failure

Priestley, Seible, Calvi (1996)

Session 2 Page 9 of 45

UMD-ITV

Seismic Bridge Design Applications
25 July 1996, NHI Course Code No. 13063

Session 2

Abutments

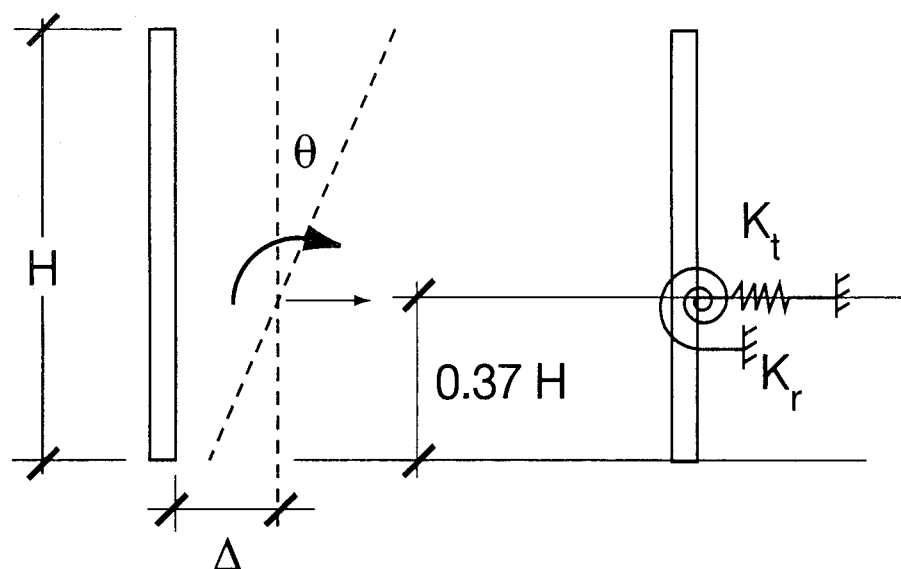
- Conceptual Behavior
- **Modeling Soil Flexibility**
- Nonlinear Effects
- Mononobe-Okabe Analysis
- Design Issues, Force Transfer, and Fuse Elements

Methods of Determining Stiffness

- Elasticity — FHWA / RD-86 / 101 (1986)
- Empirical — Caltrans

Focus on Elastic Stiffness First, Then Incorporate
Nonlinear Behavior

FHWA Method



$$K_t = 0.425 E_s B$$

$$K_r = 0.072 E_s B H^2$$

E_s = Elastic Modulus of
Backfill

B = Width of Wall

H = Height of Wall

FHWA (1986)

Session 2 Page 12 of 45

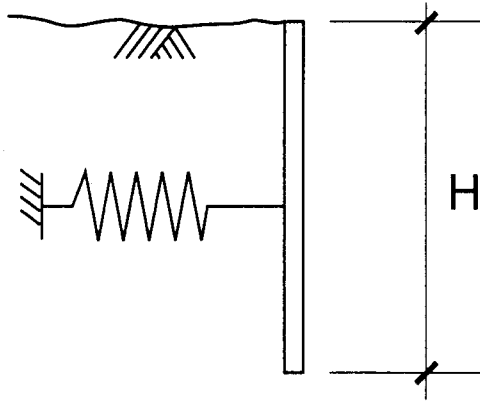
UMD-ITV

Seismic Bridge Design Applications

25 July 1996, NHI Course Code No. 13063

Caltrans Method

- **Basic Stiffness**



$$K_{\text{abut}} = 200 \frac{\text{kip/in.}}{\text{ft of Width}}$$

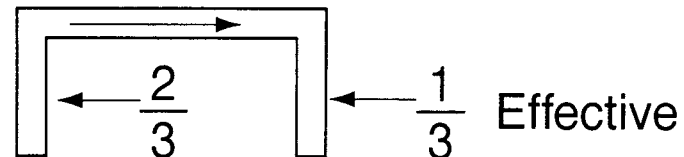
(8 ft High Wall)

- **Wall Height $\neq 8$ ft**

Linearly Prorate

- **Wingwalls**

Assume $\frac{2}{3}$ Effective into Backfill,
and $\frac{1}{3}$ Effective Away from Backfill



Caltrans Method (continued)

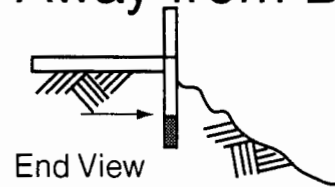
- Maximum Soil Capacity = 7.7 ksf (Passive)

Based on

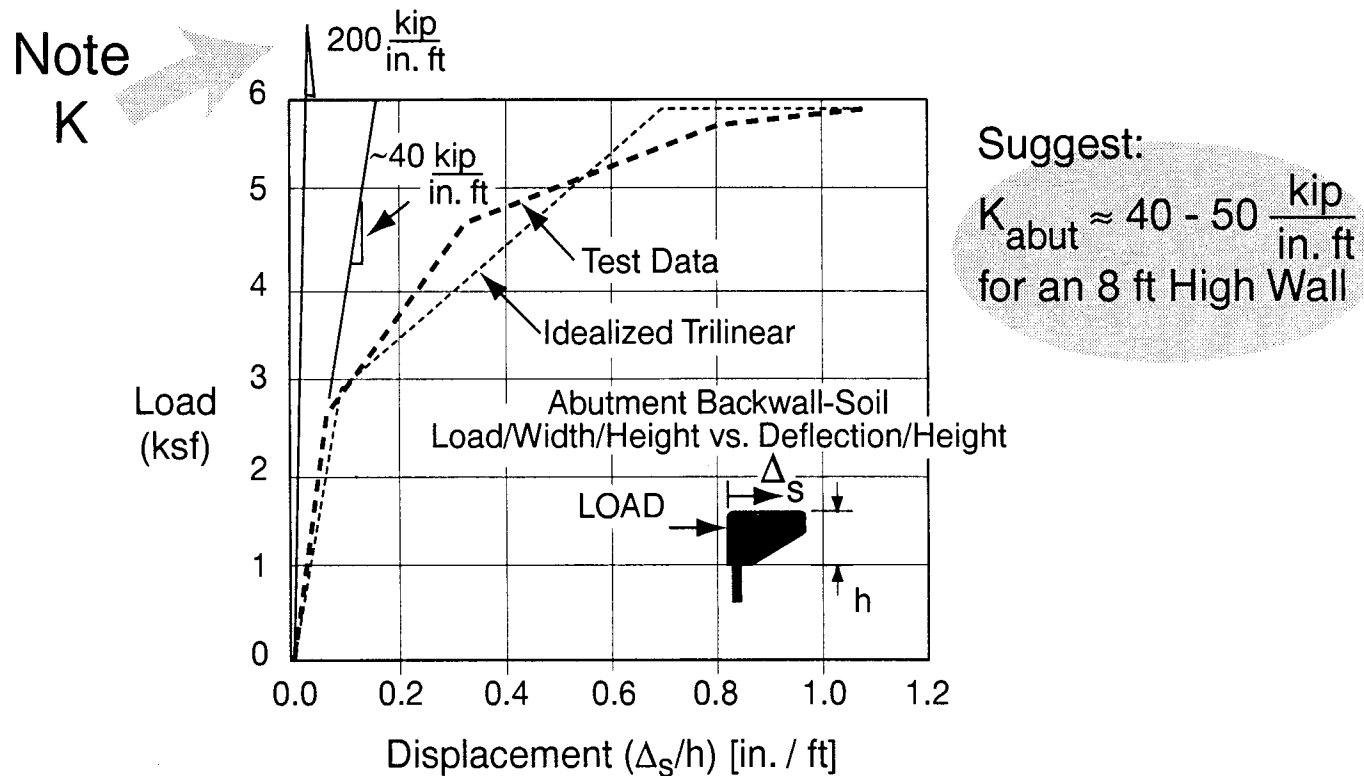
- Properly Compacted and Drained Backfill
- Maximum Static = 5.0 Amplified by 1/0.65 for Dynamic Effects

- Thoughts on Wingwalls
 - Effectiveness Acting Away from Backfill

$\frac{1}{3}$ → 0 ?



Test Data / Large Scale Abutment Tests



Priestly, Seible, Calvi, 1996

A cross-sectional diagram of a bridge structure. The diagram shows a central pier with a footing, a wingwall, and a barrier. The total width of the structure at the top is 20'-0". The height of the barrier is 3'-0". The height of the wingwall is 15'-0". The height of the pier is 3'-0". The width of the pier is 4'-0". The width of the footing is 8'-0". A dashed line indicates the approximate soil line. Labels include: Footing, Barrier, Wingwall, Approximate Soil Line, 20'-0", 3'-0", 15'-0", 3'-0", 4'-0", and 8'-0".

Diagram illustrating the cross-section of a bridge structure, showing the following components and dimensions:

- Back of Pavement Seat:** The uppermost horizontal surface.
- Bearing:** The component supporting the bridge deck.
- End Diaphragm:** The vertical structure on the left side.
- Stub Abutment:** The vertical structure supporting the bearing.
- Footing:** The base foundation.

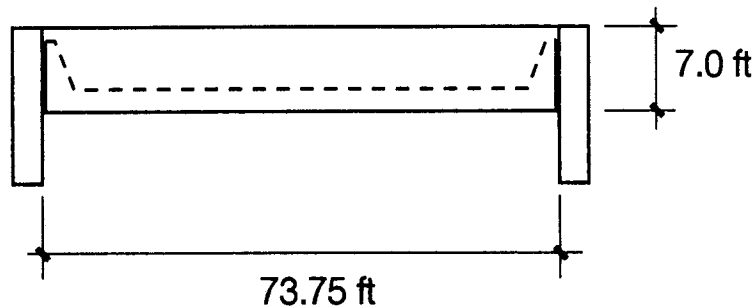
Dimensions (in feet and inches):

- Top width: 3'-6"
- End Diaphragm width: 7'-0"
- Distance from End Diaphragm to Bearing: 1'-3"
- Distance from Bearing to Stub Abutment: 1'-9"
- Stub Abutment width: 1'-9"
- Distance from Stub Abutment to Footing: 3'-0"
- Footing width: 8'-0"
- Overall height: 15'-0"
- Distance from Back of Pavement Seat to Bearing: 5'-8"

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UMD-ITV
Seismic Bridge Design Applications
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Example / Abutment Stiffness (continued)

Assume the Following Geometry Between the Wingwalls



- Caltrans $K_{\text{abut}} = 40(73.75) \frac{7}{8} (12) = 30,975 \text{ kip/ft}$
 $\frac{\text{kip/in.}}{\text{ft}}$

Example / Effect of Abutment Stiffness On Seismic Forces

- Recall $K_{\text{bent}} = 3639 \text{ kip/ft}$
 $W = 4842 \text{ kip}$
 - New Stiffness (Caltrans) $K_{\text{total}} = K_{\text{bent}} + K_{\text{abut}}$
 $K_{\text{total}} = 34,614 \text{ kip/ft}$
 - New Values $V = 1816 \text{ kip}$
 $\Delta = 0.63 \text{ in.}$
- Session 1
Consider One Abutment Acts at a Time
- 191 kip to Bent vs. 886 kip Before!
1625 kip to Soil

Example / Check of Abutment Behavior

- Determine Backfill Pressure

$$p = \frac{1625}{7(73.75)} = 3.15 \text{ ksf} < 7.7 \text{ ksf Capacity}$$

∴ OK!

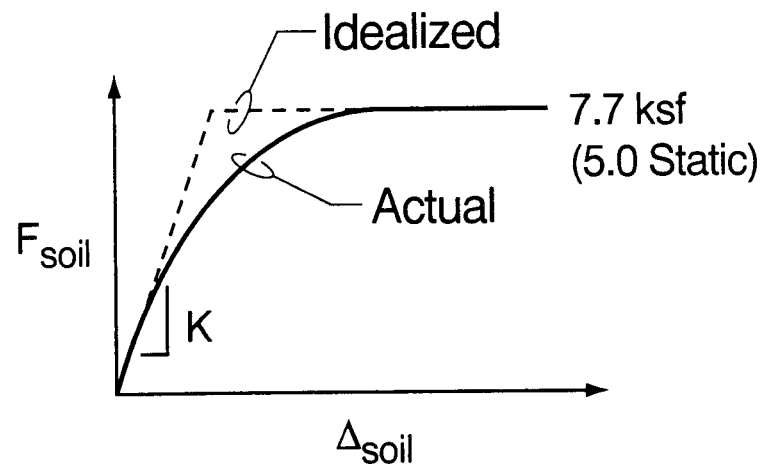
Soil Can Withstand Forces
in Longitudinal Direction

Session 2

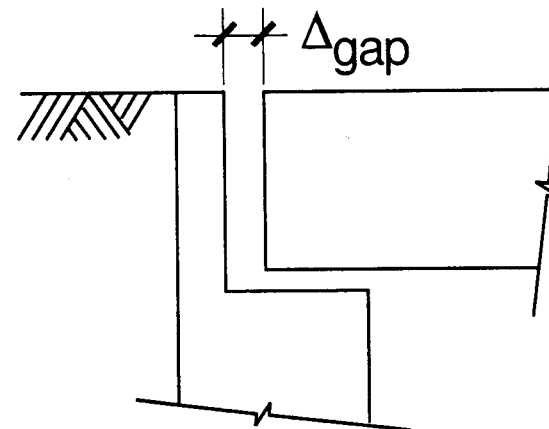
Abutments

- Conceptual Behavior
- Modeling Soil Flexibility
- **Nonlinear Effects**
- Mononobe-Okabe Analysis
- Design Issues, Force Transfer, and Fuse Elements

Sources of Nonlinearity

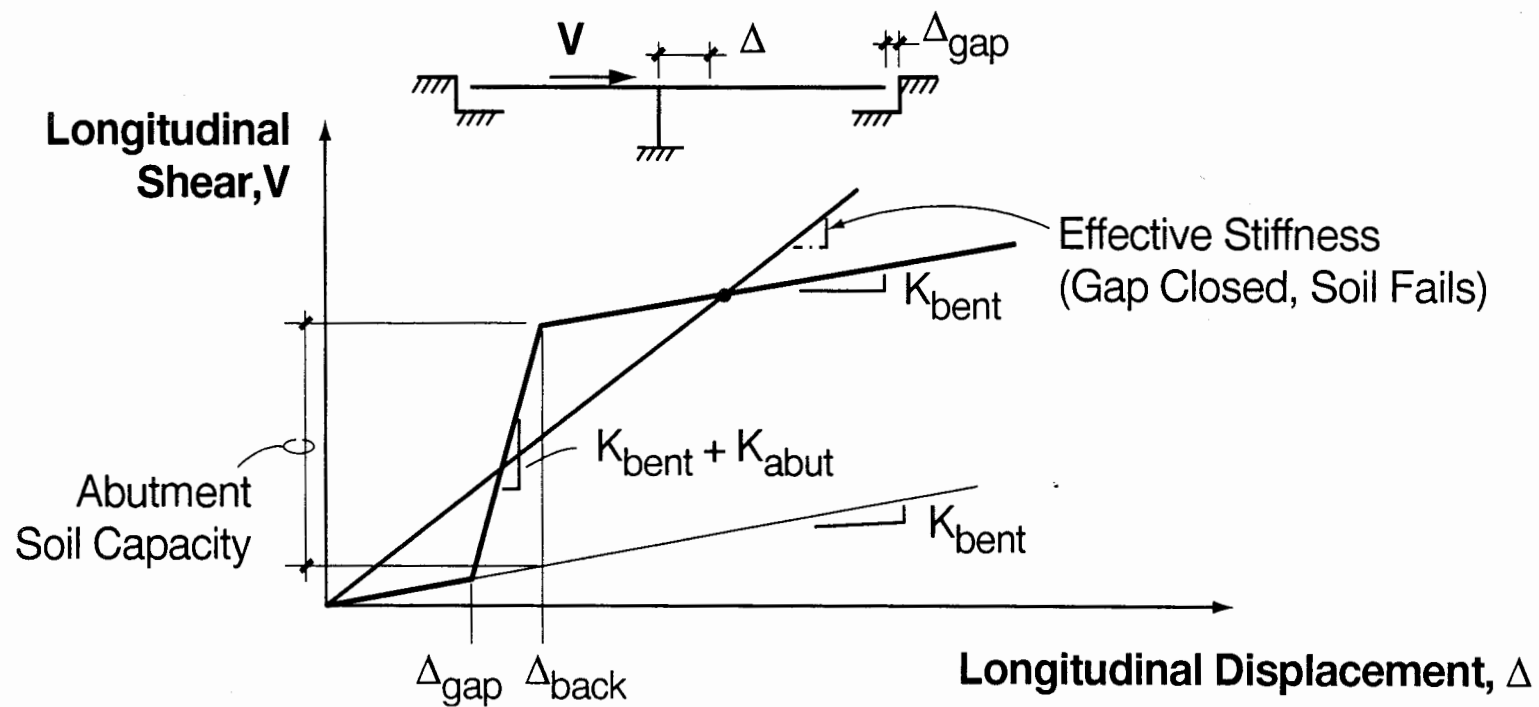


Soil Behavior



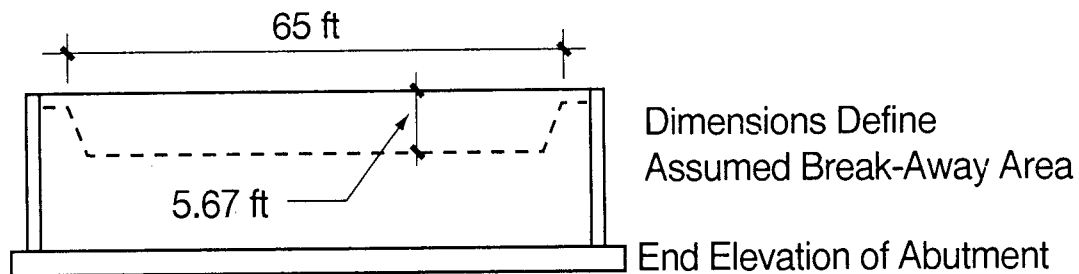
Movement Joints

Overall Structure Stiffness



Example / Abutment Nonlinearities (1 of 7)

- Use Seat Abutment Detail Given with Practice Problem No. 1
- Leave Columns at 3 ft Diameter
- Assign $A = 0.40g$ (In Order to Be Well into Nonlinear Range)
- Assume Backwall Breaks Away Around Perimeter of Box Girder
- Recall $K_{bent} = 3639 \frac{\text{kip}}{\text{ft}}$, $\Delta_{gap} = 6 \text{ in.}$, $S = 1.2$, and $W = 4842 \text{ kip}$



Example / Abutment Nonlinearities (2 of 7)

- Longitudinal Stiffness of Abutment (Caltrans)

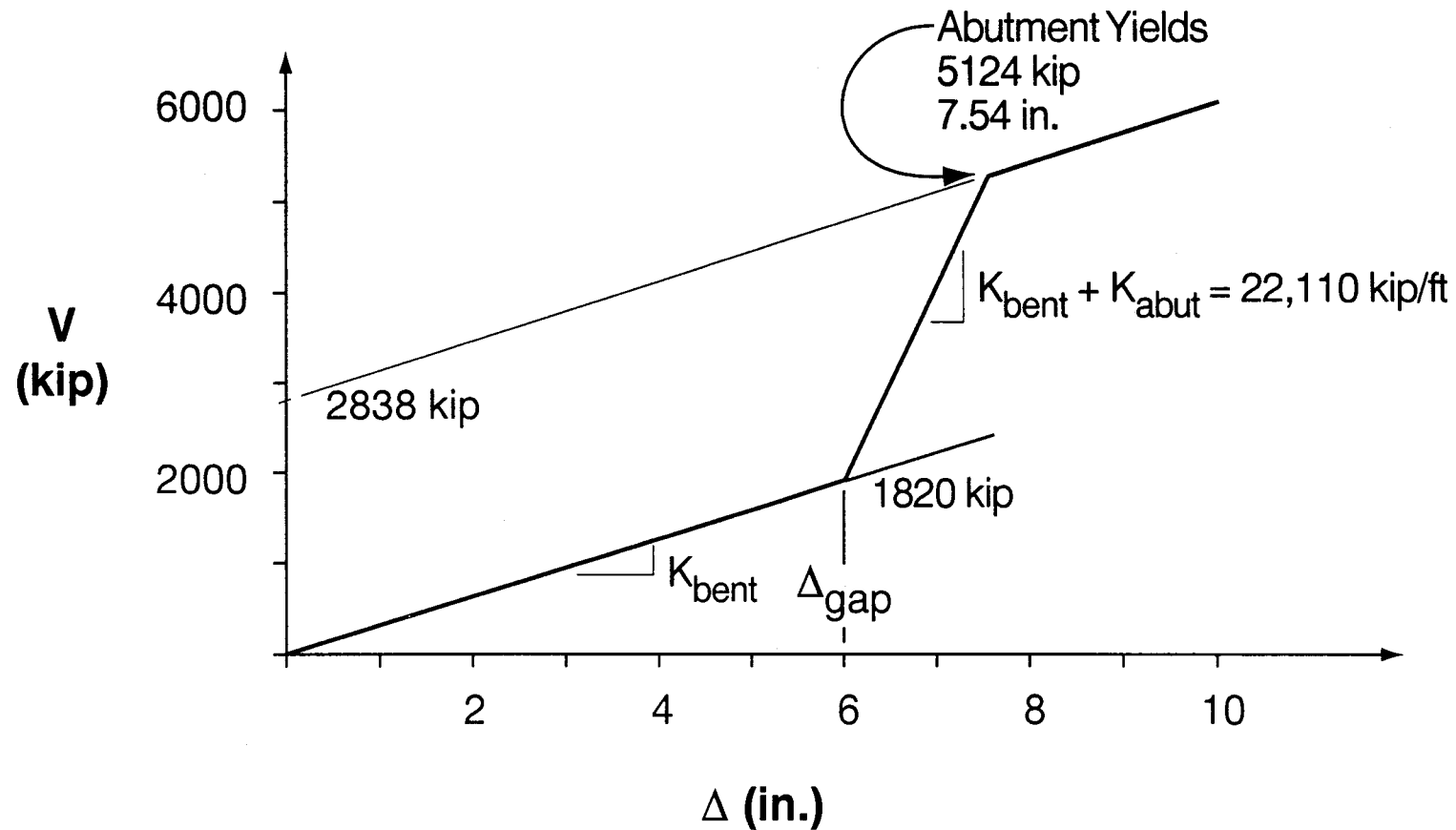
$$K_{\text{abut}} = 40 (65) \frac{5.67}{8} (12) = 22,110 \text{ kip/ft}$$

- Abutment Backfill Capacity (Caltrans)

$$P_{\text{max}} = 7.7(65)5.67 = 2838 \text{ kip}$$

- Construct V vs. Δ Curve for Structure (Longitudinal)

Example / Abutment Nonlinearities (3 of 7)



Example / Abutment Nonlinearities (4 of 7)

- Check Δ with Only Bent

$$K = 3639 \text{ kip/ft} \longrightarrow T = 2\pi \sqrt{\frac{4842}{32.2(3639)}} = 1.28 \text{ sec}$$

$$C_s = \frac{1.2 (0.4) 1.2}{1.28^{2/3}} = 0.49 < 1.00 \longrightarrow V = 0.49(4842) = 2373 \text{ kip}$$

$$\Delta = \frac{2373}{3639} (12) = 7.8 \text{ in.} > 6 \text{ in.} \quad \therefore \text{Into Nonlinear Range}$$

- Iterative Approach — Guess K, Determine V and Δ , Revise
- Direct Approach — Plot Spectral V vs. Δ

Example / Abutment Nonlinearities (5 of 7)

Direct Spectral Approach

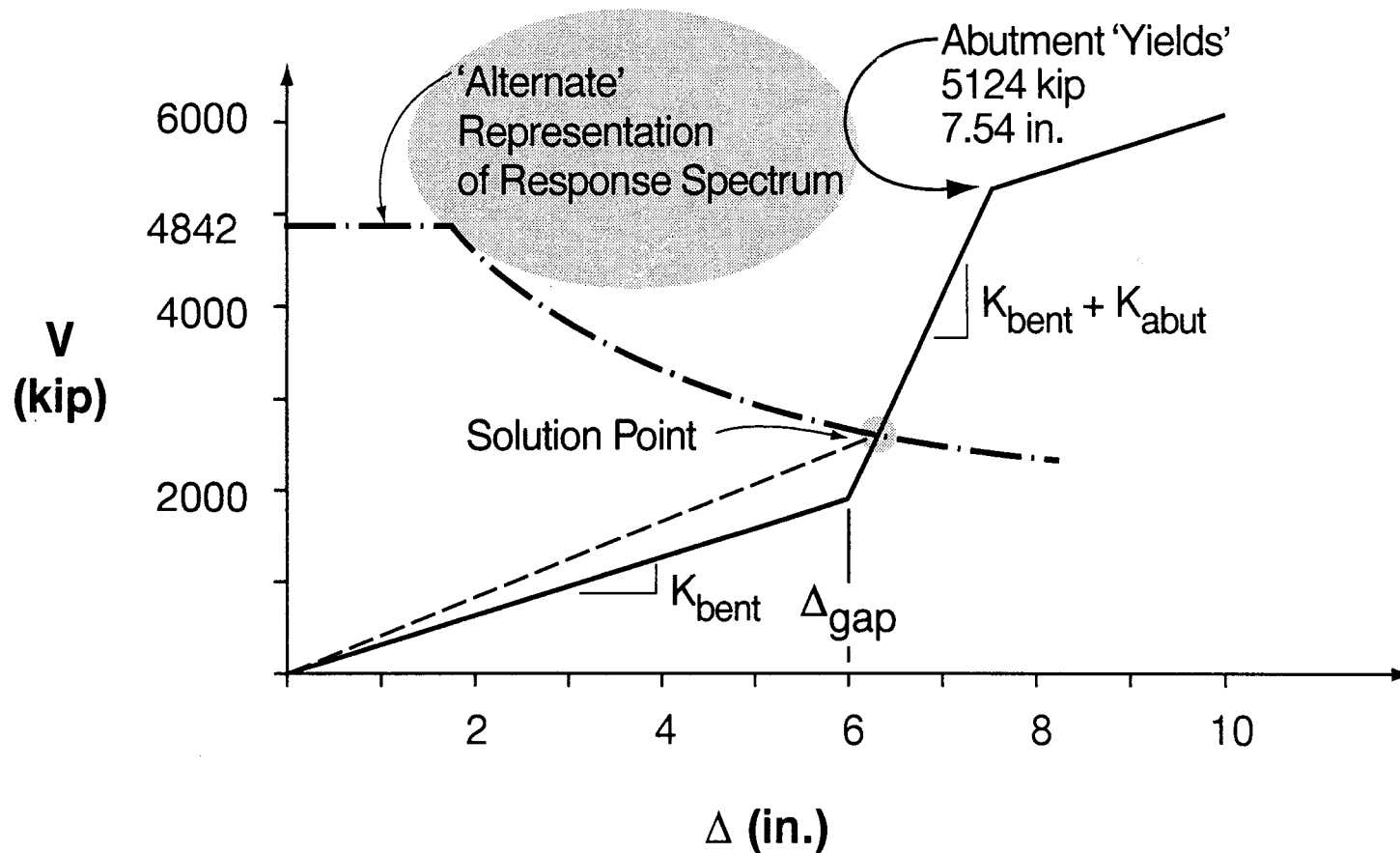
- $V = f(C_s) \quad C_s = f(T) \quad T = f(W/K) \quad K = f(V/\Delta) \quad \therefore \mathbf{V = f(\Delta)}$
- For a SDOF System with Full Mass Participation ($V = C_s W$)

$$V = \frac{(1.2AS)^{3/2} W g^{1/2}}{2\pi} \frac{1}{\Delta^{1/2}} \leq 2.5 AW$$

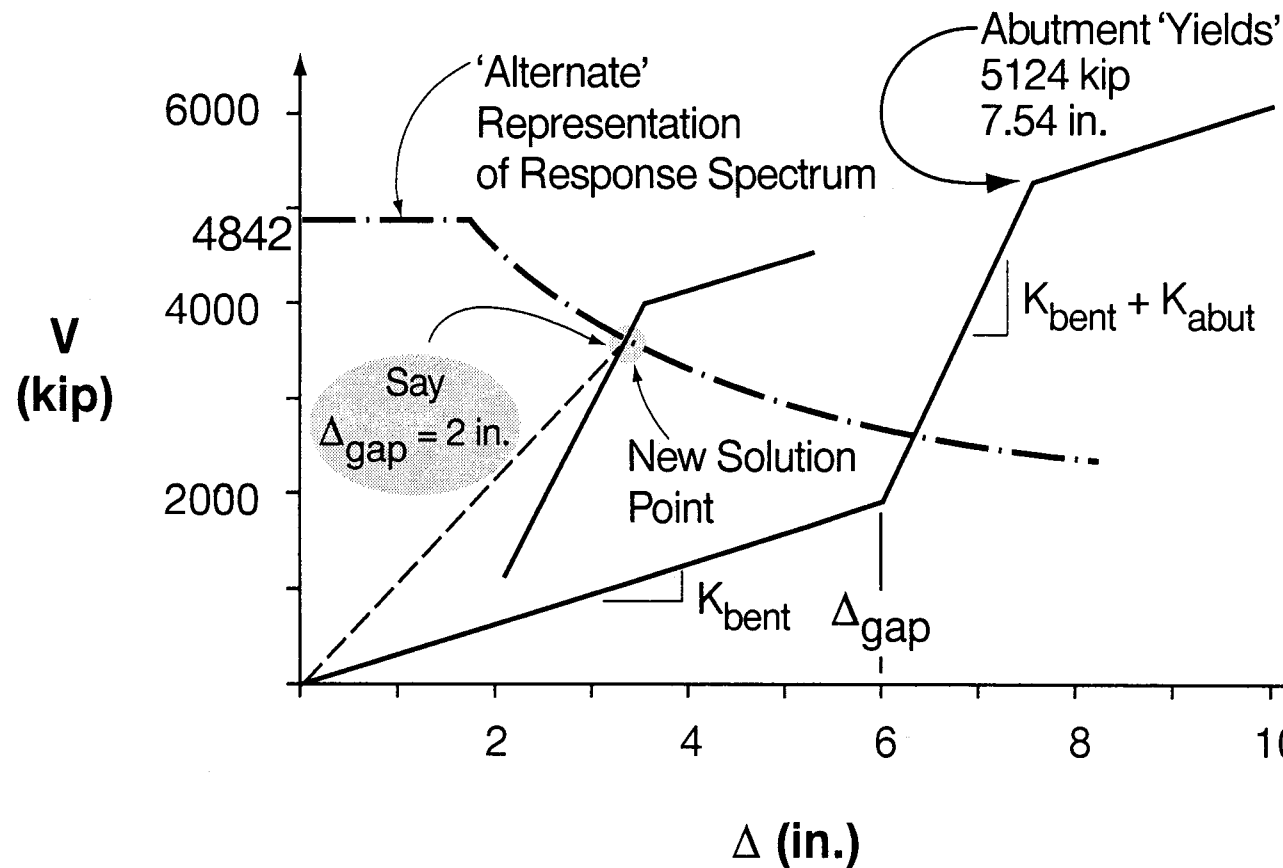
- For This Example

$$V = 1912 \frac{1}{\Delta^{1/2}} \leq 4842 \text{ kip } (\Delta \text{ in ft})$$

Example / Abutment Nonlinearities (6 of 7)



Example / Abutment Nonlinearities (7 of 7)



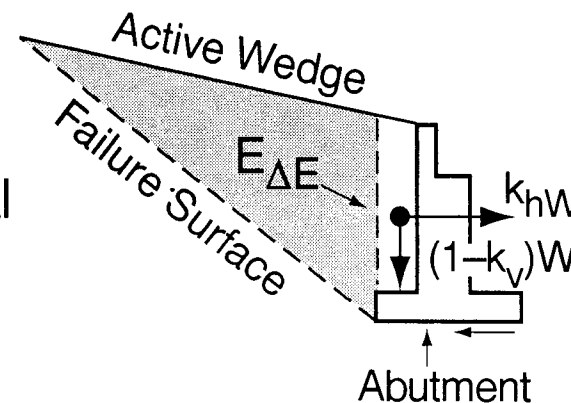
Session 2

Abutments

- Conceptual Behavior
- Modeling Soil Flexibility
- Nonlinear Effects
- **Mononobe-Okabe Analysis**
- Design Issues, Force Transfer, and Fuse Elements

Pseudostatic Approach / Yielding Abutments

- Applies to Seat-Type (Freestanding) Abutments that Are Not Restrained by Superstructure
- Cohesionless Backfill with Friction Angle ϕ
- Unsaturated / No Liquefaction
- Coulomb Sliding Wedge + Vertical and Horizontal Inertia Effects



Calculation of Active Seismic Loading on Wall

$$E_{AE} = \frac{1}{2} \gamma H^2 (1 - k_v) K_{AE}$$

- Inertial Effect Increases Forces

γ = Soil Unit Weight

H = Wall Height

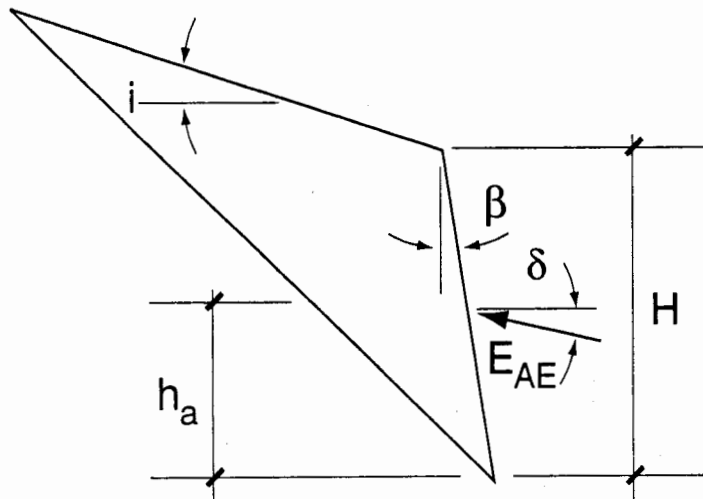
k_v = Vertical Acceleration Coefficient

k_h = Horizontal Acceleration Coefficient

Typically $\left. \begin{array}{l} k_v = 0 \\ k_h = 0.5A \end{array} \right\} \begin{array}{l} \text{Division I-A} \\ 6.4.3(A) \text{ and } 7.4.3(A) \end{array}$

Active Seismic Loading (continued)

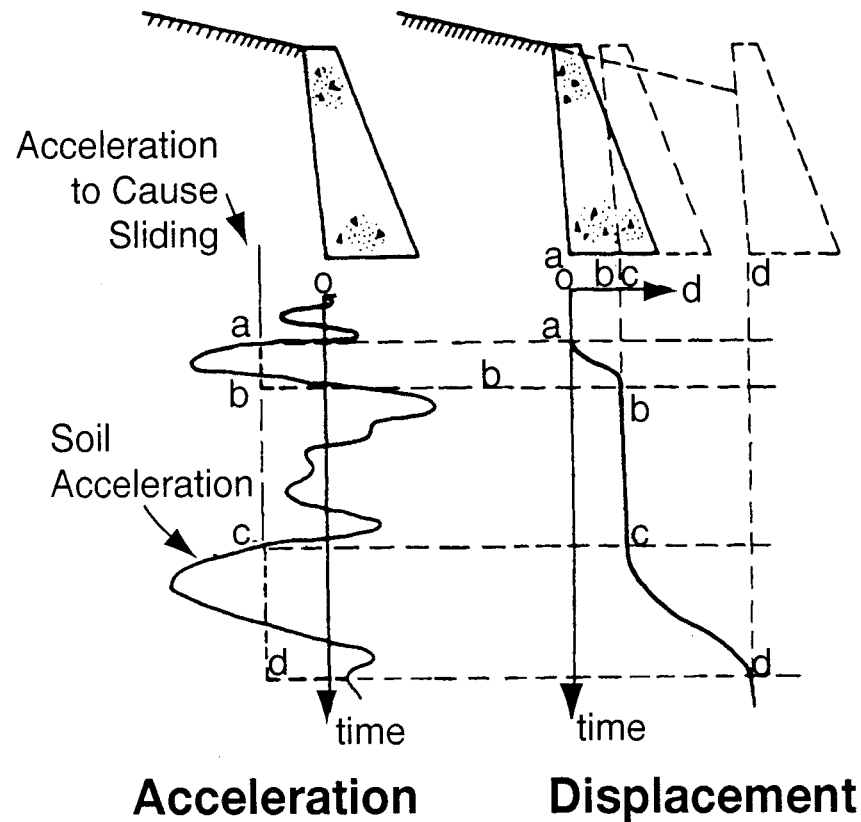
$$K_{AE} = \frac{\cos^2(\phi - \theta - \beta)}{\cos\theta \cos^2\beta \cos(\delta + \theta + \beta) \left[1 + \sqrt{\frac{\sin(\theta + \delta) \sin(\phi - \theta - i)}{\cos(\delta + \beta + \theta) \cos(i - \beta)}} \right]^2}$$



$$\theta = \tan^{-1} \left(\frac{k_h}{1 - k_v} \right)$$

$$\delta = \frac{\phi}{2} \text{ (Typical Approximation)}$$

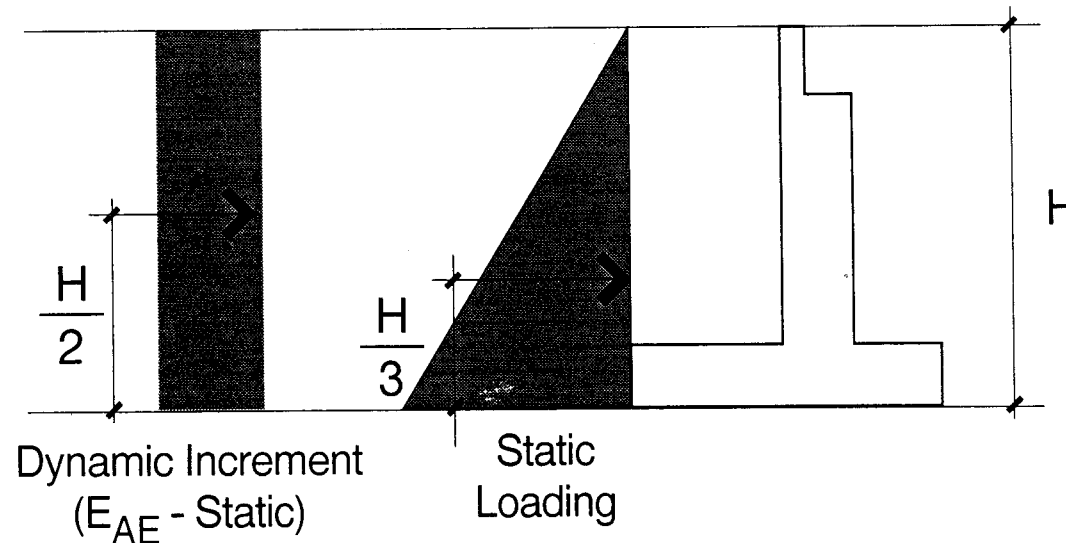
Allowing Some Wall Movement



- By Allowing Some Movement,
 $k_h = 0.5 A$ (Instead of A)
- Expect Displacements to $10 \cdot A$ (in.)
- Also Basis of 7.7 ksf vs. 5.0 ksf Used by Caltrans

Distributing the Force

- M-O Expression Includes the Static Active Load
- Obtain Static Force by Using k_h (or θ) = 0



Other Conditions

- Abutments Restrained by Soil Anchors or Battered Piles,
Use $k_h = 1.5A$
- Abutments Moving into Soil, — Could Use
M-O Passive, But No Experimental Verification

Using the Concepts

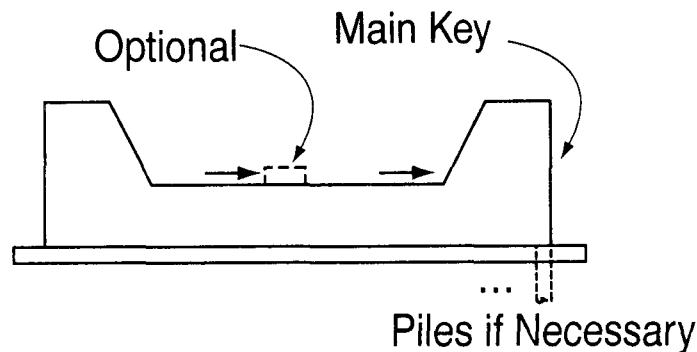
Abutment Type / Condition	Method	...	Product
• Seat / Gap Open	M-O Active	...	Loading
• Seat / Gap Closed	Caltrans	...	Stiffness / Capacity
	or		
	FHWA	...	Stiffness
• Integral	Caltrans	...	Stiffness / Capacity
	or		
	FHWA	...	Stiffness

Session 2

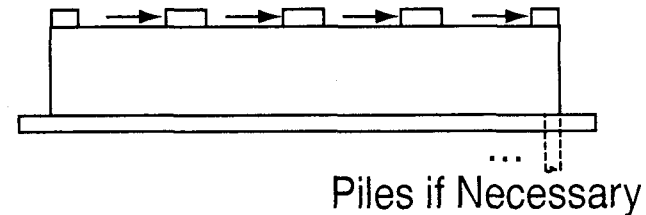
Abutments

- Conceptual Behavior
- Modeling Soil Flexibility
- Nonlinear Effects
- Mononobe-Okabe Analysis
- **Design Issues, Force Transfer, and Fuse Elements**

Transverse Loading of Abutments / Shear Keys



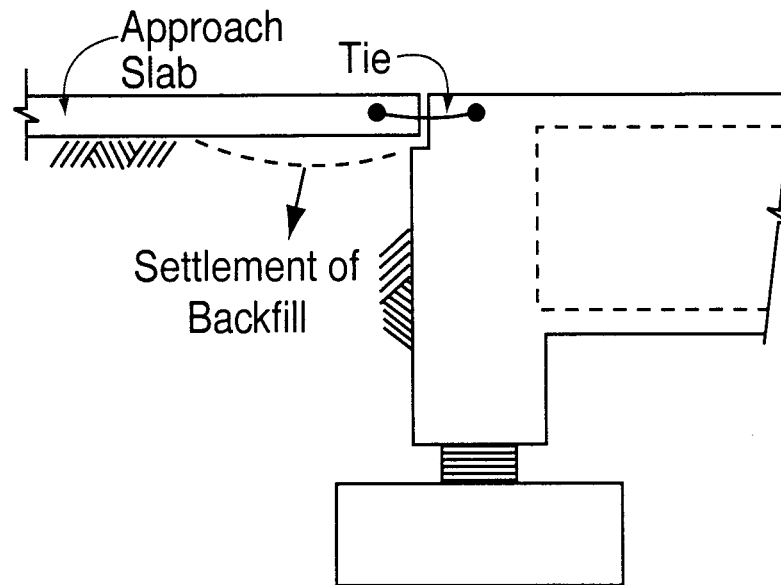
**Box Girder
Arrangement**



**Precast or Steel
Girder Arrangement**

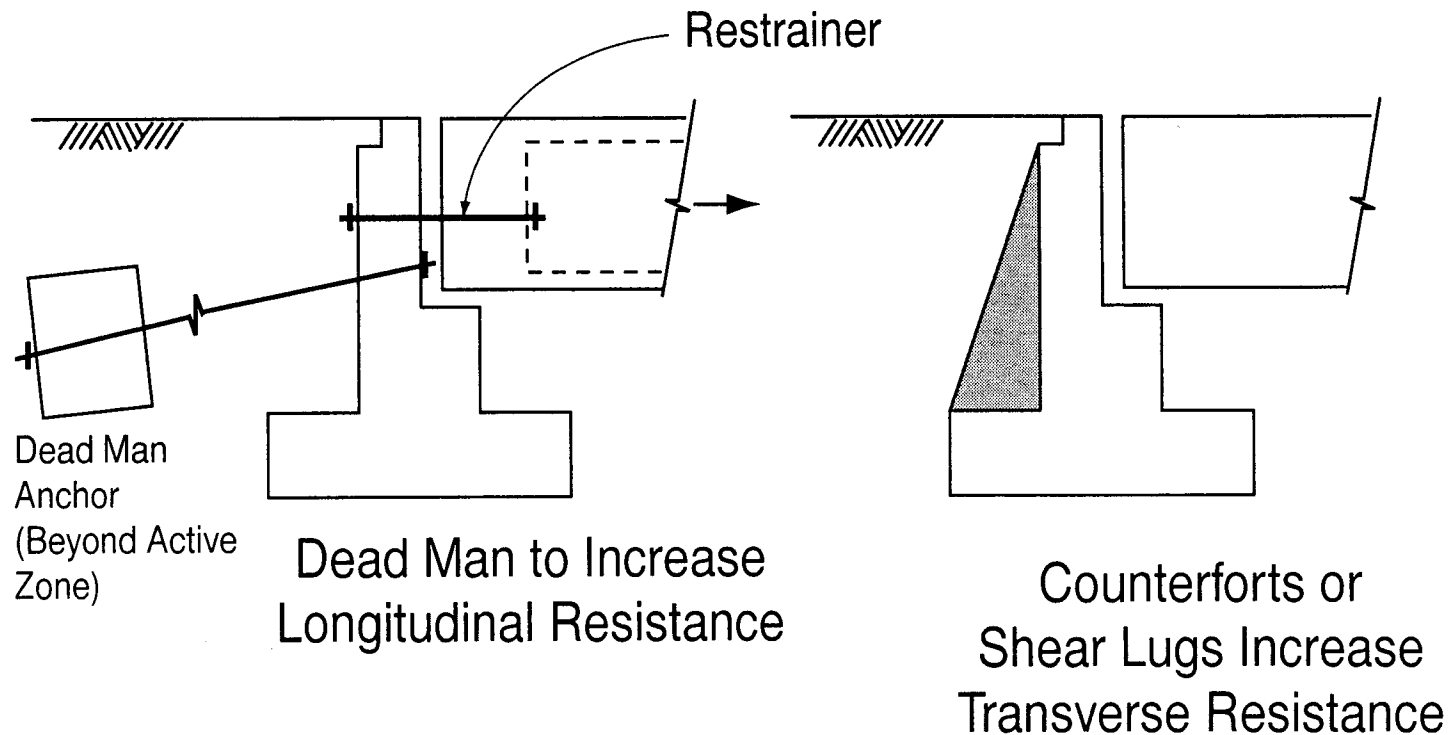
- Interior Keys for Box Girders Difficult to Inspect and Repair
- Multiple Keys May Not Load Evenly (Be Conservative / Ductile)
- Consider 'Fusing' Keys to Fail Before Damaging Piles

Approach Slabs



- If Settlement Occurs, Approach Slab Provides Access to Bridge (Required for SPC **D**, Emergency Response)
- Tie to Superstructure to Prevent Unseating

Enhancements for Force Transfer



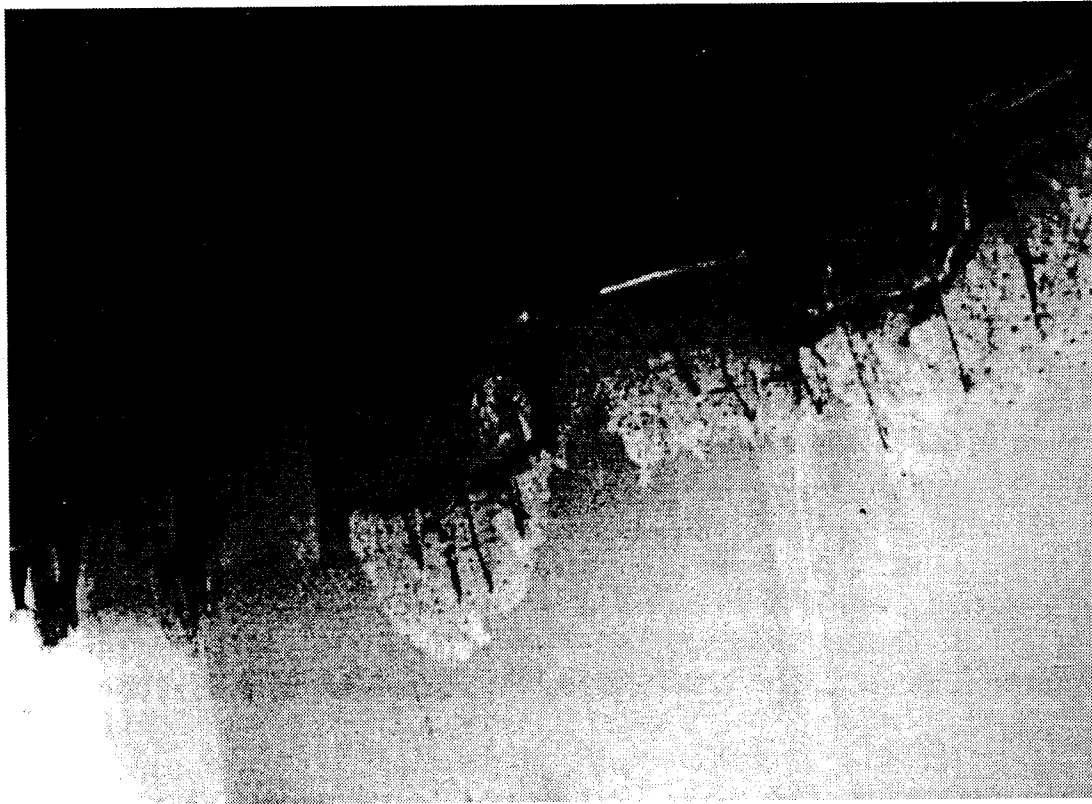
External Shear Key Damage



Northridge,
1994

EERI (1995)

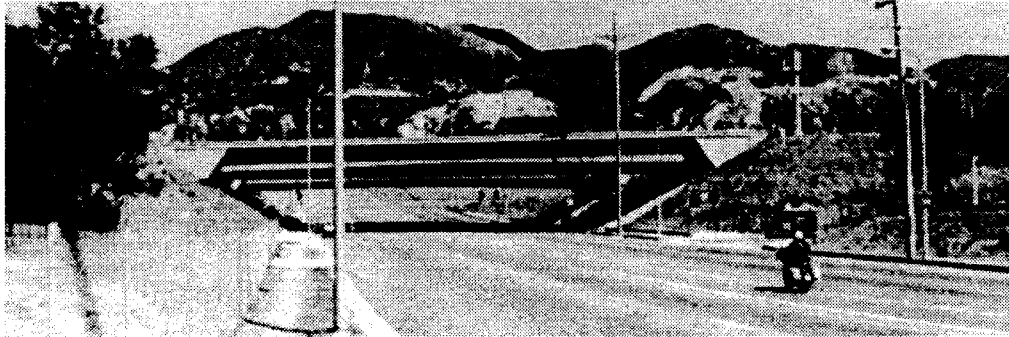
Internal Shear Key Damage



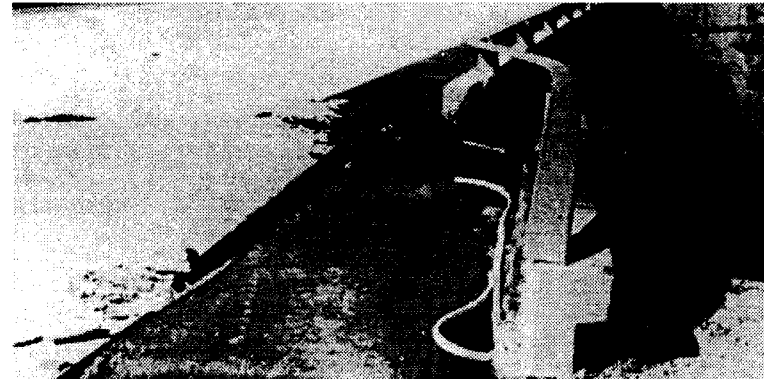
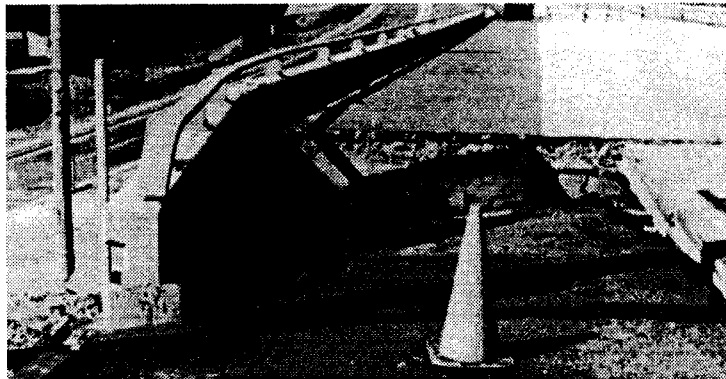
Northridge,
1994

EERI (1995)

Transverse Response and Backfill Settlement Issues

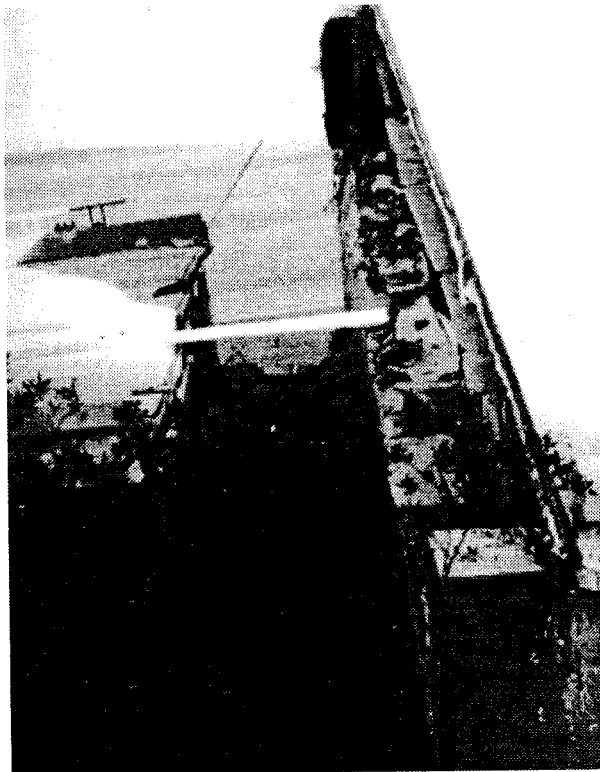


San Fernando,
1971



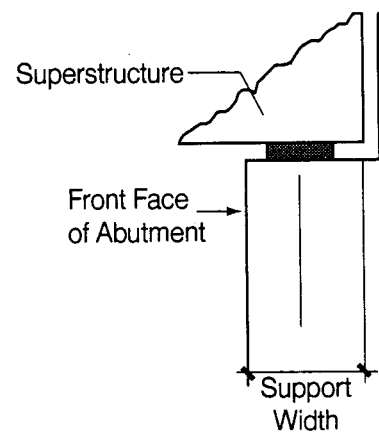
Caltech (1971)

Most Important of All – Seat Width

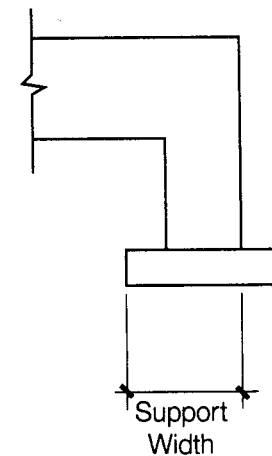


EERI (1995)

Northridge, 1994



Seat Abutment



Integral Abutment

Session 3

Steel Plate Girder Bridge Examples

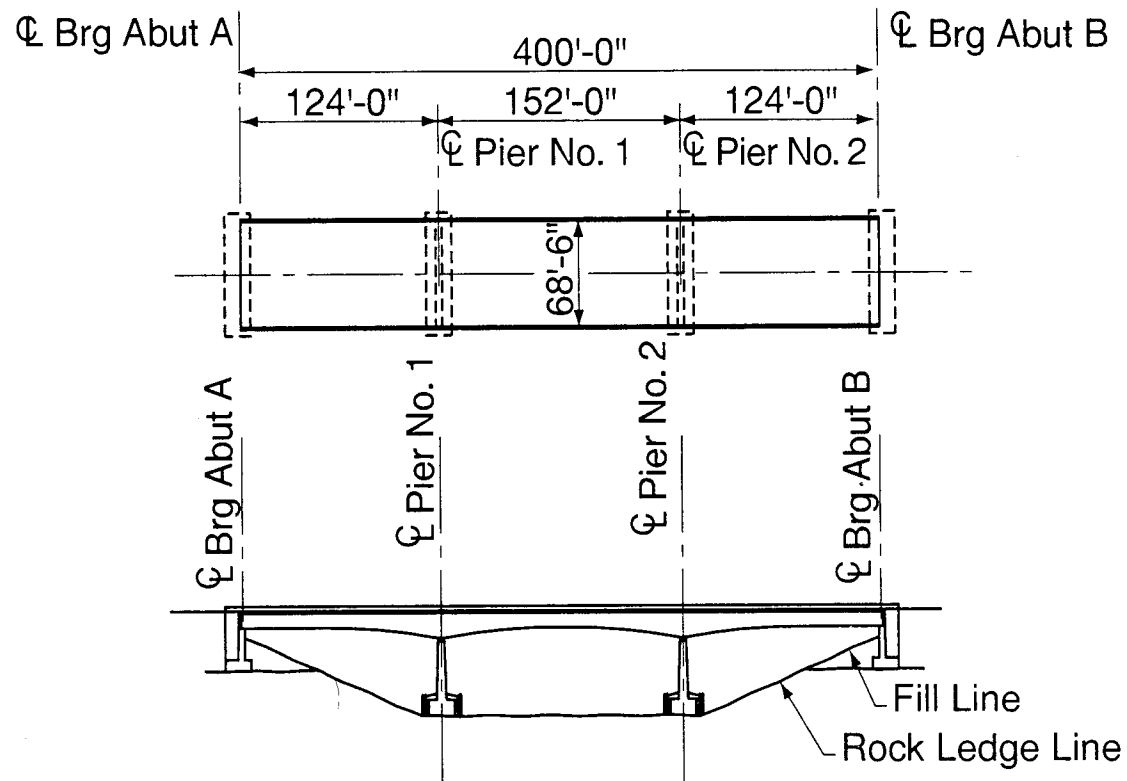
Session 3

- **Practice Problem No. 2**
- **Conceptual Design Considerations**
- **Steel Superstructure Issues**

Session 4

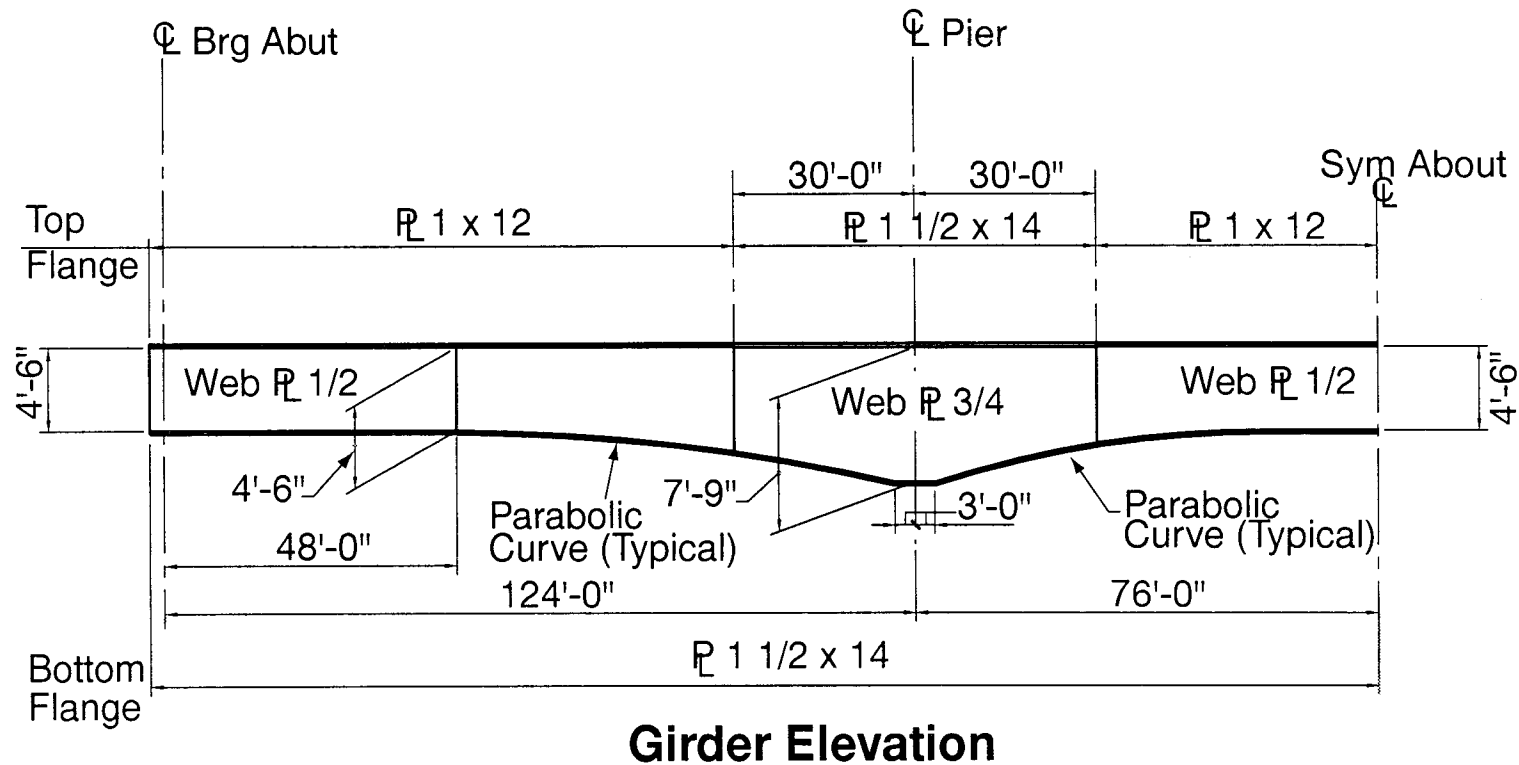
- **Skew Structure Issues**
- **Elastomeric Bearing Modeling**

Steel Plate Girder Bridge / Layout

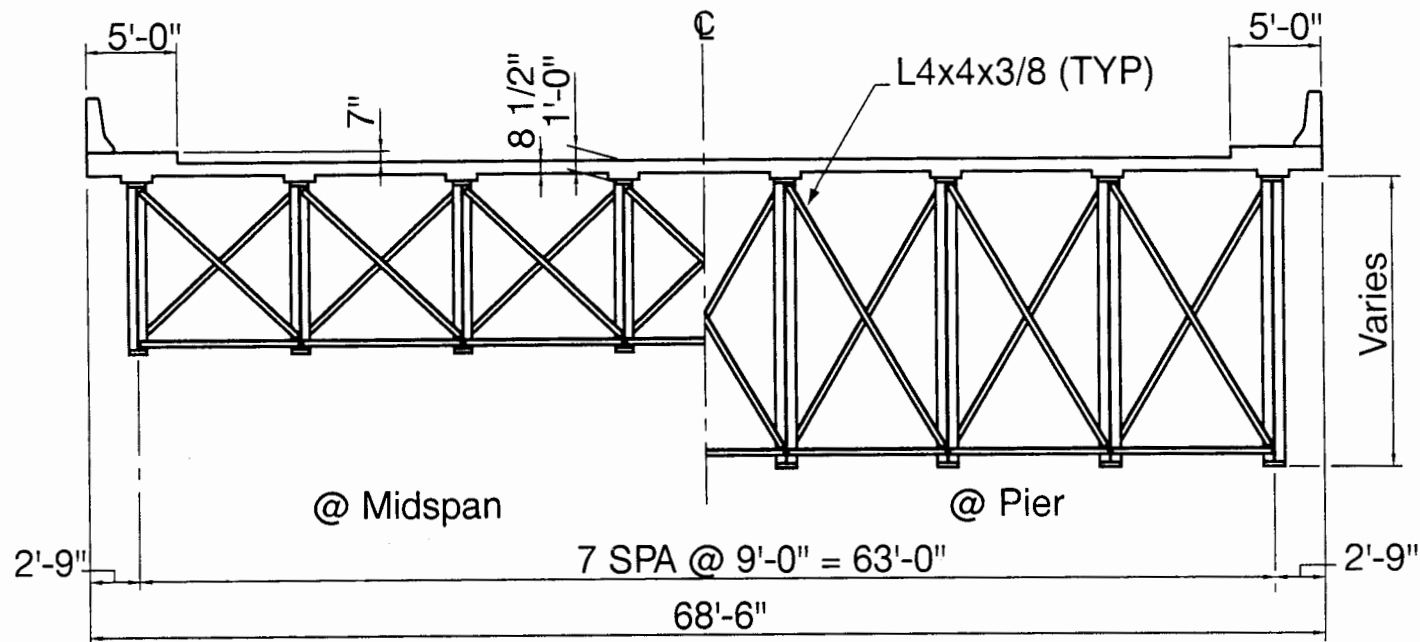


End Elevation

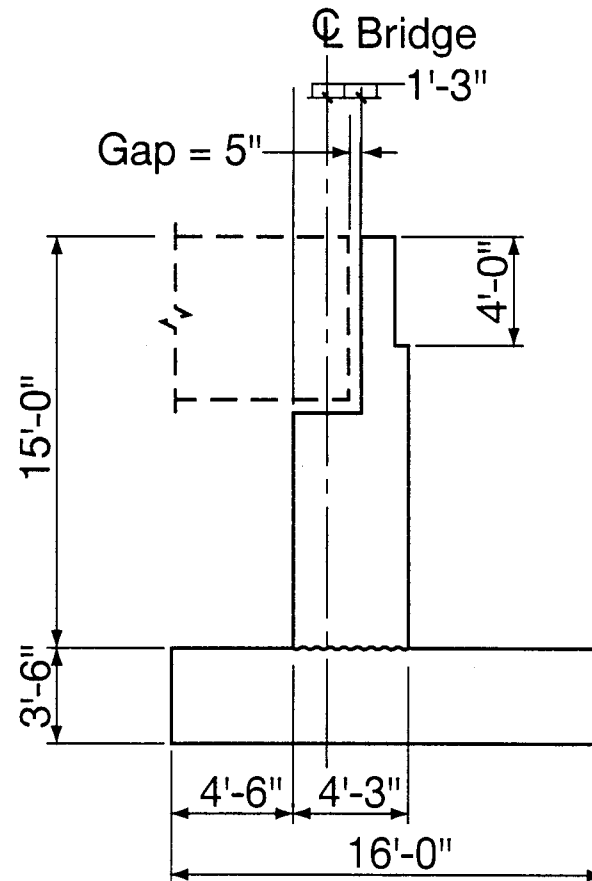
Steel Plate Girder Bridge / Girder Elevation



Steel Plate Girder Bridge / Superstructure Section



Steel Plate Girder Bridge / Abutment Section



Session 3

Required / Practice Problem No. 2

- **Calculate Longitudinal Period**
- **Calculate Elastic Longitudinal Shear, Moment, and Displacement of Pier No. 1**
- **Design Pier No. 1 Reinforcement**
- **Size Footing**
- **Consider Alternatives**

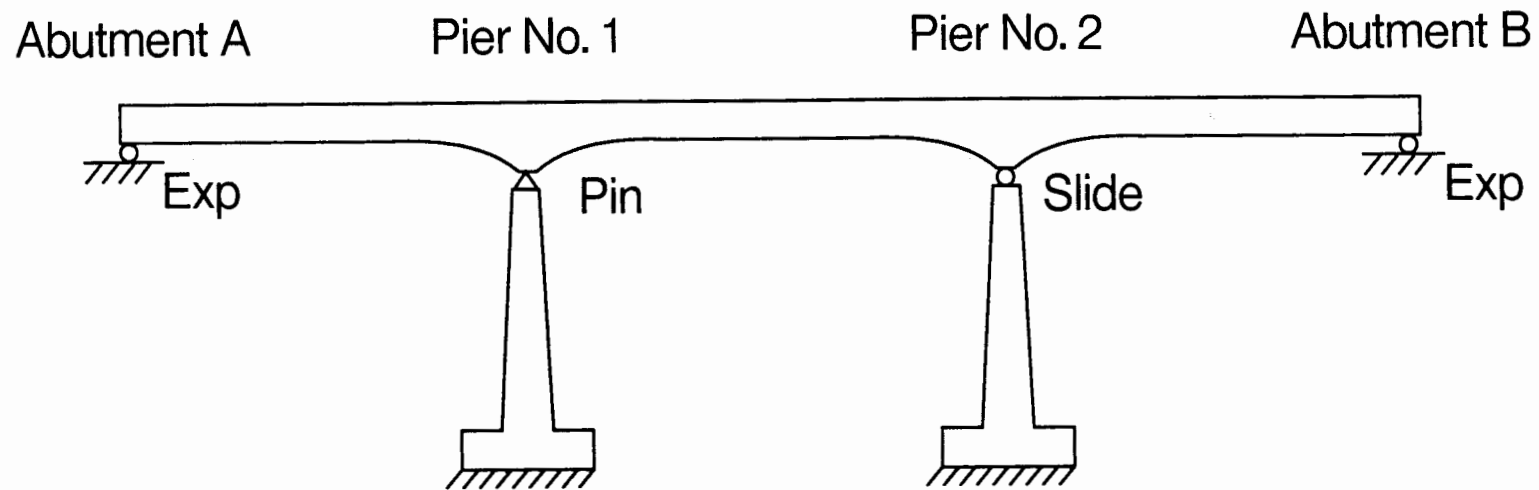
Basic Data for Bridge

- Acceleration Coefficient, $A = 0.15g$
- Seismic Performance Category, $SPC = B$
- Soil — Rock

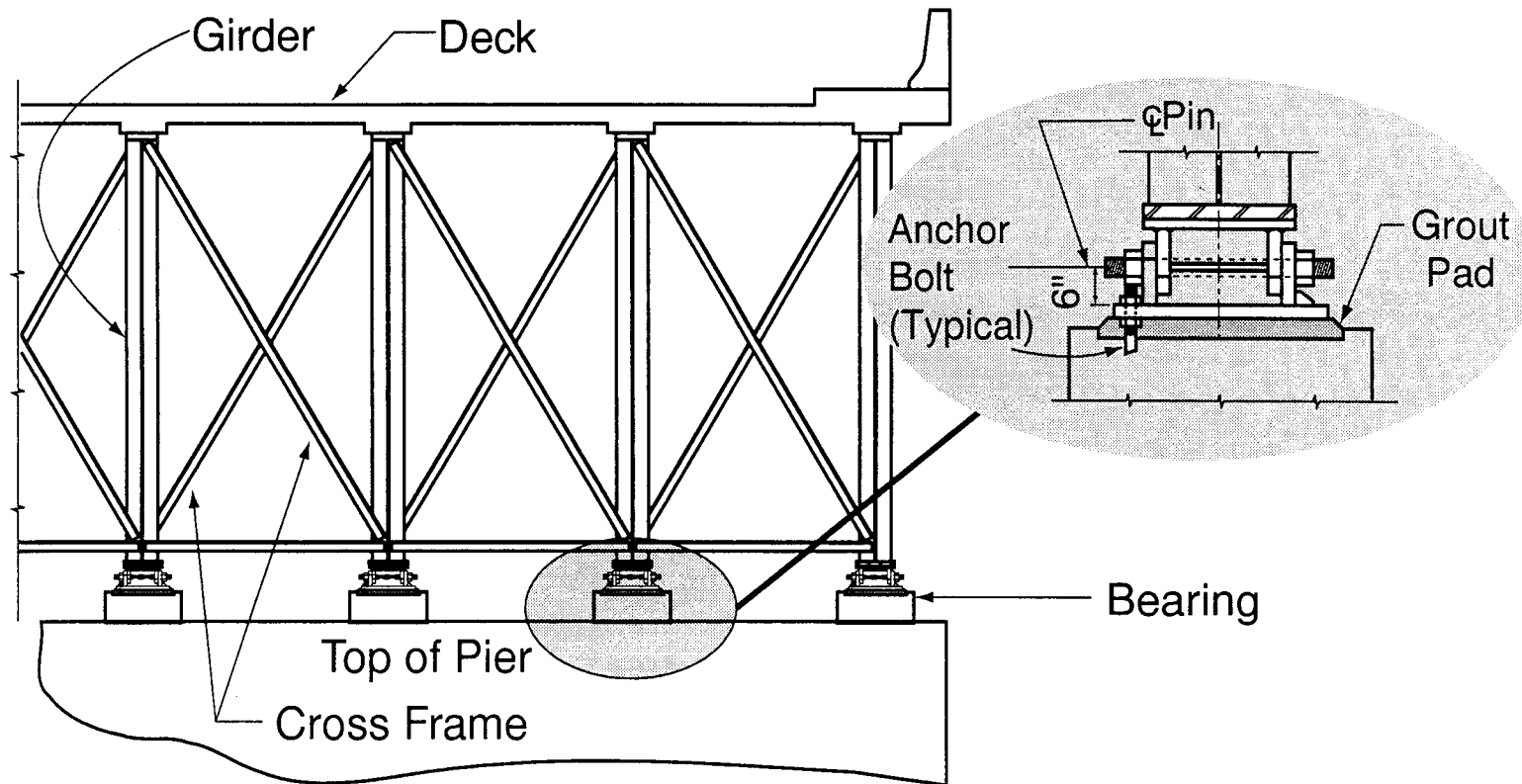
$$S = 1.0$$

$$f_{ult} = 50 \text{ ksf} \quad \text{Ultimate Bearing Capacity}$$

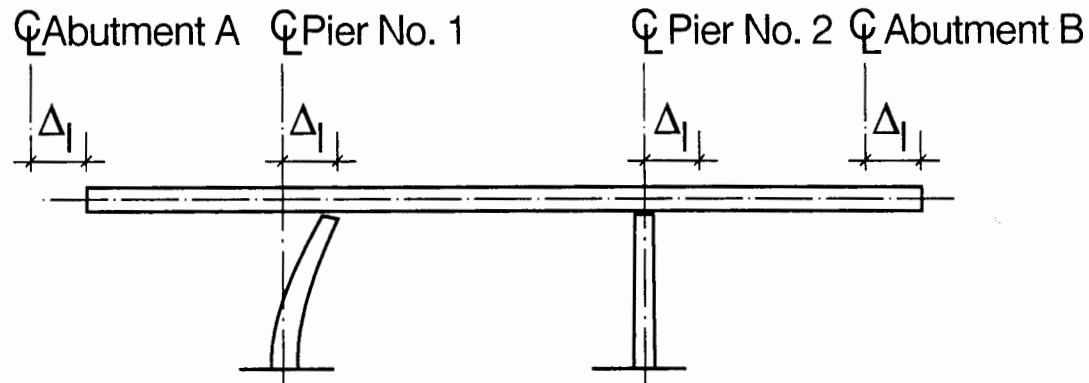
Bearing Conditions – Longitudinal



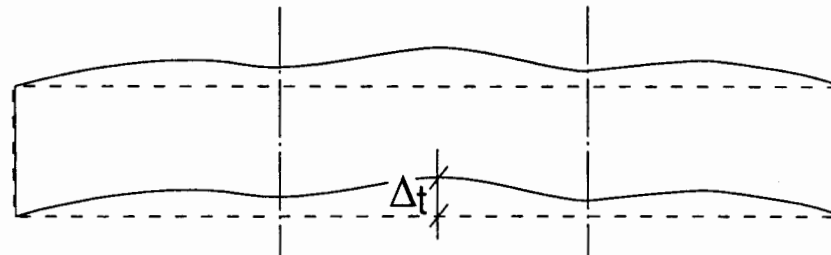
Bearing Conditions – Transverse



Expected Lateral Seismic Behavior

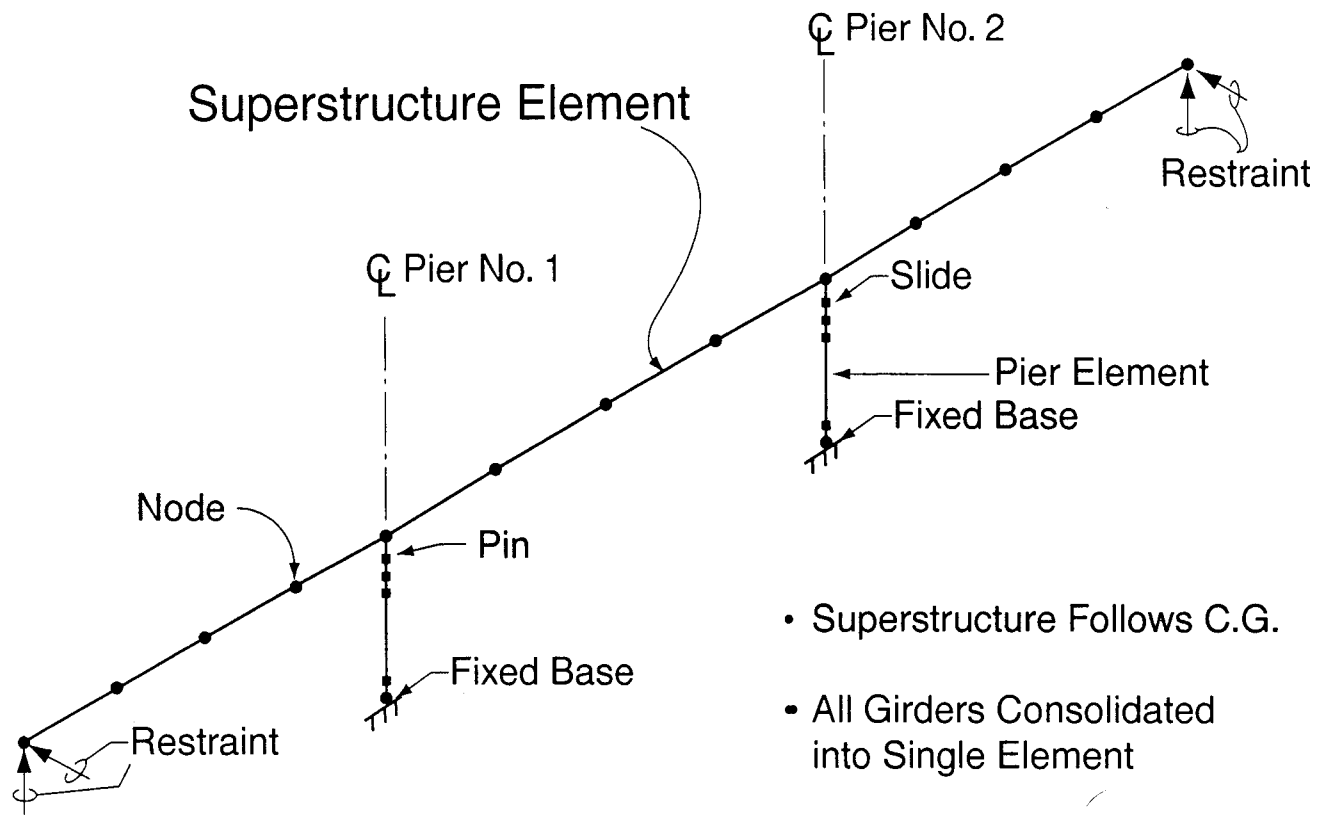


Longitudinal Behavior — One Column Resists Loads



Transverse Behavior — Piers and Abutments Resist Loads

Seismic Analysis Model



Superstructure Properties

Location	Area A (ft ²)	Effective Density γ^a (k/ft ³)	Moment of Inertia		
			Bending in Horiz. Plane	Bending in Vert. Plane	
			I horiz ^b (ft ⁴)	y bar ^c (ft)	I vert ^b (ft ⁴)
Abutment	81.0	0.166	36207	1.377	296
End Span 1/4 Pt	81.0	0.166	36207	1.377	296
1/2 Pt	81.0	0.166	36353	1.407	311
3/4 Pt	84.3	0.162	36607	1.698	473
Pier	104.0	0.143	45988	2.477	996
Center Span 1/4 Pt	83.4	0.163	37206	1.603	417
1/2 Pt	81.0	0.166	36207	1.377	296

- a. Includes Weight of Barriers, Overlay, Forms, Stiffeners, and Cross Frames
- b. I Based on Full Composite Action of Deck and Girders
- c. 'y bar' Is Measured from the Top of the 9 in. Deck

Superstructure Specifics

- Properties Based on Equivalent Concrete

- Weights Include

Concrete $w_C = 8.16 \text{ kip/ft}$

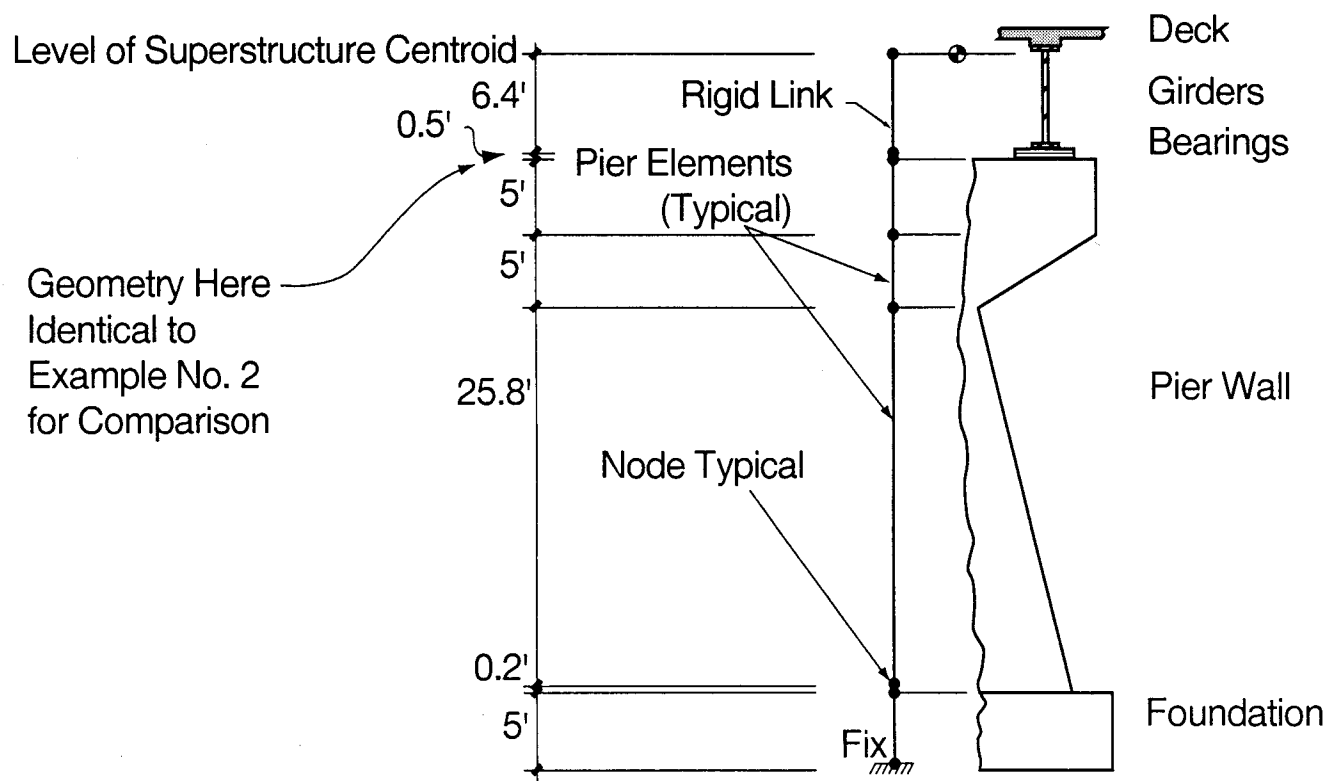
Girders $w_g = 3.04 \text{ kip/ft to } 1.63 \text{ kip/ft}$

Barrier Overlay, Stay-in-Place Forms, Allowance
for Cross Frames and Stiffeners

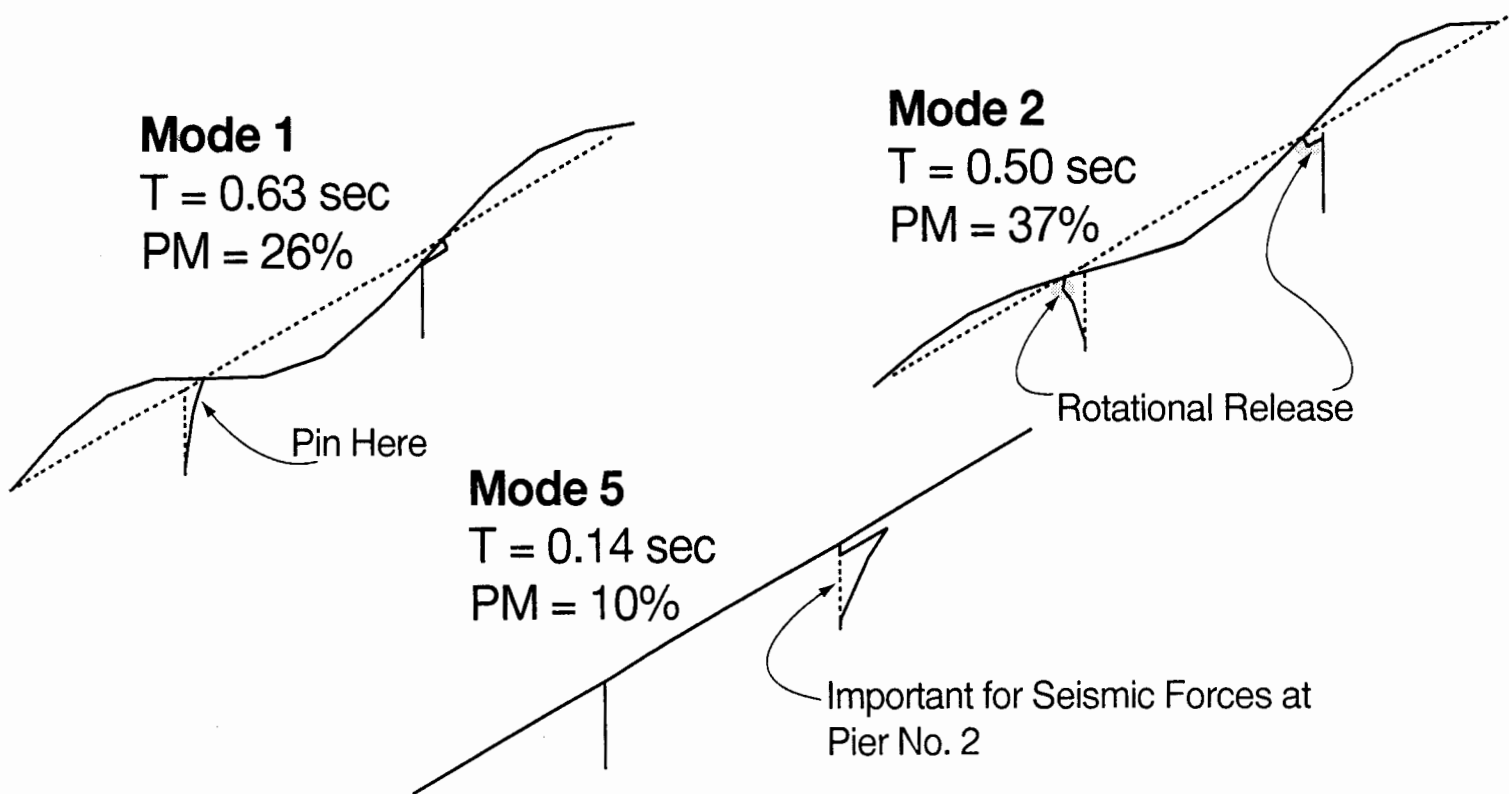
$w_m = 3.69 \text{ kip/ft}$

- Full Composite Action Assumed

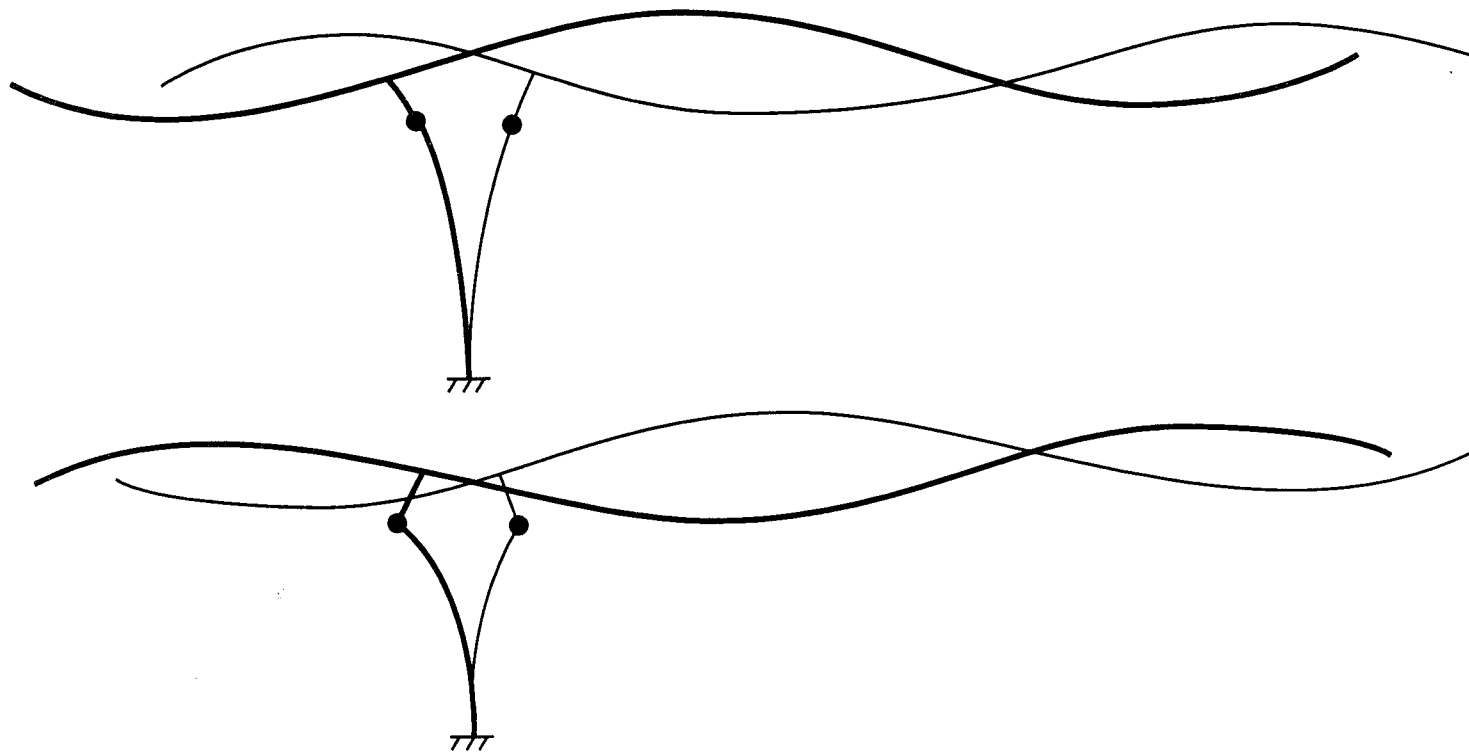
Pier Geometry



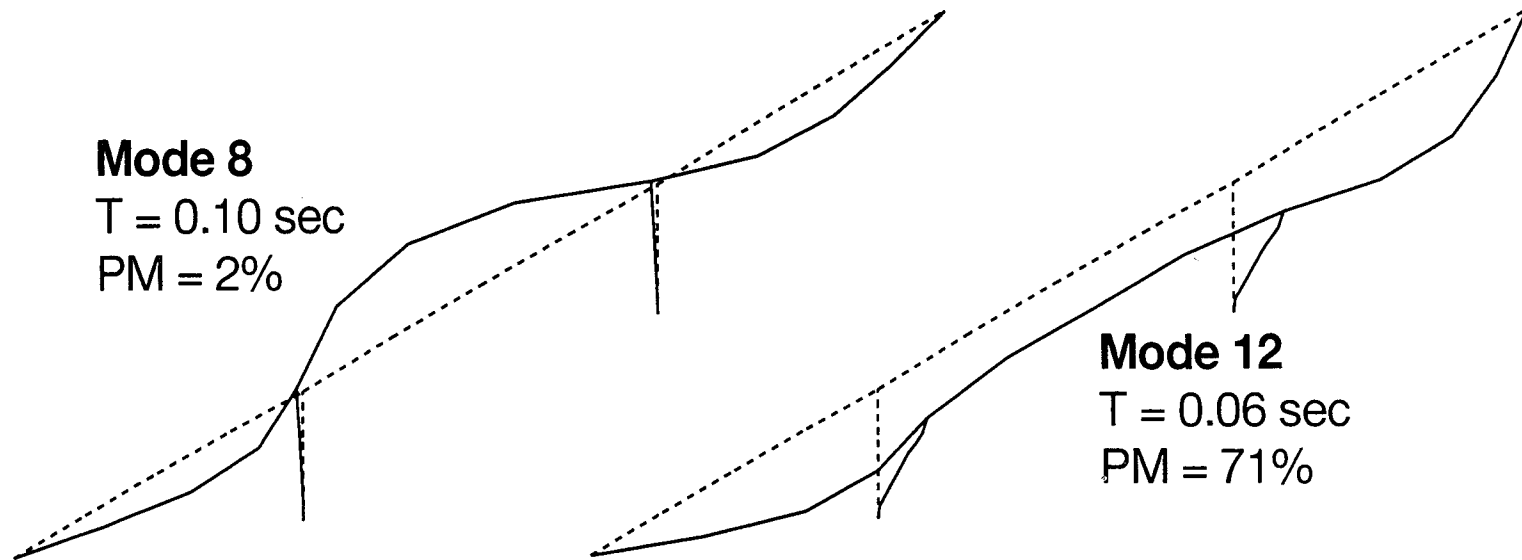
Longitudinal Mode Shapes



Reasons for Two Longitudinal Modes

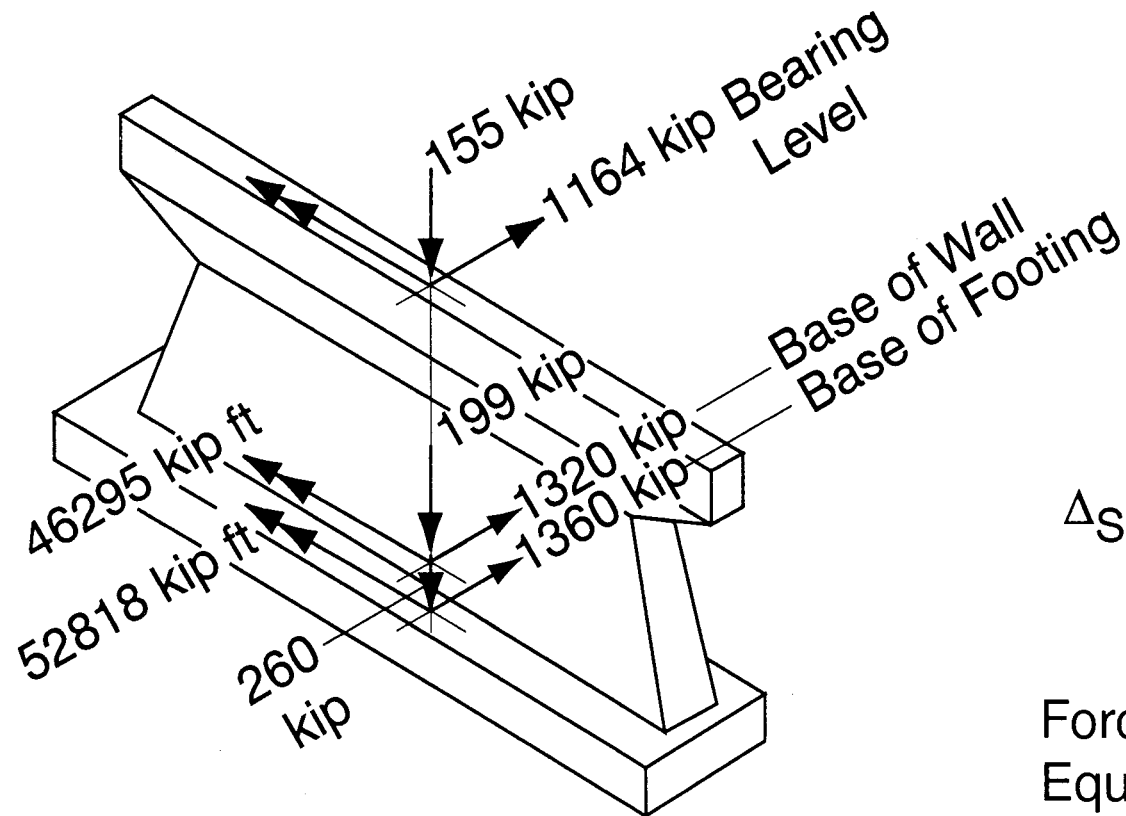


Transverse Mode Shapes



(Recall 3 • No. of Spans = 9)

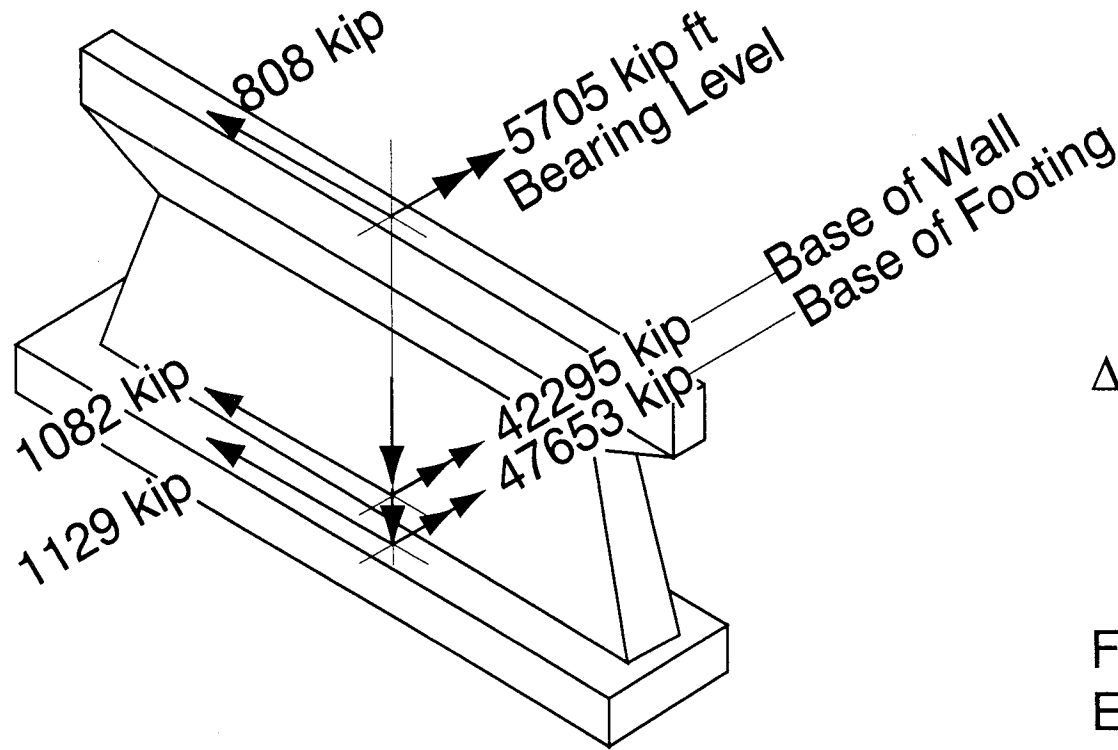
Longitudinal Modal Analysis Results



$$\Delta_{\text{Super}} = 0.61 \text{ in.}$$

Forces Not Shown
Equal Zero

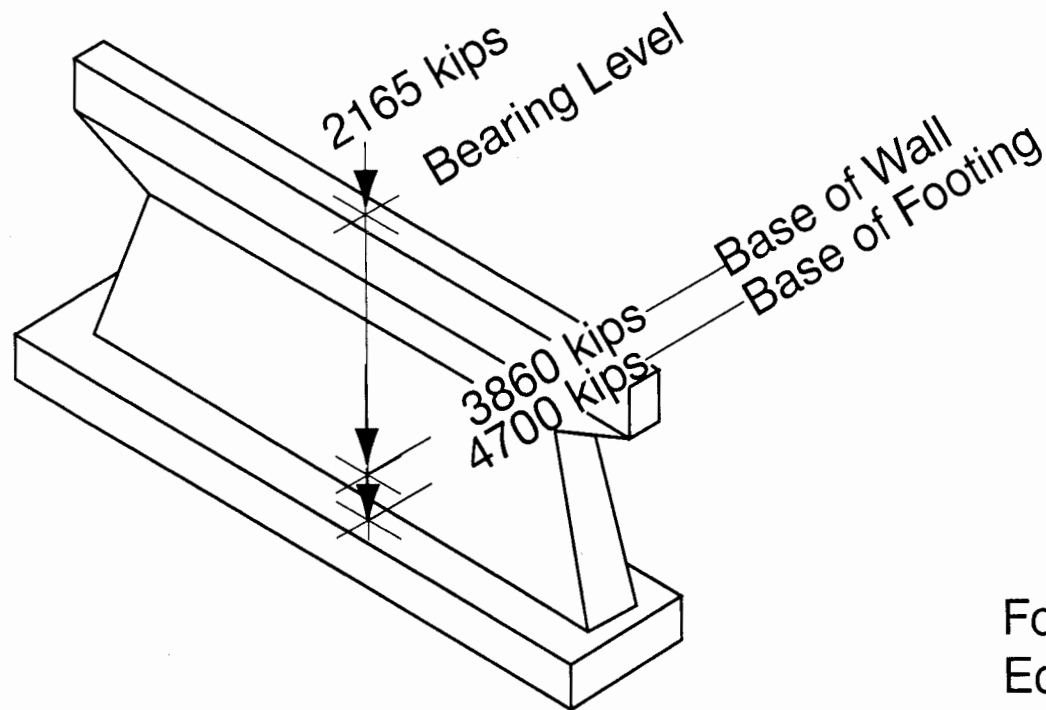
Transverse Modal Analysis Results



$$\Delta_{\text{Super}} = 0.014 \text{ in.}$$

Forces Not Shown
Equal Zero

Dead Load Analysis Results / Spine Model



Forces Not Shown
Equal Zero

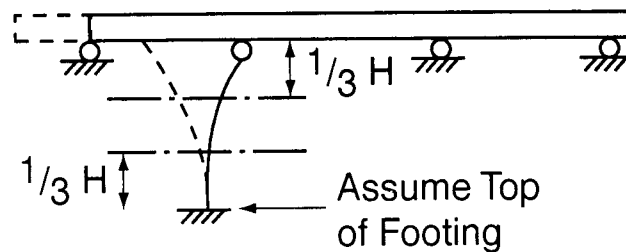
Check of Results / Hand and Computer

Strategy: • Compare Period and Base Shear

Use:

- Hand Model with Rigid Superstructure
- Computer Model with Rigid Superstructure
(Only Change from Previous Modal Analysis)

Hand Check



- Seismic Weight**

$$W_{\text{super}} = 5525 \text{ kip}$$

$$W_{1/3} = 517 \text{ kip}$$

$$W_{\text{total}} = 6041 \text{ kip}$$

- Stiffness**

Use Stiffness at $1/3$ of Height of Tapered Wall Above the Footing

$$K = \frac{3(519000)764}{(36)^3} = 25508 \text{ kip/ft}$$

$B = 60.46 \text{ ft} \quad T = 5.333 \text{ ft}$

Hand Check (continued)

- **Period**
$$T_{\text{Long}} = 2 \pi \sqrt{\frac{W}{g K}} = 2 \pi \sqrt{\frac{6041}{32.2 (25508)}}$$

$$T_{\text{Long}} = 0.54 \text{ sec} \quad \text{Bracketed by Mode 1 and 2 Periods}$$

- **Base Shear**
$$V_{\text{Long}} = C_s W = \frac{1.2(0.15)1.0}{(0.54)^{2/3}} (6041)$$

$$V_{\text{Long}} = (0.272)(6041) = 1642 \text{ kips}$$

Computer Model with 'Rigid' Superstructure

Let:

$$I_{\text{super}} \rightsquigarrow 10^7 \cdot I_{\text{super}} \rightsquigarrow T_{\text{long}} = 0.53 \text{ sec}$$

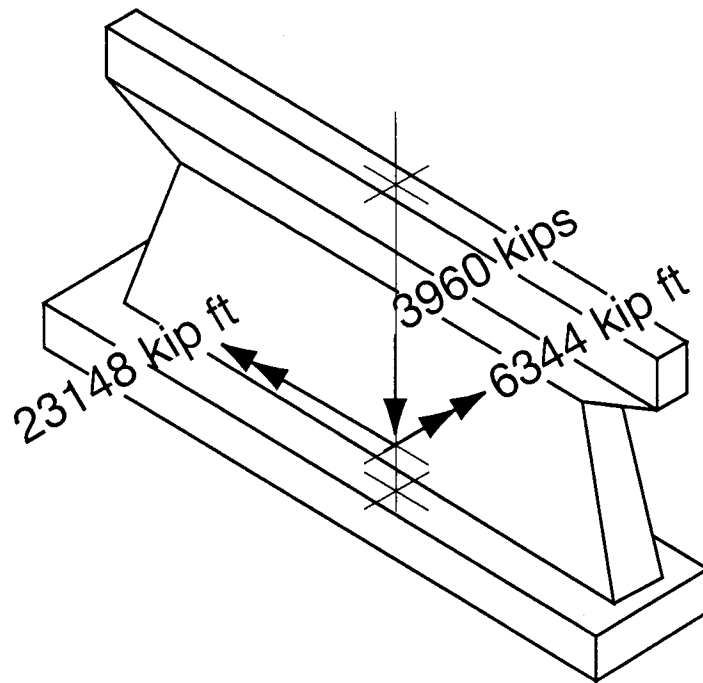
Then:

$$V_{\text{long}} = 1776 \text{ kip}$$

Comparison of Results and Checks

- **Basic Model** $V = 1320$ kip at Base of Wall
- **Hand Check** $V = 1642$ kip ... Higher Due to Single
Mode Contributing All
Response
- **Rigid Superstructure
Computer Model** $V = 1776$ kip ... Higher Than Hand Check
Due to Contribution of
Lower Part of Pier
(~ 90 kip)

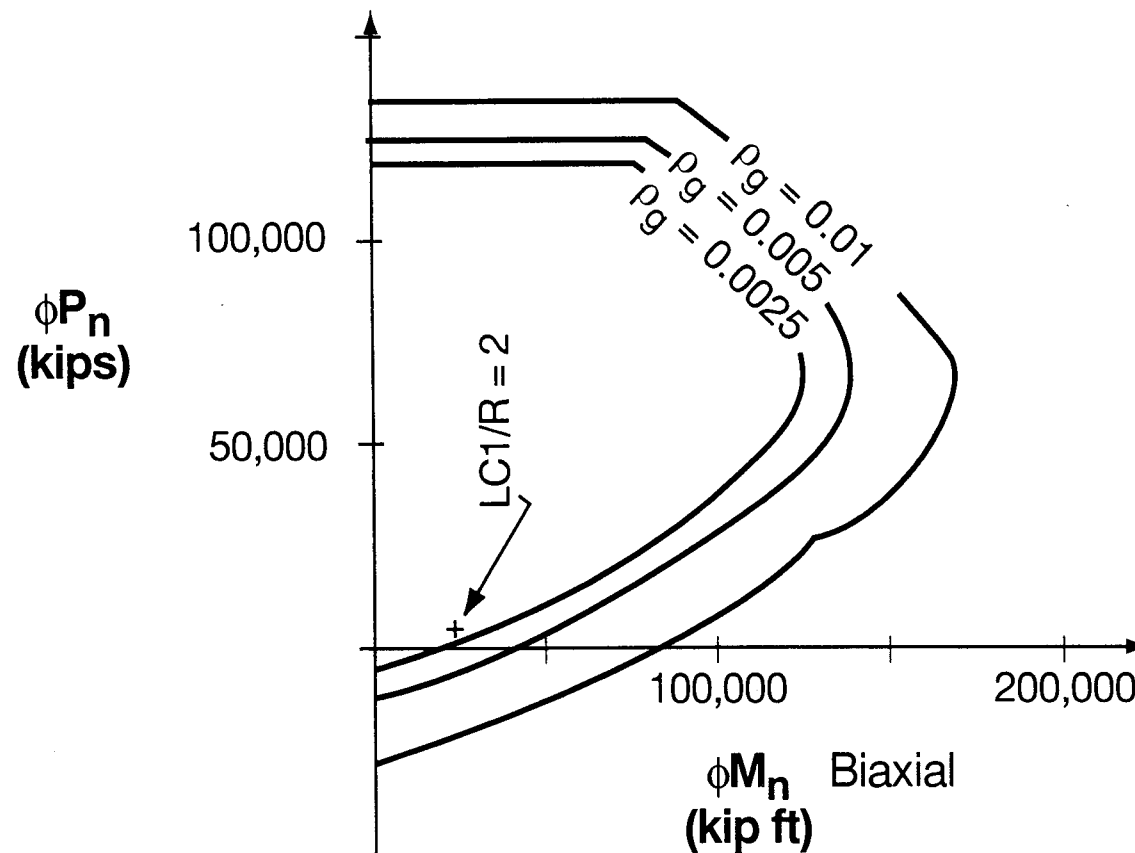
Design Forces at Base of Wall



R = 2 Weak

R = 2 Strong

Vertical Reinforcement Options



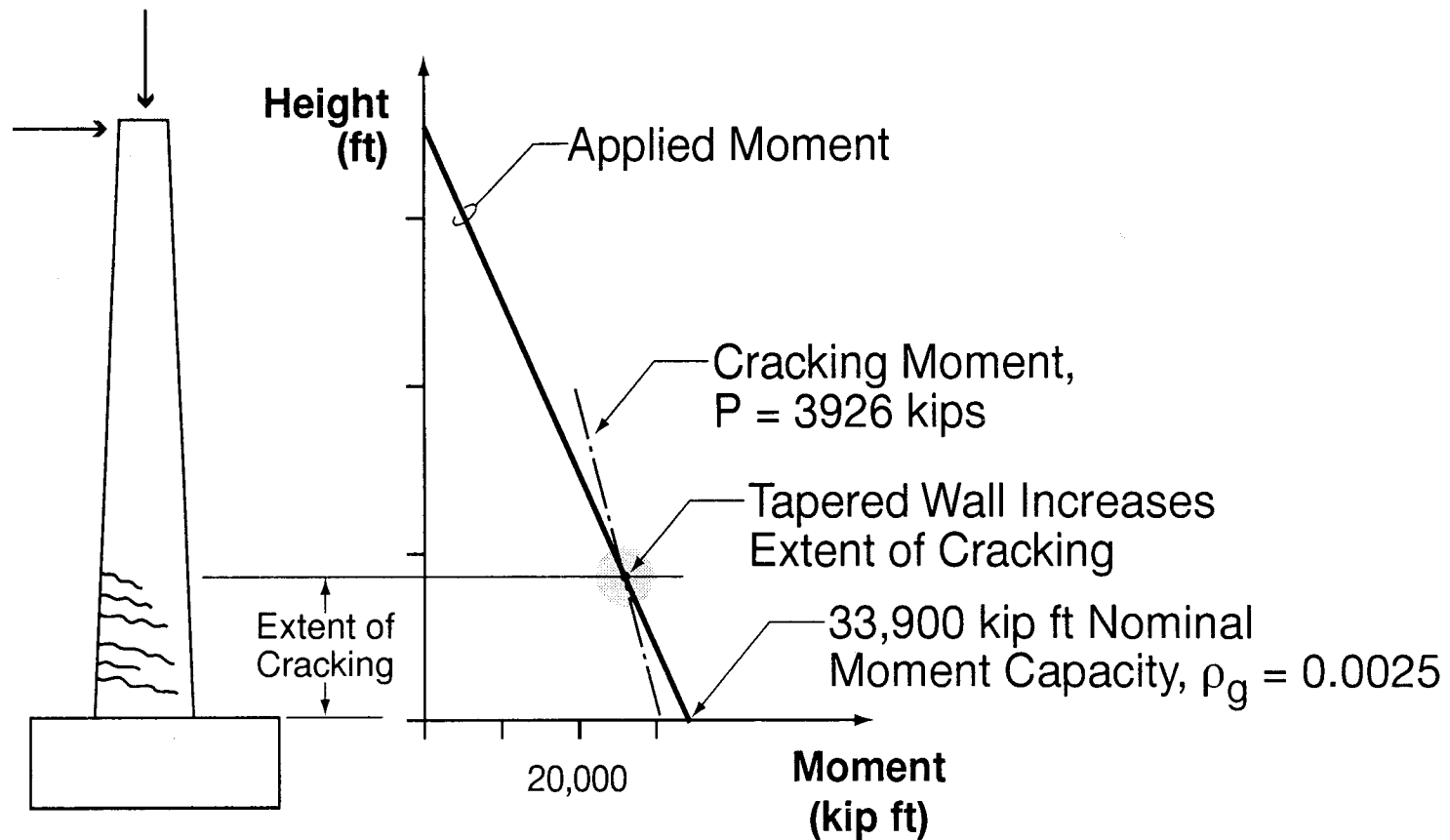
Minimum Vertical Steel Considerations

- a) Wall — $\rho_g \geq 0.0025$ SPC C & D Div. I-A. 7.6.3
- b) $\phi M_n \geq 1.2 M_{\text{crack}}$ (Flexural Members) Div. I 8.17.1.1

This Wall:

- $\rho_g = 0.0025$ Can Satisfy a) Since $R = 2$
- Consider b) for Crack Distribution

Distribution of Cracking

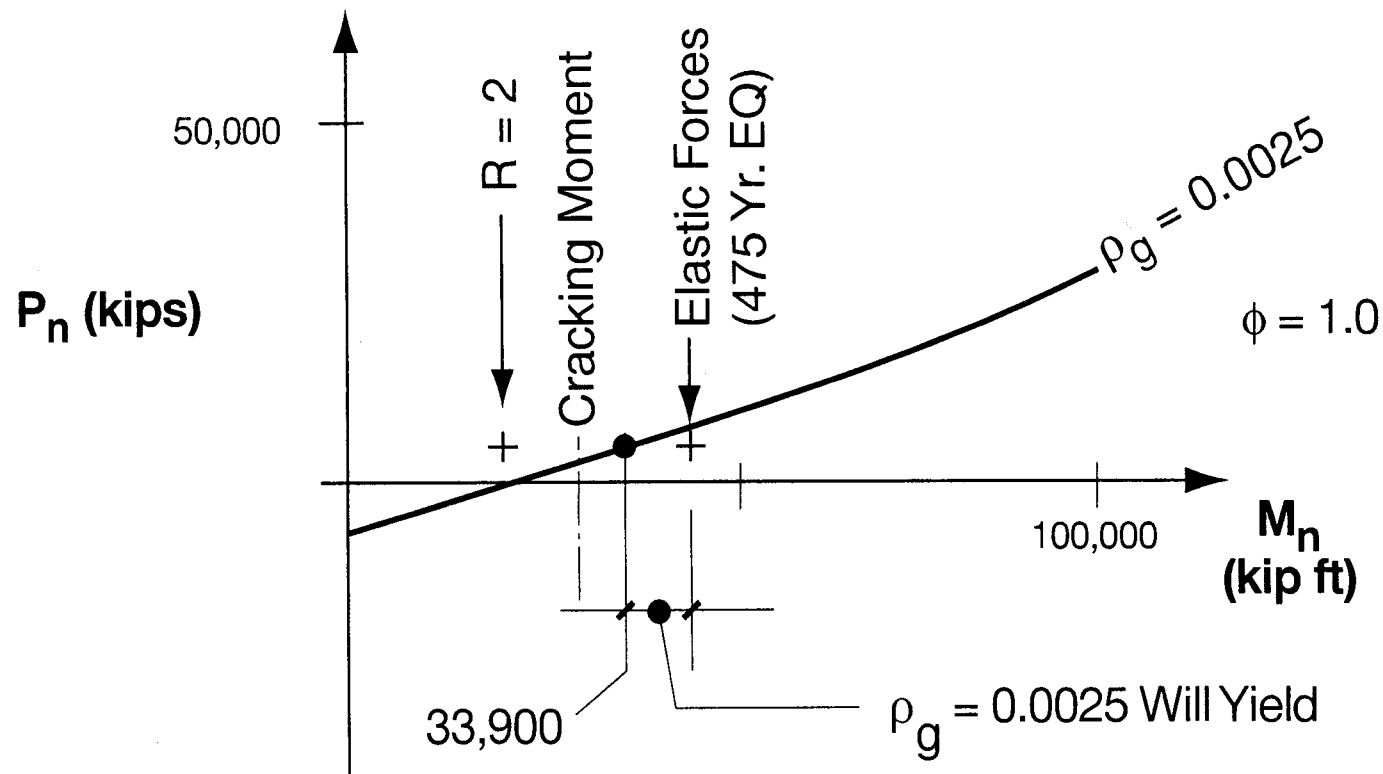


Selection of Vertical Reinforcement

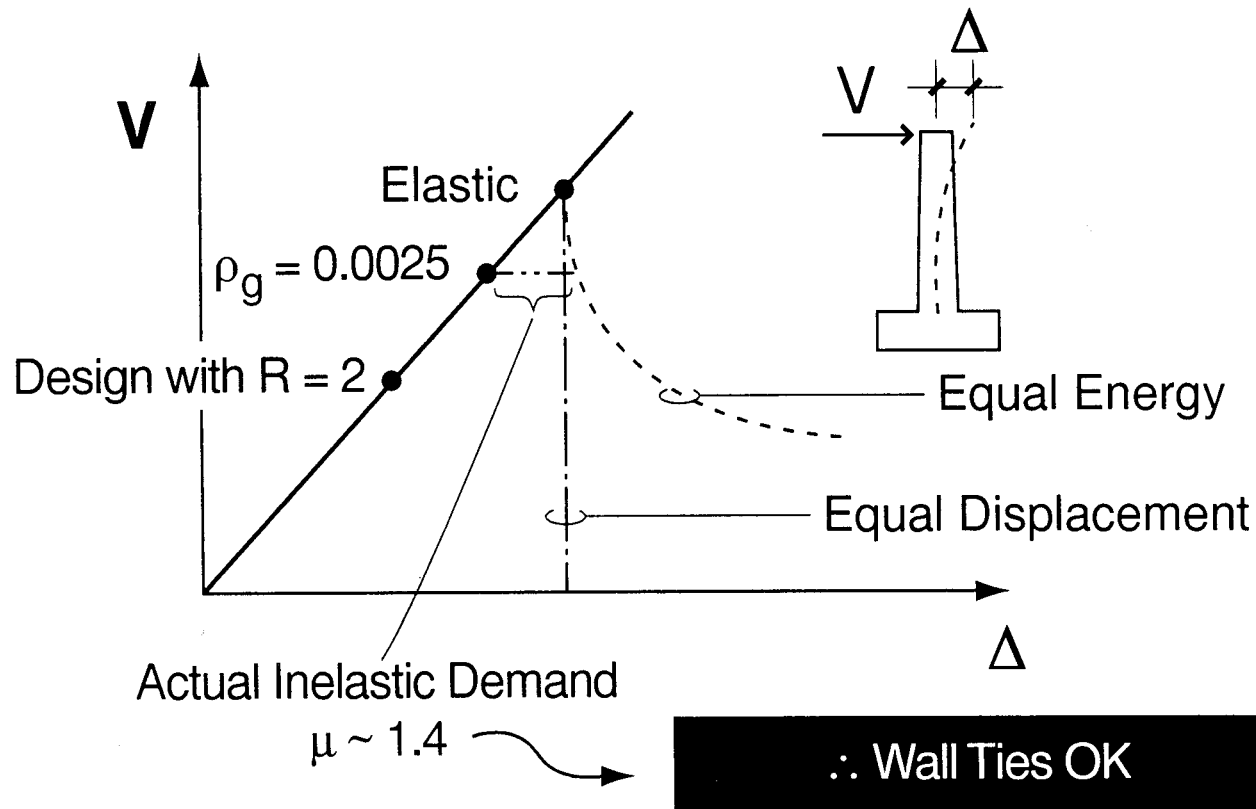
Use $\rho_g = 0.0025 \rightarrow 142 \text{ \#9 Bars}$

- This Will Work for $R = 2$
- Wall Is Expected to Yield During 475 Year Earthquake, but Ductility Demand Will Be Low ($M_{elas} \sim 1.2 M_n$)
- Even Though $M_n \sim 1.10 M_{cr}$, Cracking Will Be Distributed Due to Wall Taper

Nominal Capacity of Wall in Weak Direction



Expected Inelastic Demands

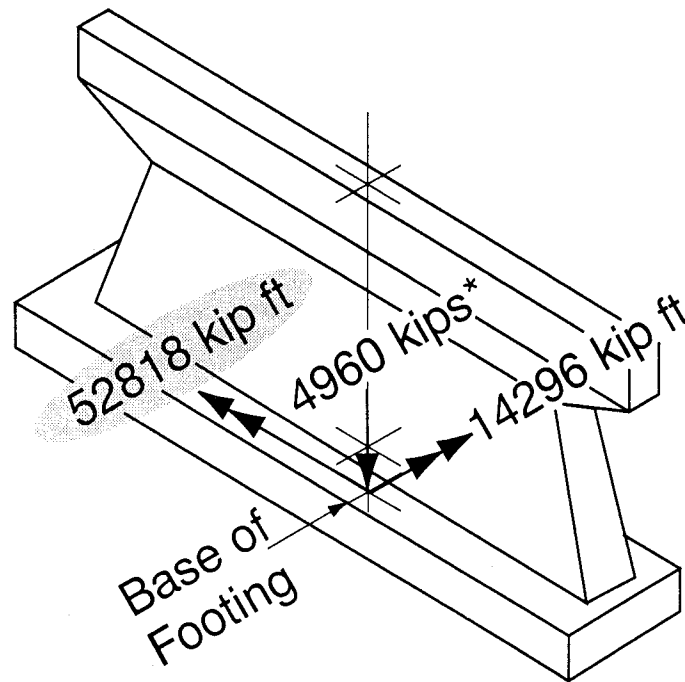


Wall Cross Ties

Weak Direction / Designed as a Column / $R = 2$

Use #4 at 2 ft O.C. Horizontal and 8 in. Vertical
See Design Example No. 2

Foundation Design Forces / Controlling Case LC1



$R = \frac{2}{2}$ Weak

$R = \frac{2}{2}$ Strong

*Does Not Include
Buoyancy and Stone Fill

Foundation Behavior / 33' Footing

Results for:

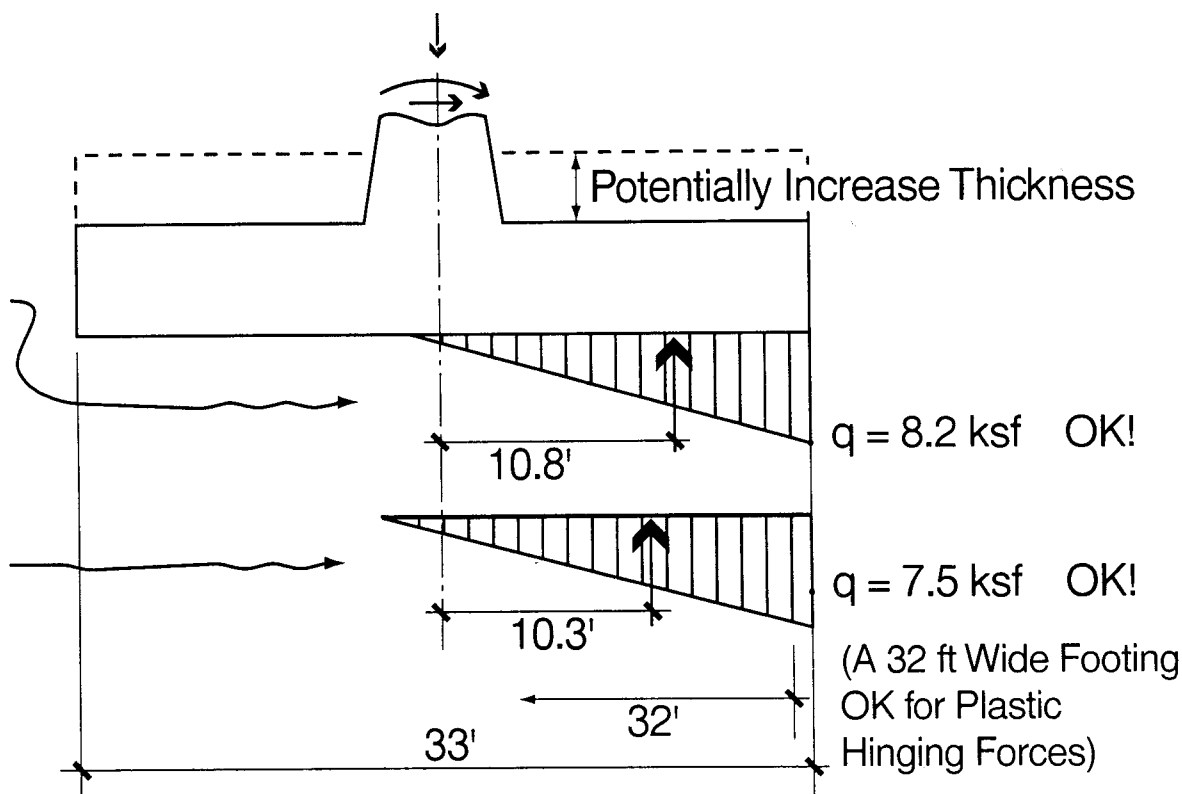
- Design Forces

$$R = \frac{2}{2}$$

(Elastic)

- Plastic Hinging Forces

$$\rho_g = 0.0025$$



Choices and Implications / Flexural Design

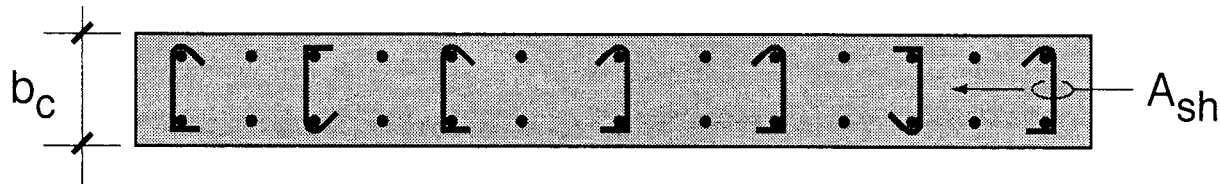
SPC B Weak Direction

	R = 2 (Wall)	R = 3 (Column) 1% Vertical Steel
Wall:	Less Vertical Steel ($\rho_g = 0.0025$)	More Cross Ties in Hinge Zone
Foundation:	Larger Footing	Smaller Footing

Cross Ties

Weak Direction / Designed as a Column / $R = 3$

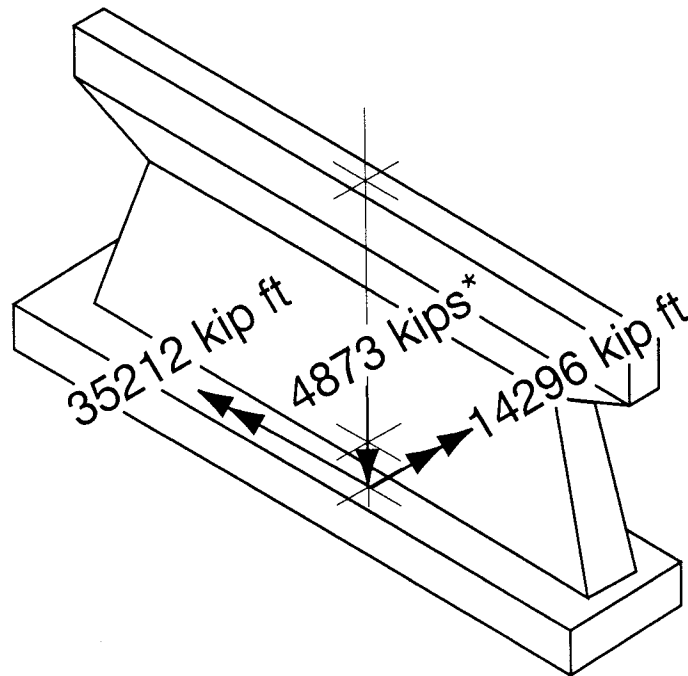
$$\text{I-A / 6.6.2} \quad A_{sh} = 0.3ah_c \left[\frac{A_g}{A_{core}} - 1 \right] \geq 0.12ah_c \frac{f'_c}{f_{yh}}$$



Try #7 \rightarrow 63 Required / Use 67 #7 Cross Ties, One for Each Vertical, at 6 in. Vertical Spacing

Cross Ties Required Over Lower 6 ft ~ Plastic Hinge Zone

Foundation Design Forces



Design as a Column

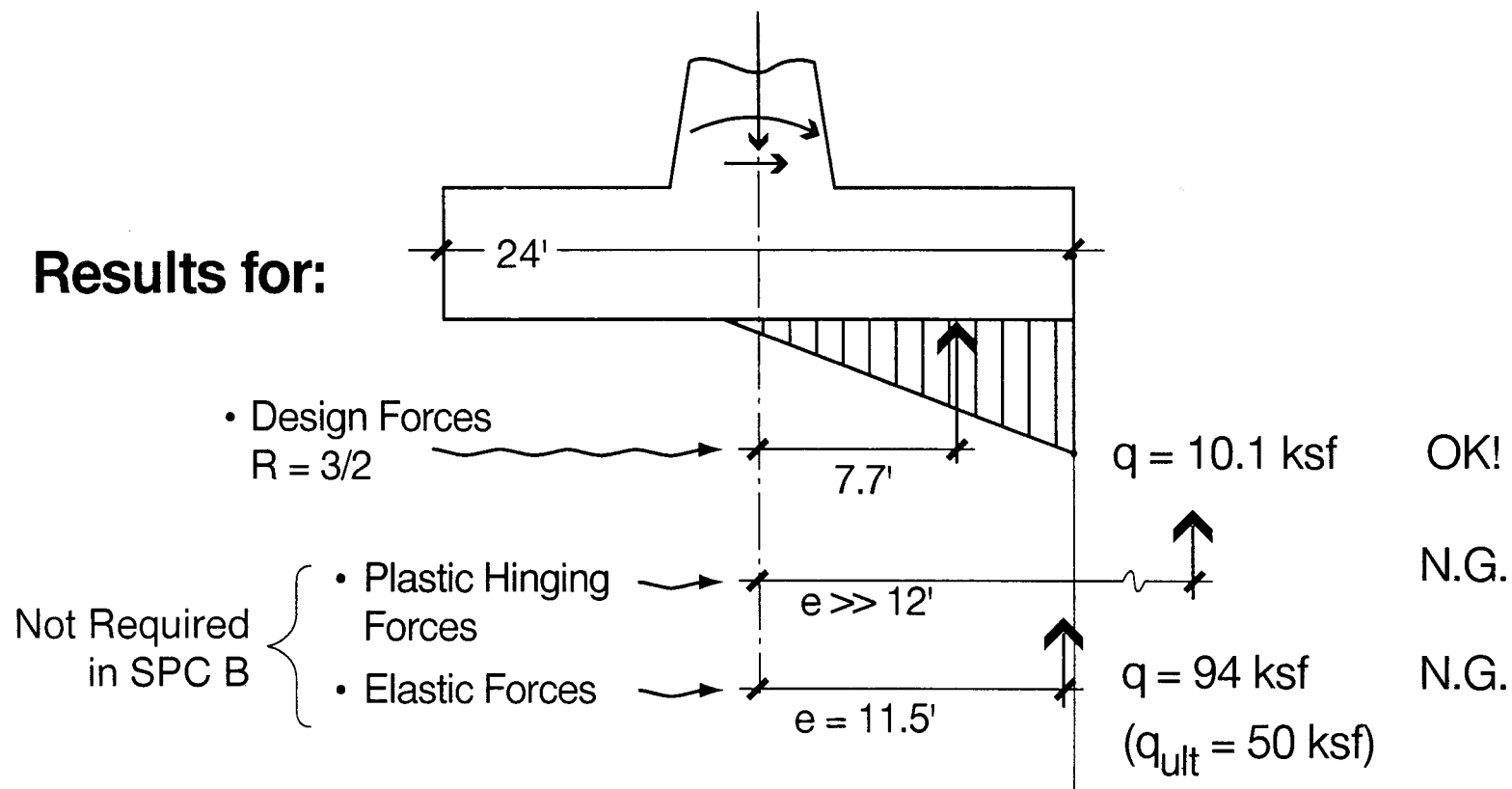
$R = \frac{3}{2}$ Weak

$R = 1$ Strong

*Does Not Include
Buoyancy and Stone Fill

Foundation Behavior / 24' Footing

Results for:



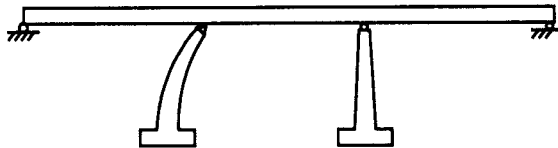
Summary

	Designed As:	
	Wall	Column
Vertical Reinforcement	10 Tons	40 Tons ($\rho_g = 0.01$)
Cross Ties	0.6 Tons	4.6 Tons
Footing Width.....	33 ft	24 ft*

* Permitted by Code for SPC B, But if Designed for Elastic or Hinging Forces 33 ft Would Be Required

Choices and Implications

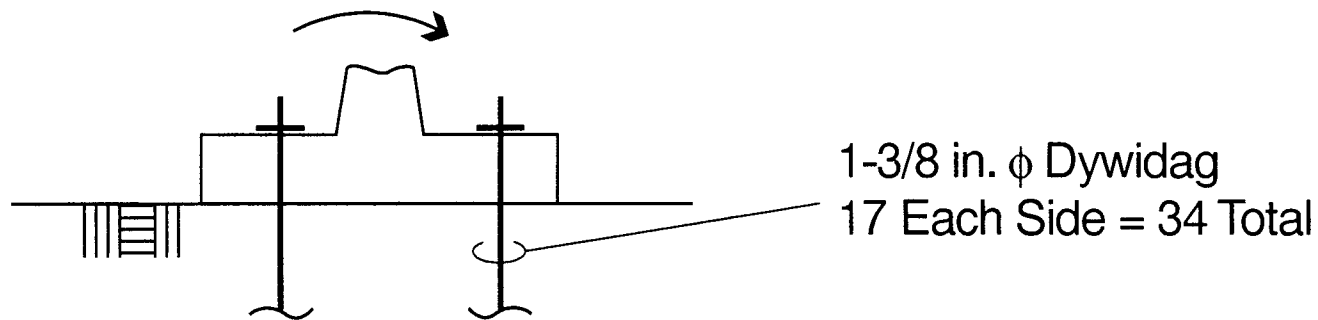
1. Use 33 ft Footing ... Design as a Wall



- Best Solution for Single Conventional Bearing Configuration
- No Foundation Damage

Alternative

2. Use 16 ft Footing ... Use Rock Anchors to Prevent Overturning

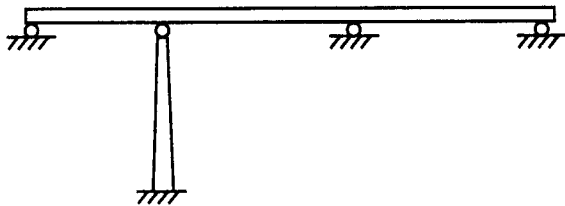


Session 3

Conceptual Design Considerations

- **Conventional vs. Elastomeric Bearings**
- **Longitudinal Releases and Restraints**

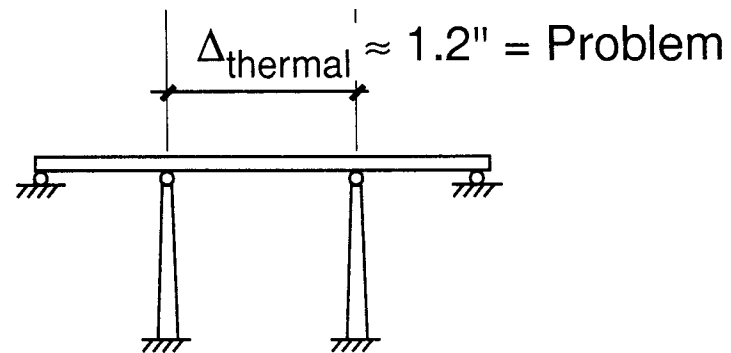
Conventional Bearings



$$T = 0.52 \text{ sec}$$

$$\Delta = 0.74 \text{ in.}$$

One Restraint



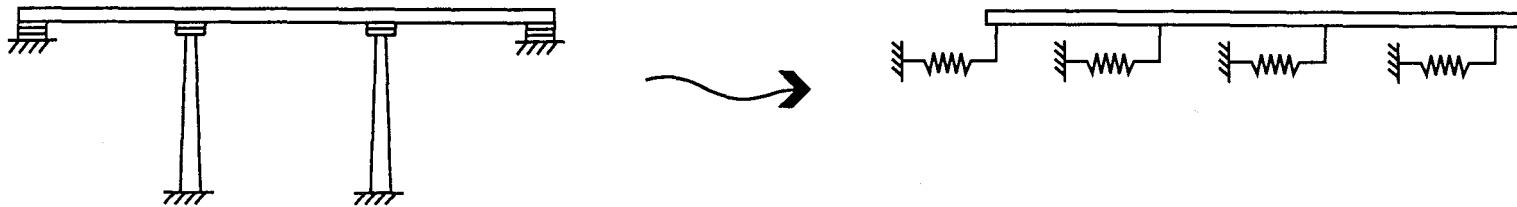
$$T = \frac{0.52}{\sqrt{2}} = 0.37 \text{ sec}$$

$$\Delta = 0.74 \text{ in.} \left(\frac{1}{\left(\frac{1}{\sqrt{2}} \right)^{2/3}} \right) \frac{1}{2} = 0.47 \text{ in.}$$

No. of Piers

Two Restraints

Elastomeric Pads at Each Support

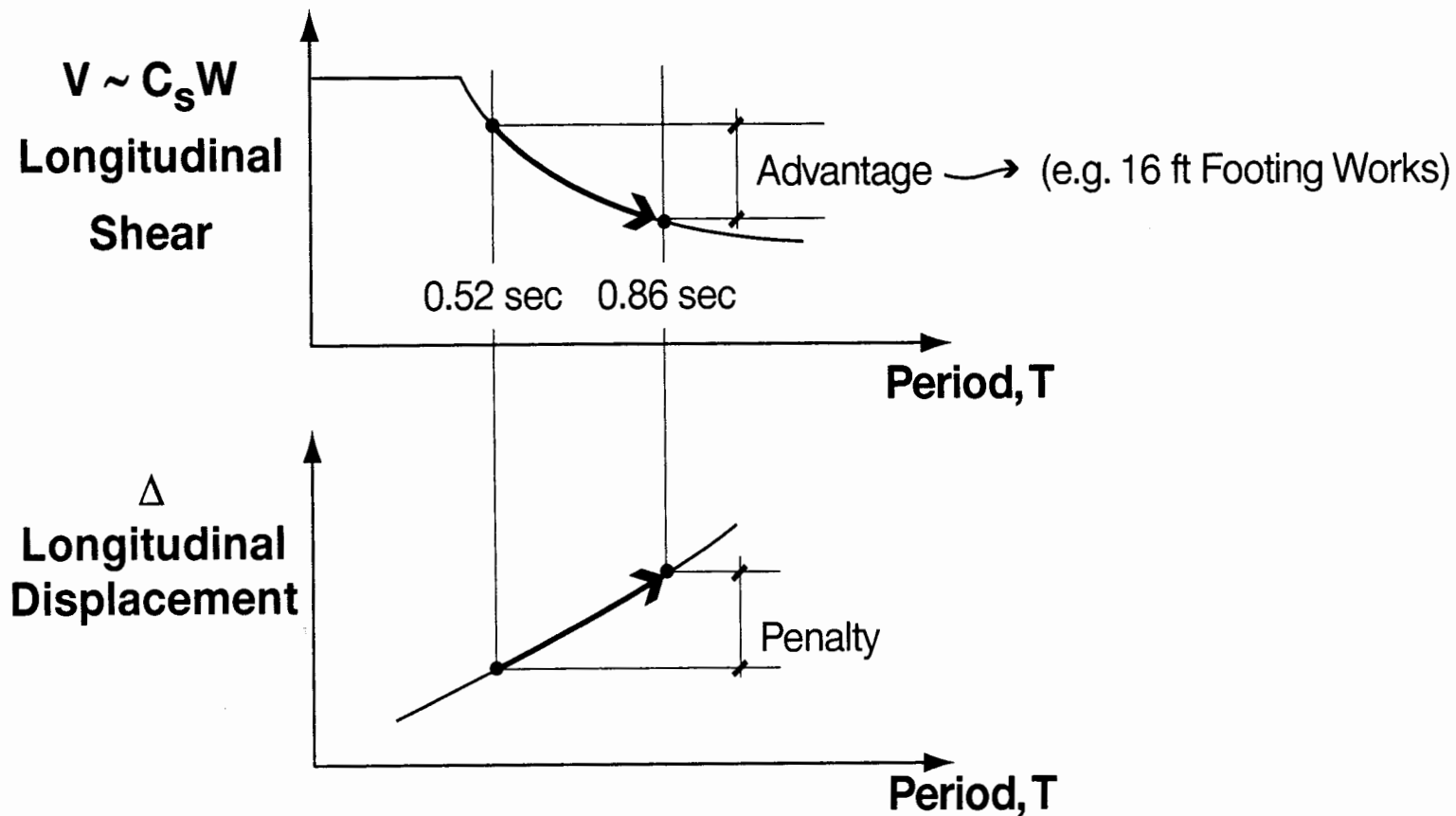


Incorporate
Flexibility of
Elastomeric Pads

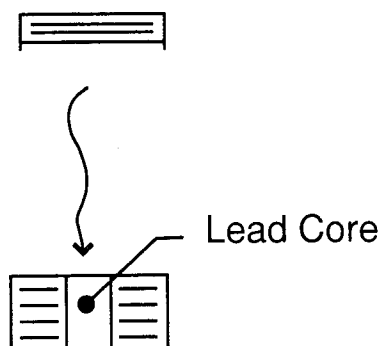
$T \rightarrow 0.86 \text{ sec}$

$\Delta \rightarrow 1.44 \text{ in.}$

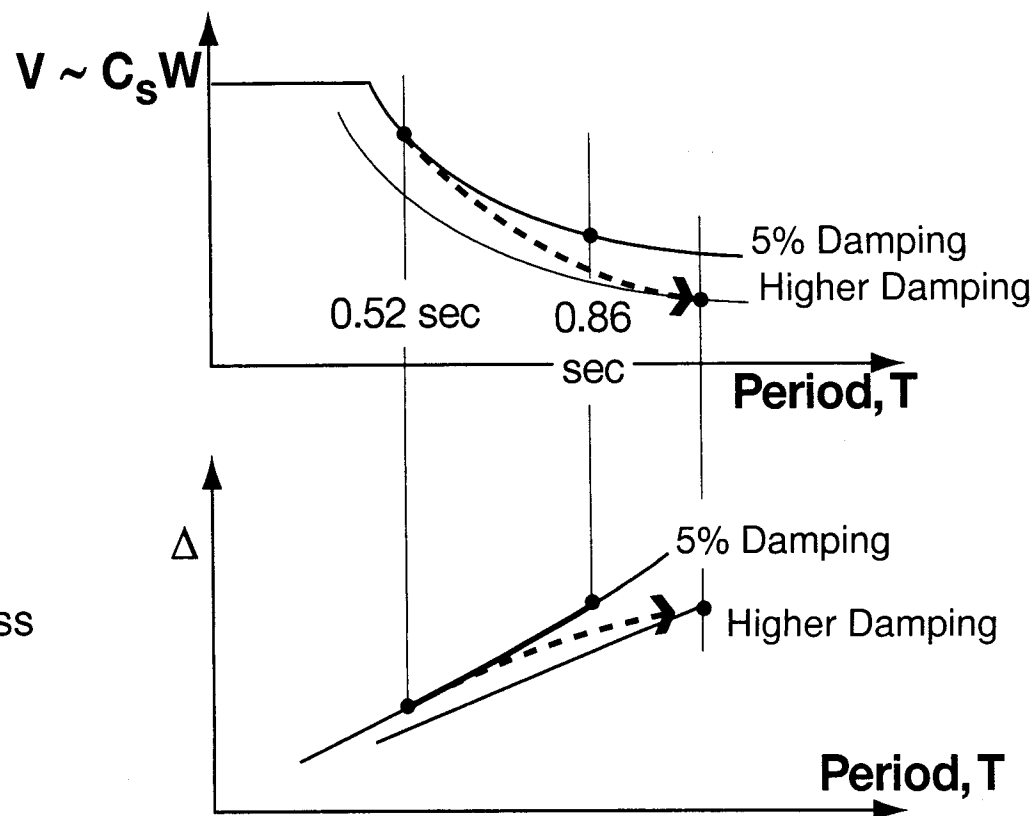
How the Elastomeric Pads Affect the System



How a 'Base Isolated' Concept Would Affect System



- **Lead Core**
Damping
Low Amplitude Stiffness
- **Increased Height**
Added Flexibility

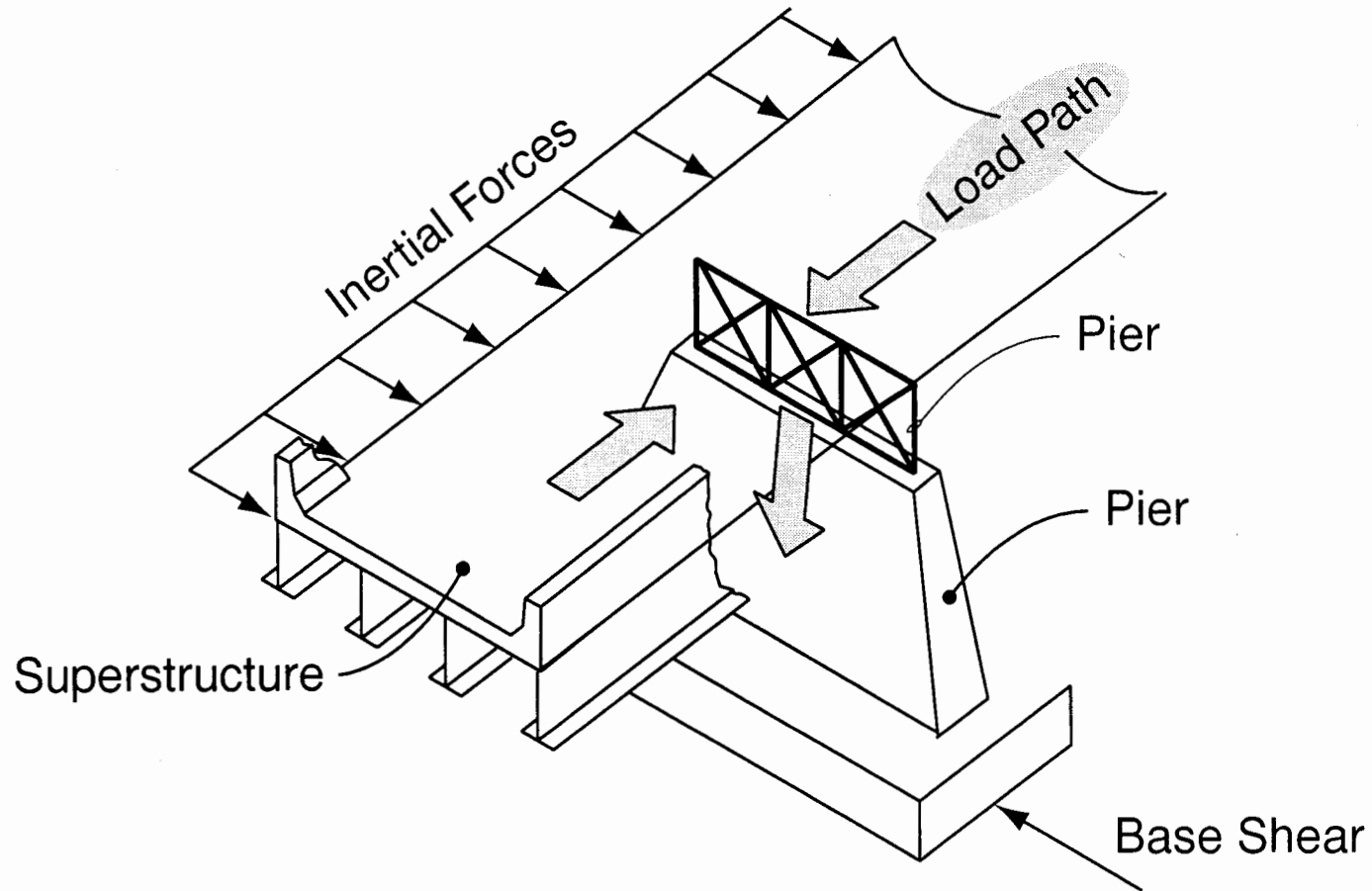


Session 3

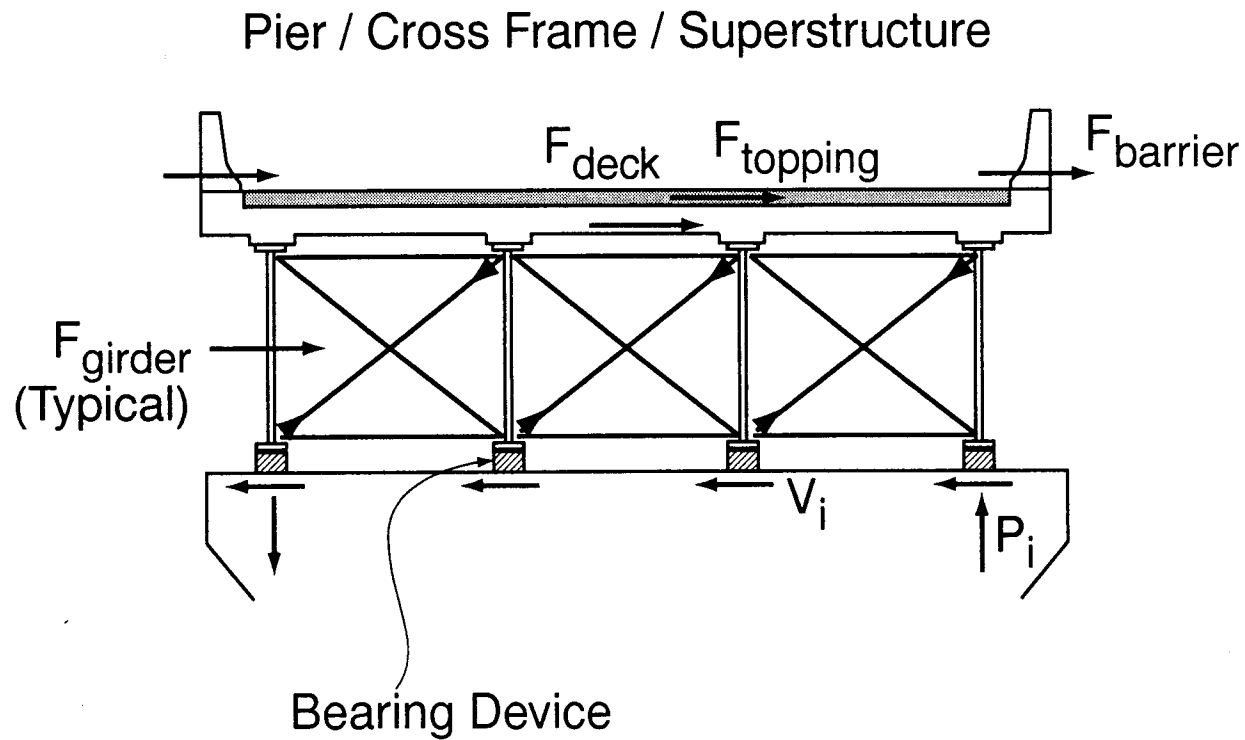
Steel Superstructure Issues

- **Cross Frame Design**
- **Shear Key Considerations**

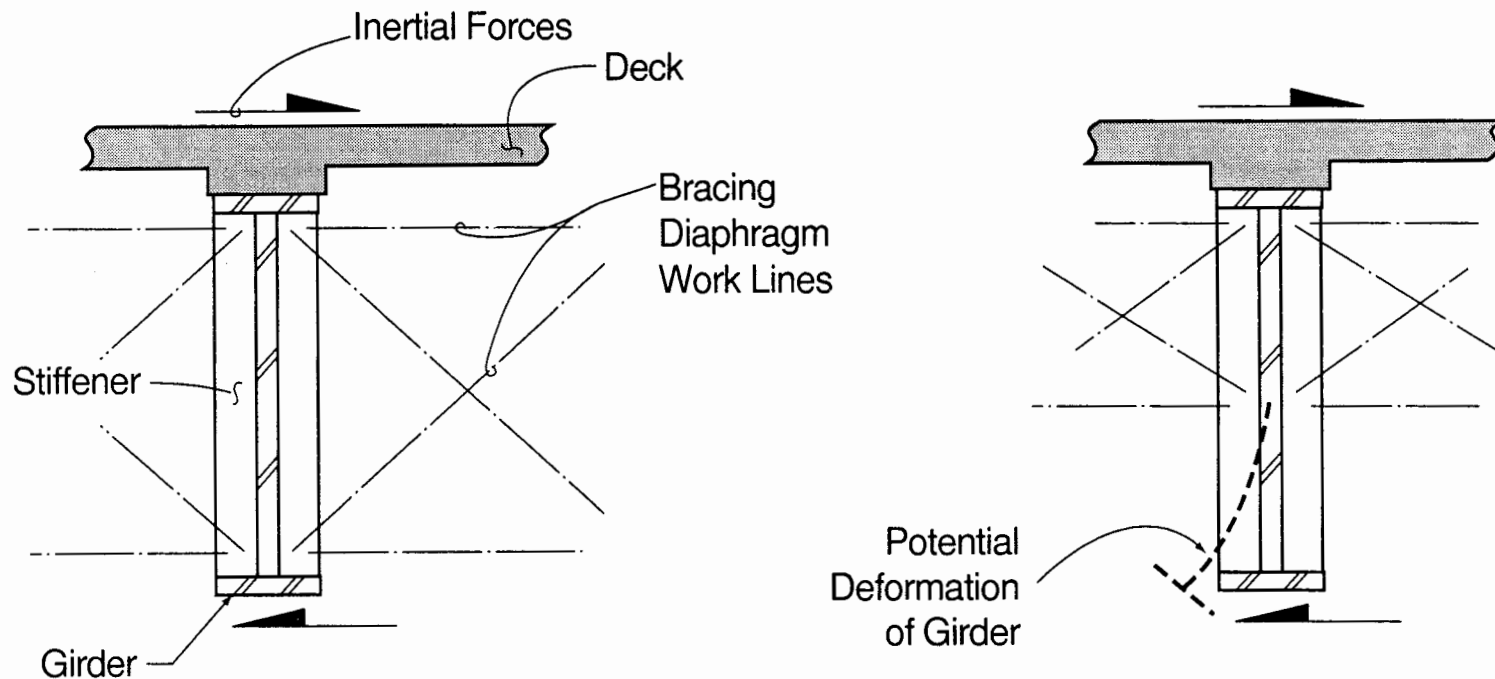
Inertial Forces and Lateral Load Path



Cross Frame Forces



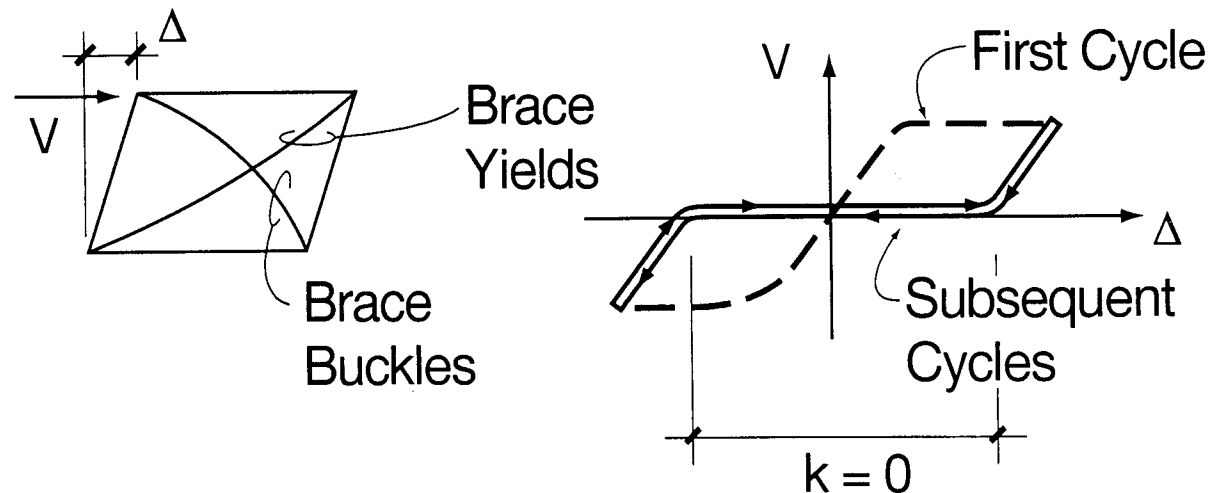
Failure Mode / Lateral Bending



Lateral Rigidity vs. Service Load (Fatigue) Performance

Failure Mode / Tensile Yielding

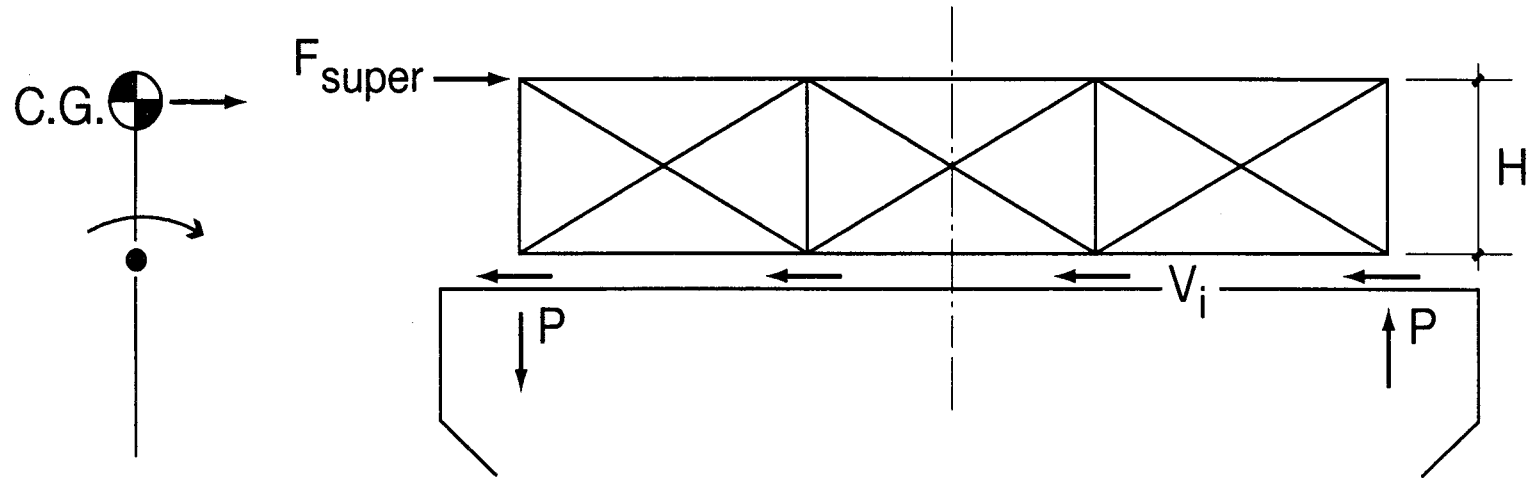
Problem with
Cross Frame
Yielding



Code Specifies $R = 1.0$ to Prevent Yielding

- Preserves Elastic (Tight) Response
- Preserves Lateral and Gravity Load Paths

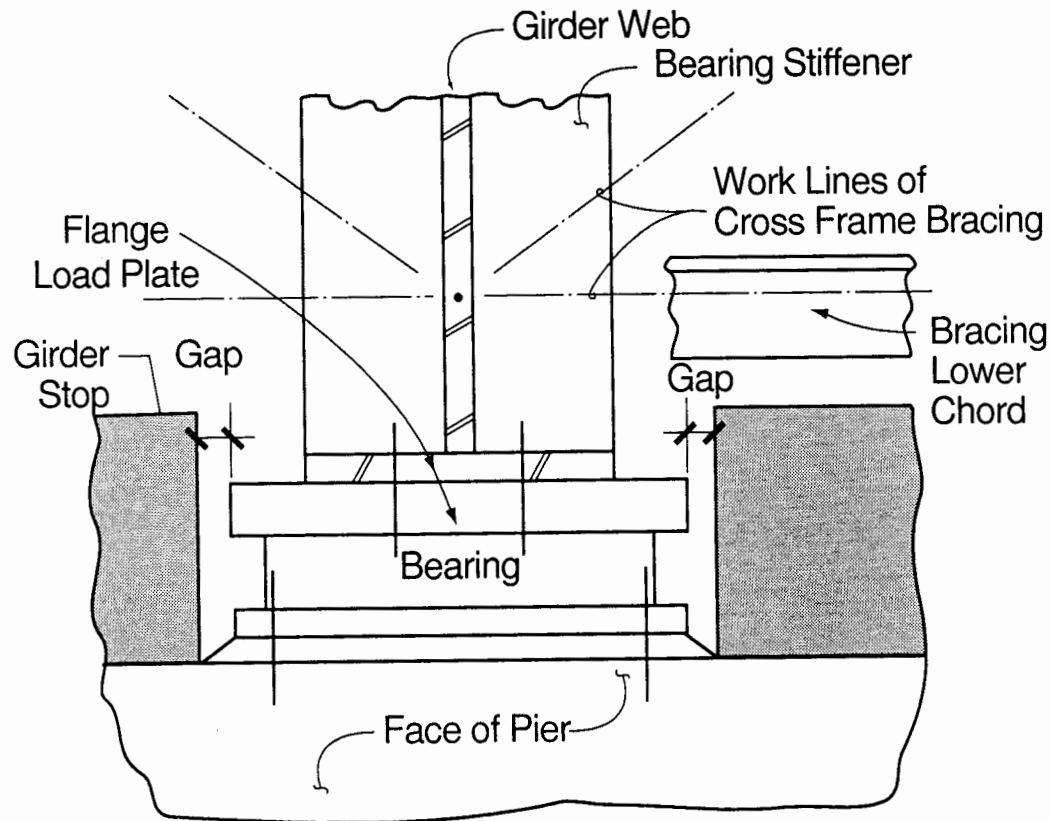
Seismic Model vs. Actual Structure



$$V_i \approx \frac{F_{\text{super}}}{n} \quad \dots \quad \text{Actual May Be Higher Due to Tolerances}$$

For Relatively Flexible Superstructure Overturning Is Resisted Primarily at Exterior Bearings

Shear Keys / Girder Stops



- Failsafe Load Path for Bearing
- Load May Not Be Even Due to Construction Tolerances (Unbuttoning)
- Design to Fail in Ductile Manner

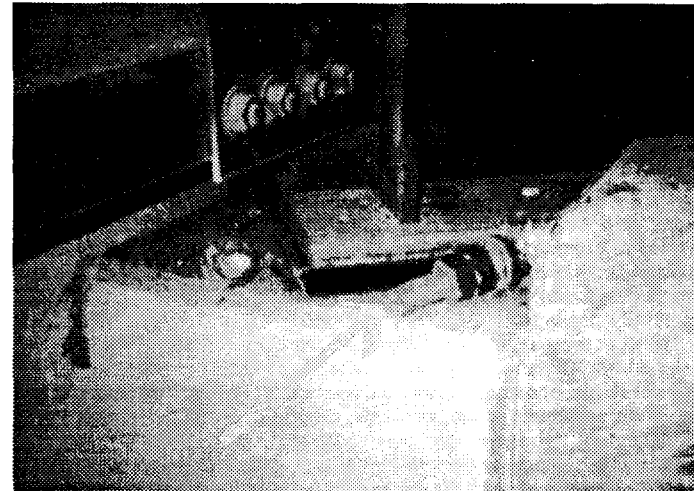
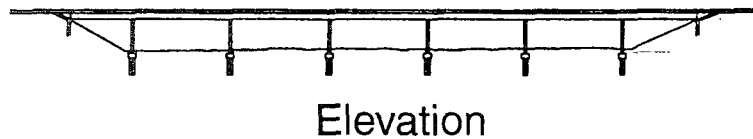
Session 4

Steel Plate Girder Bridge Example

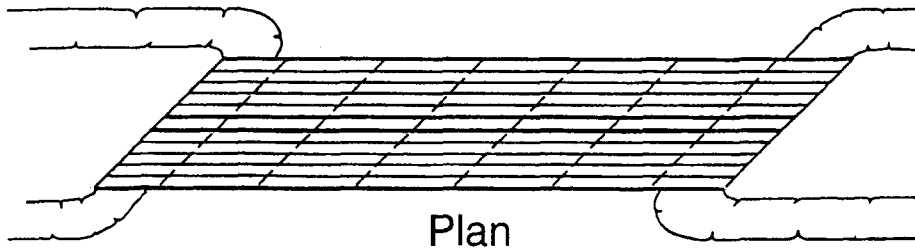
Skew Structure Issues

- **Conceptual Behavior**
- **Stiffness Considerations**
- **Bearing Orientation and Releases**
- **Effects on Lateral Behavior**

Damage to Steel Superstructure Bridge

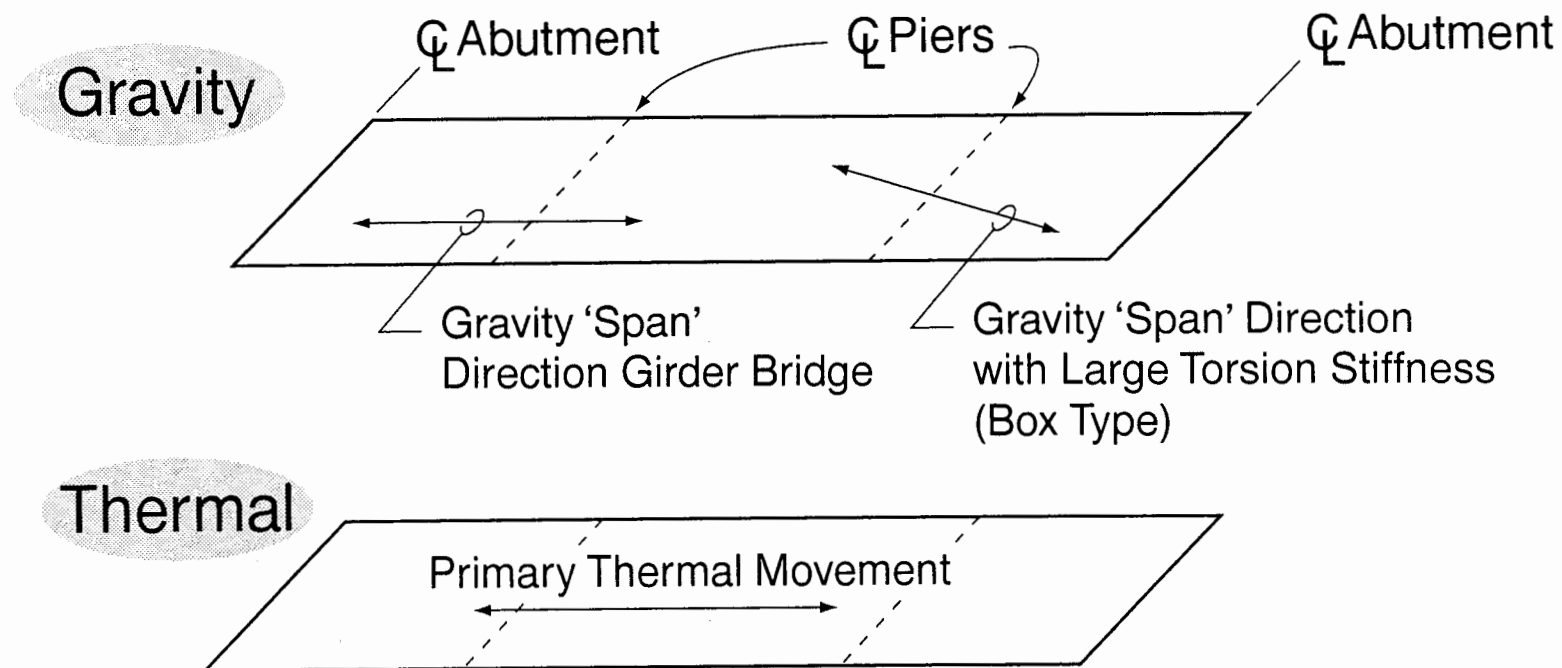


Sheared Anchor Bolts

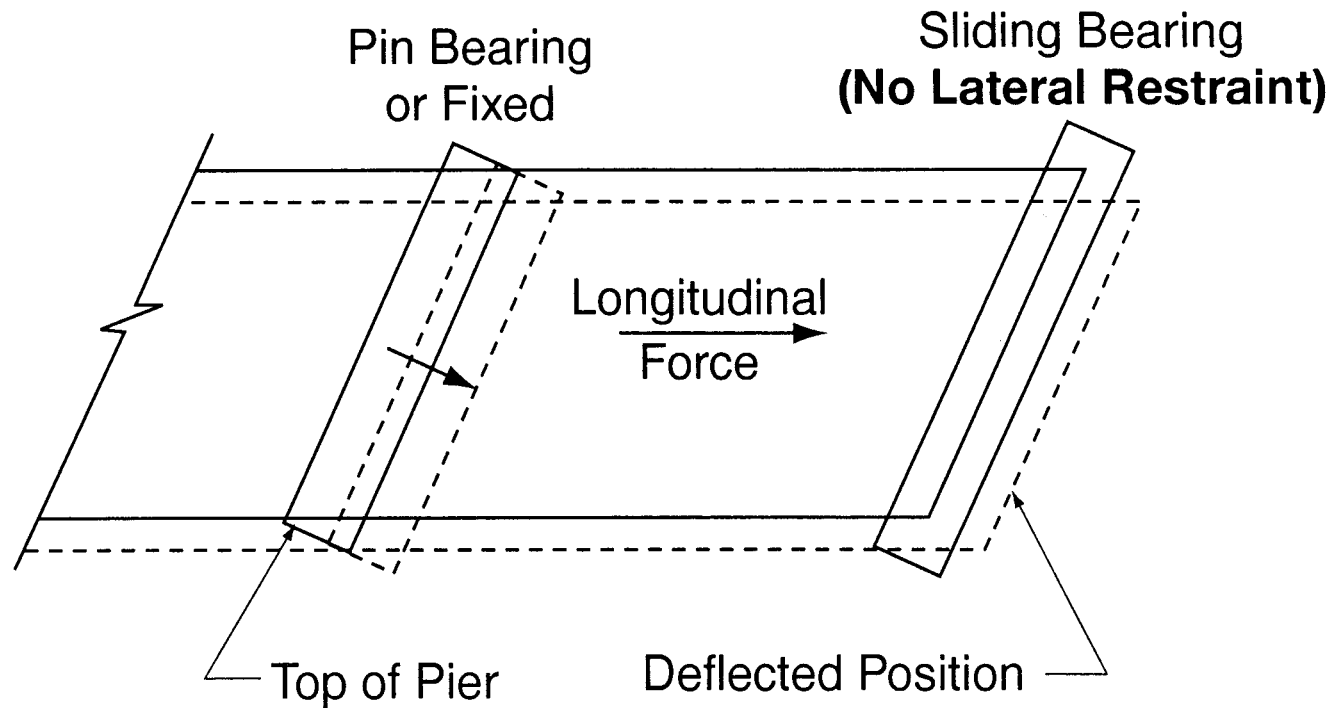


EERI (1995)

Skew Behavior Under Gravity and Thermal Loads

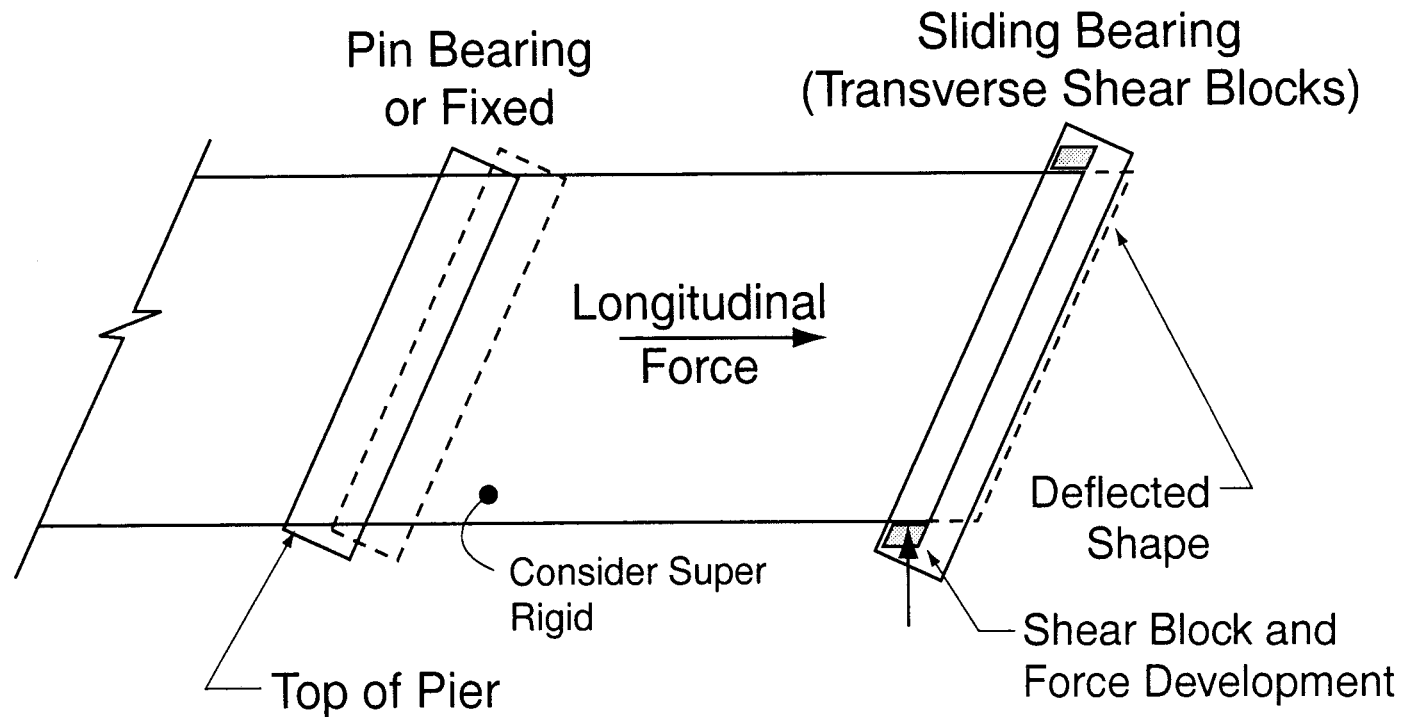


Lateral Loading Concepts




Plan View

Lateral Loading Concepts (continued)



Plan View

Lateral Behavior Observations

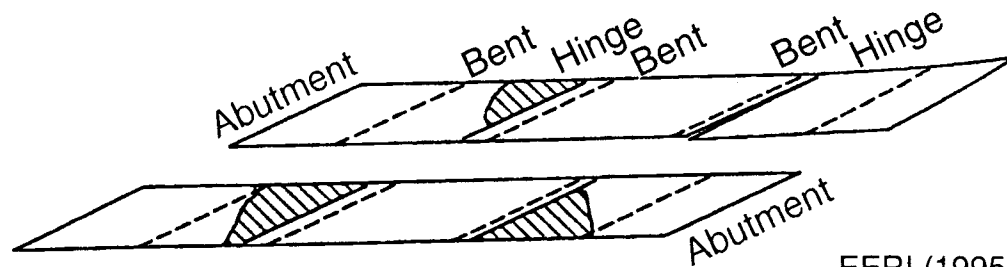
- Bridge Would Like to Move Along Weak Axis of Piers
- Shear Blocks Oriented Transversely Prevent Such Movement  Large Transverse Forces?

- Behavior Coupled in Orthogonal Plan Directions

$$F_{\text{long}} \text{ } \text{~~~~~} \rightarrow F_{\text{trans}} \text{ and } F_{\text{trans}} \text{ } \text{~~~~~} \rightarrow F_{\text{long}}$$

- Twisting Also Likely if Mass and Stiffness Centers Are Not Coincident

Damage to Skewed Box Girder Bridge



EERI (1995)



USCD (1994)

- End Spans Have Large Eccentricity Between C.M. and C.S.

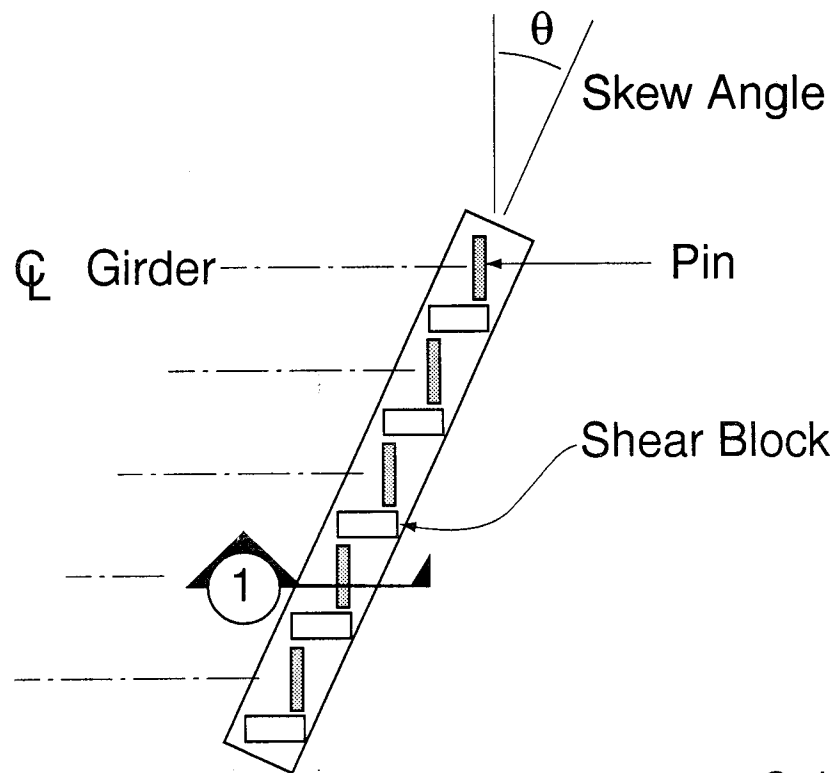
Session 4 Page 7 of 42

UMD-ITV

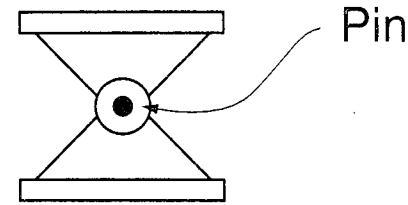
Seismic Bridge Design Applications

25 July 1996, NHI Course Code No. 13063

Steel Superstructure Bearing Orientation



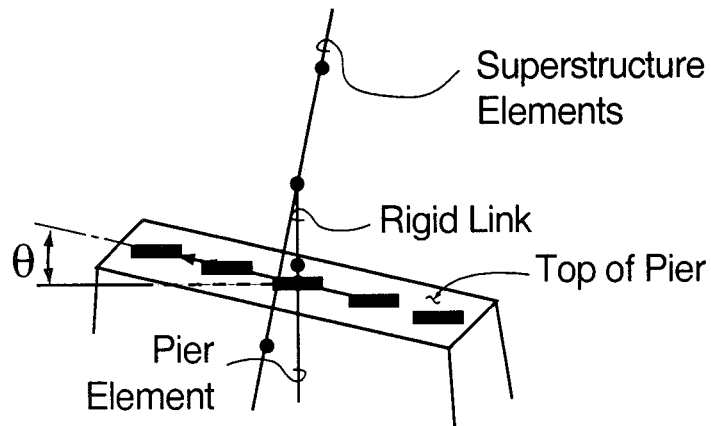
Plan View



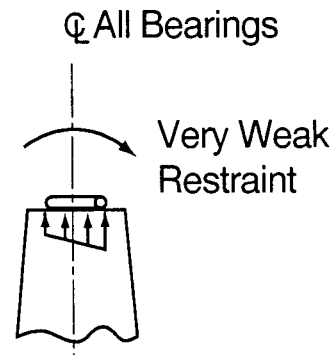
Section 1

- Selection of Seismic Model Releases Is Important

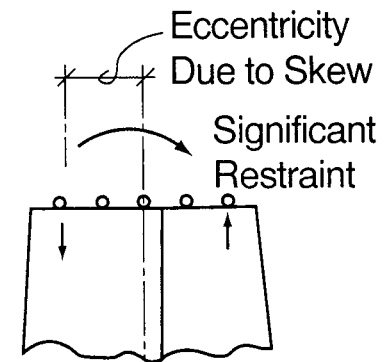
Release Directions for Bearings



**Rotational Release
for Pin Bearings**



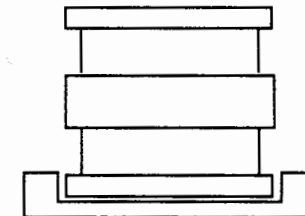
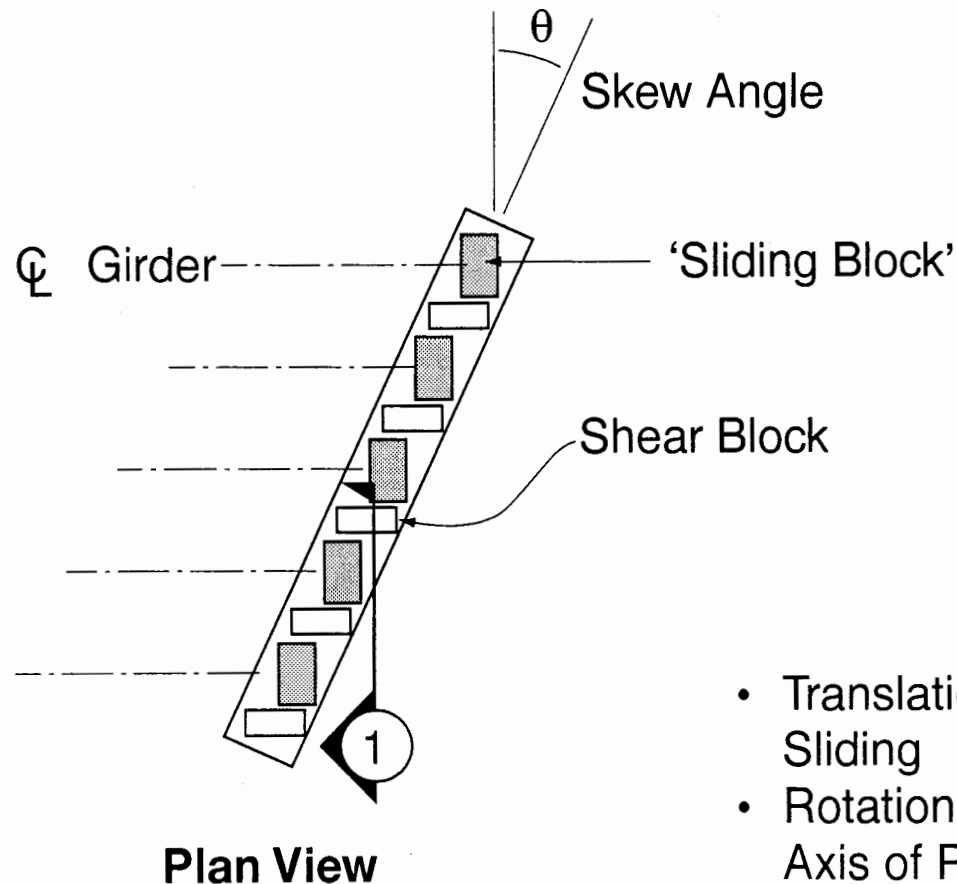
**Looking Along Weak
Axis of Pier**



**Elevation from
Side of Bridge**

Use Rotational Release About Weak Axis of Pier

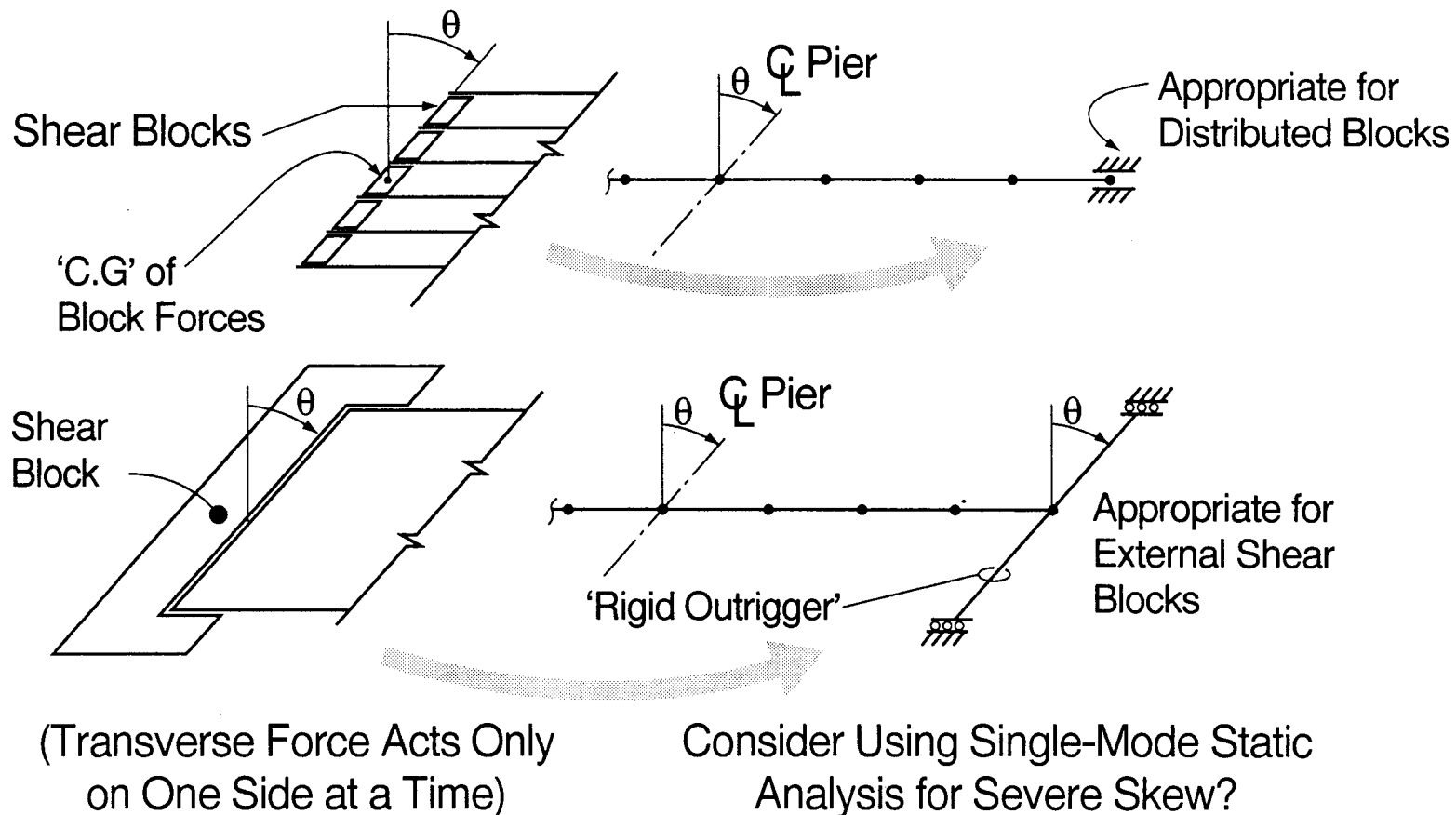
Sliding Bearing Orientation



Section 1

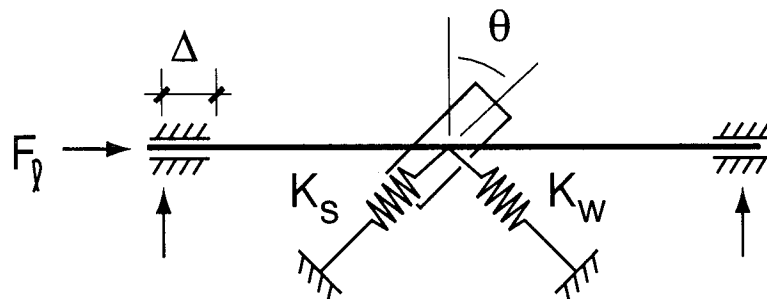
- Translational Release in Direction of Sliding
- Rotational Release About Weak Axis of Pier

Modeling Considerations for Shear Blocks



Stiffness Considerations (1 of 3)

Consider a Two-Span **Rigid Deck** System as Shown



Plan View

- For a Given Longitudinal Displacement, the Transverse Forces Developed by K_s and K_w Are Not Equal

\therefore Transverse Reactions Are Required

Stiffness Considerations (2 of 3)

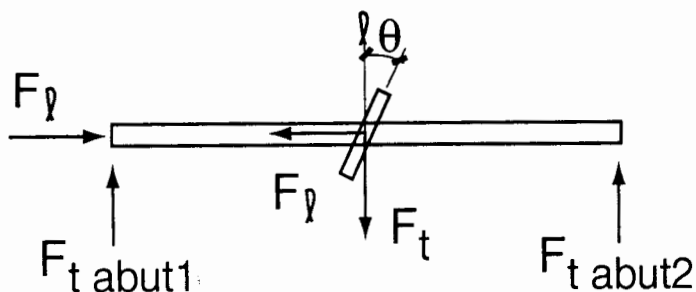
- It Can Be Shown That

$$K_l = K_s \sin^2 \theta + K_w \cos^2 \theta$$

Structure Stiffness in
Longitudinal Direction

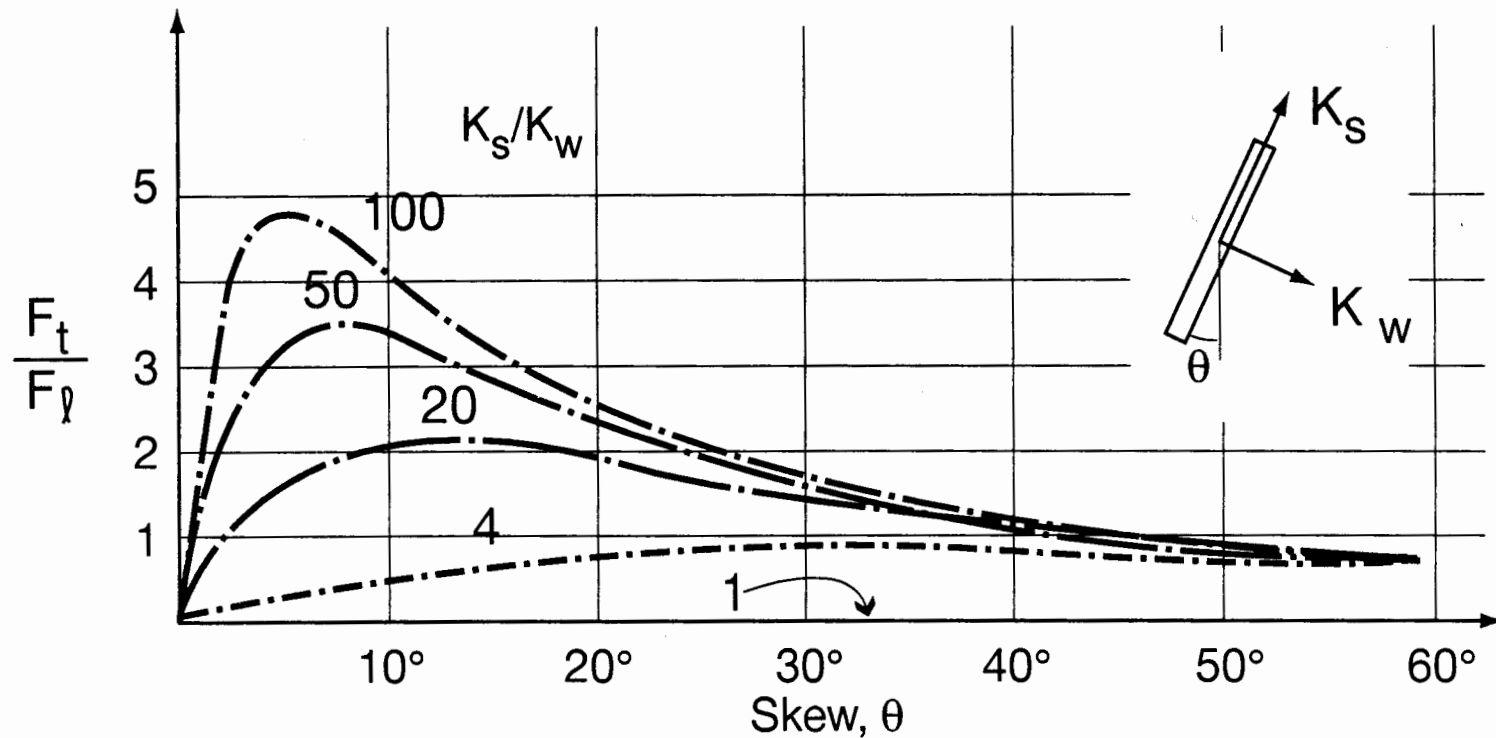
$$\frac{F_t}{F_l} = \frac{(K_s - K_w) \sin \theta \cos \theta}{(K_s \sin^2 \theta + K_w \cos^2 \theta)}$$

Ratio of Transverse
Force to Longitudinal Force
for a Given Displacement



Plan View

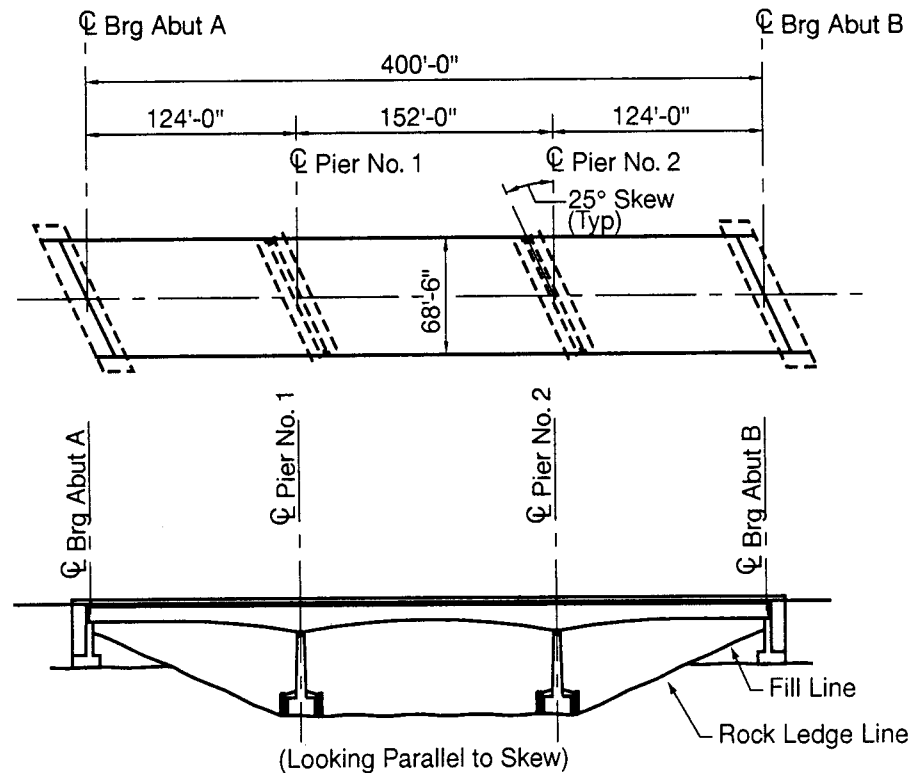
Stiffness Considerations (3 of 3)



- For Infinitely Stiff Superstructures, Large Transverse Forces May Develop!

Example / Effects of Skew (1 of 6)

- Consider Practice Problem No. 2 with 25° Skew

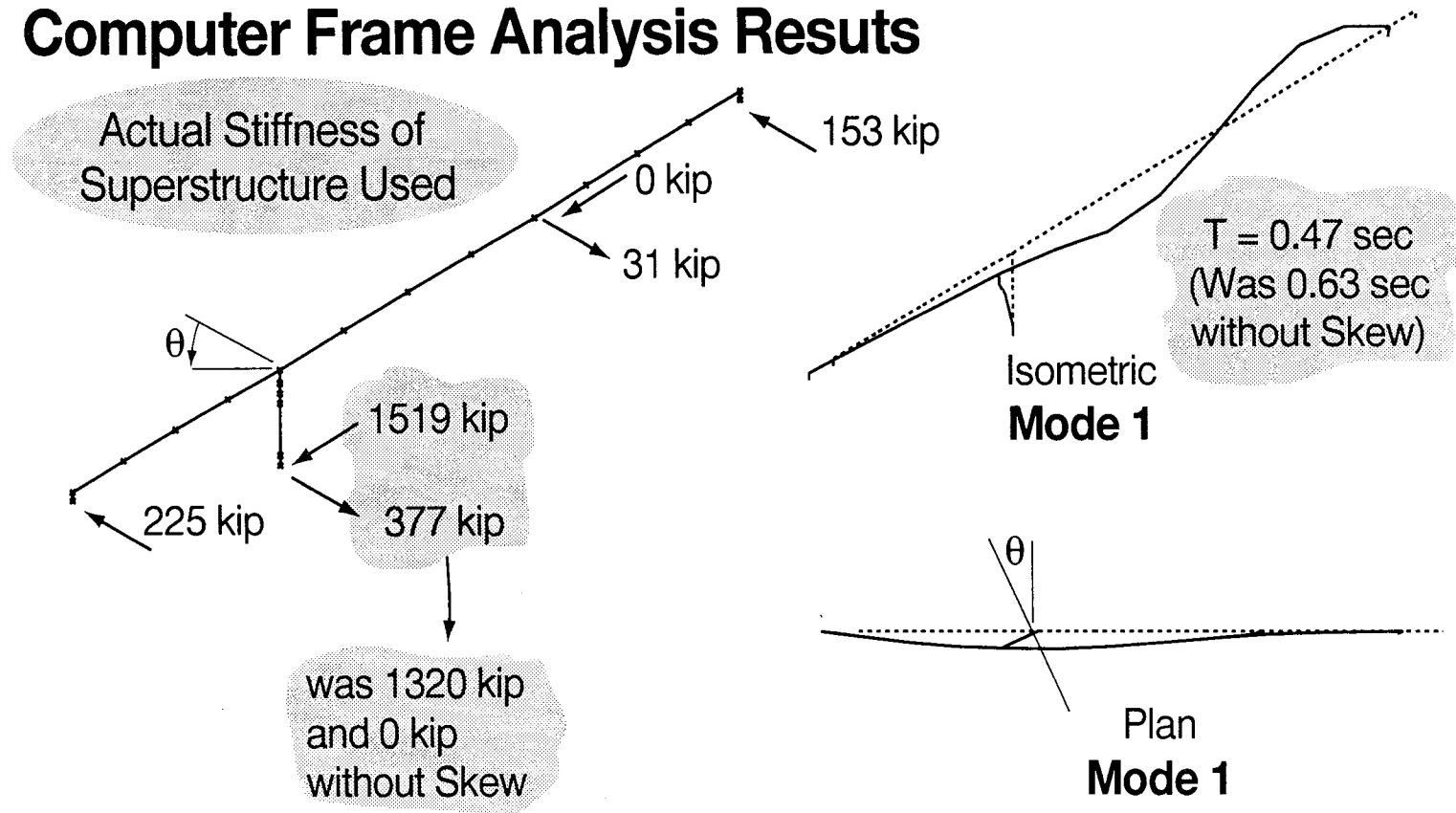


Example / Effects of Skew (2 of 6)

Determine the Longitudinal Base Shear and Transverse Restraint Forces by Frame Analysis and by Hand for Longitudinal Earthquake

Example / Effects of Skew (3 of 6)

Computer Frame Analysis Results



Example / Effects of Skew (4 of 6)

Hand Analysis (Assume Rigid Superstructure)

Recall Pier Stiffness, $K_{\text{weak}} = 27150 \text{ kip/ft}$
Seismic Weight, $W = 6041 \text{ kip}$

Strong Direction
Pier Stiffness } Approximate Using:

Width = 60 ft, Thk = 5 ft

H = 36 ft

E = 519,000 ksf G = 220,000 ksf

Example / Effects of Skew (5 of 6)

$$K_{\text{strong}} = 1,140,000 \text{ kip/ft} \quad \frac{K_s}{K_w} = \frac{1140000}{27150} = 42$$

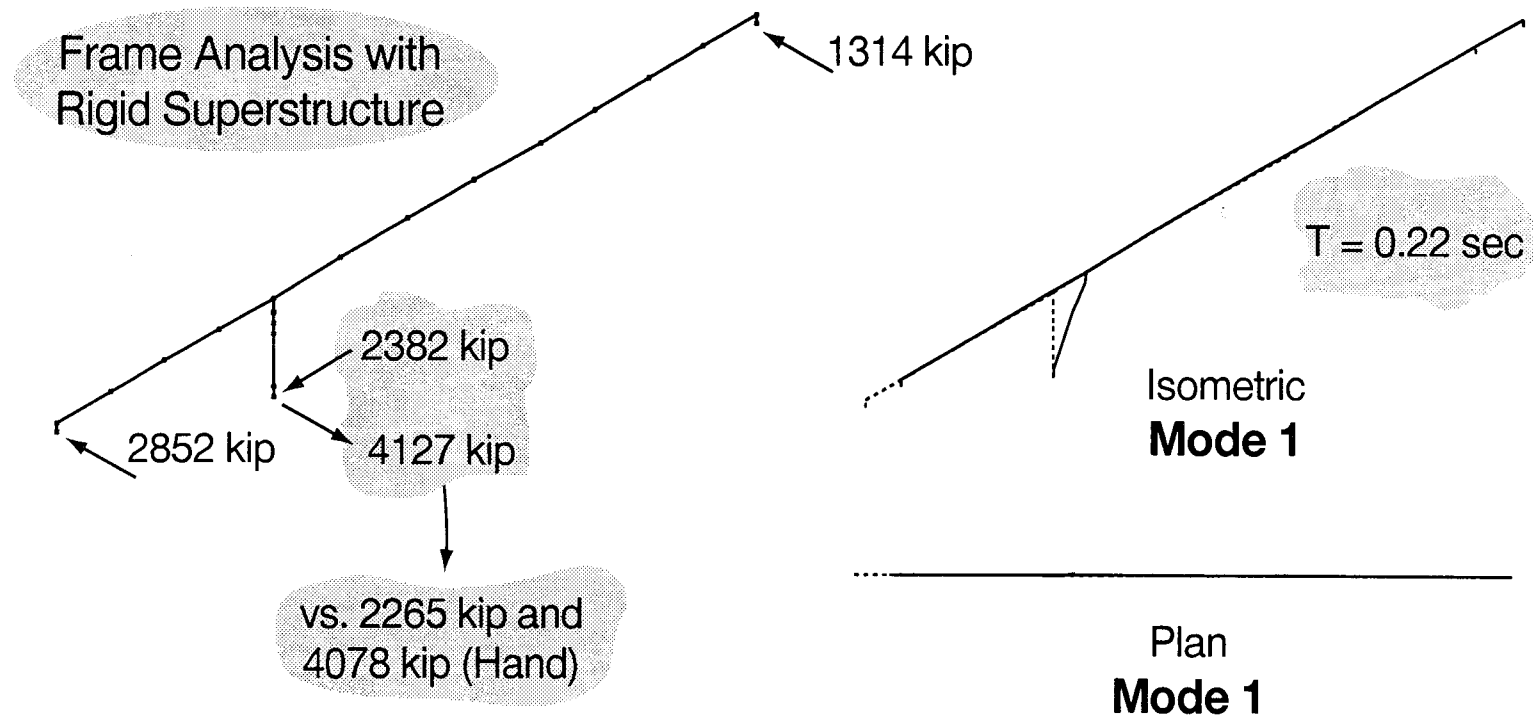
$$\text{Using Plot, } \theta = 25^\circ \quad \frac{F_t}{V_\lambda} = 1.8$$

$$K_{\text{long}} = K_s \sin^2 \theta + K_w \cos^2 \theta = \underbrace{205,200 + 22,300}_{9.2/1} = 227,500 \text{ kip/ft}$$

$$T = 0.18 \text{ sec} \quad C_s = 0.375 \quad V_\lambda = 2265 \text{ kip}$$

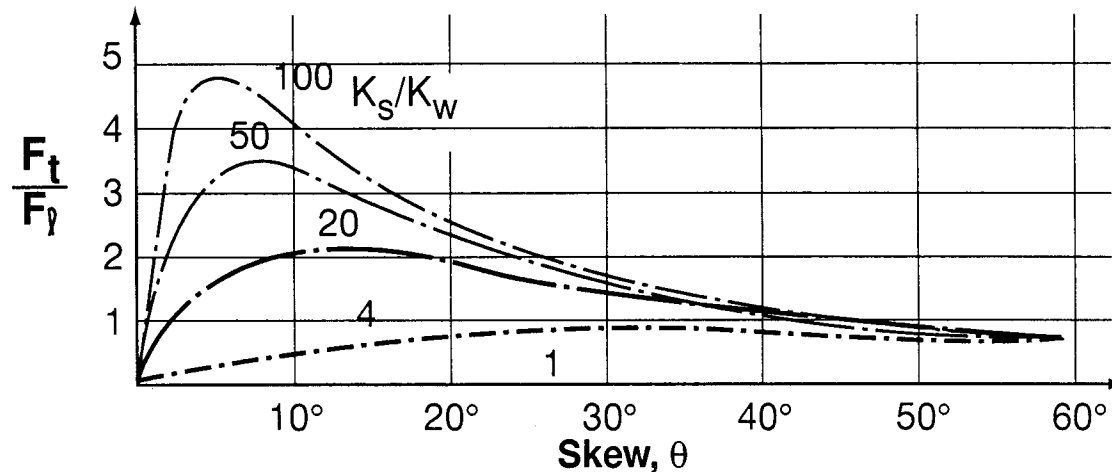
$$F_t = 1.8 (2265) = 4078 \text{ kip (vs. 377 from Frame Analysis)}$$

Example / Effects of Skew (6 of 6)

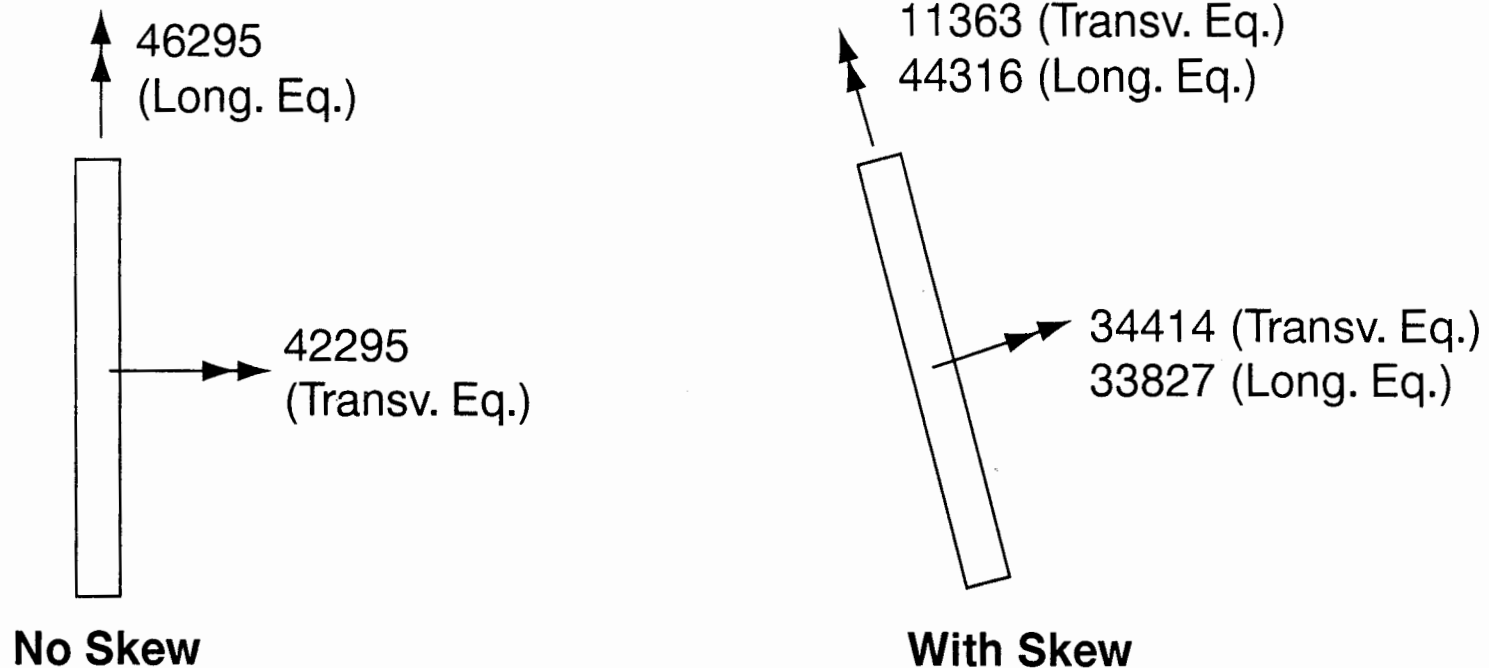


Relative Stiffnesses

- $K_S/K_W = 1$ Round Columns Fixed Top and Bottom
 $K_S/K_W = 4$ Columns Fixed Top in Strong Direction and
Free Top in Weak Direction
 $K_S/K_W = 20$ Rectangular Columns or Walls
 $K_S/K_W = 50+$ Walls, But Superstructure Not Rigid, Relative to
Stiff Walls, Need Frame Analysis

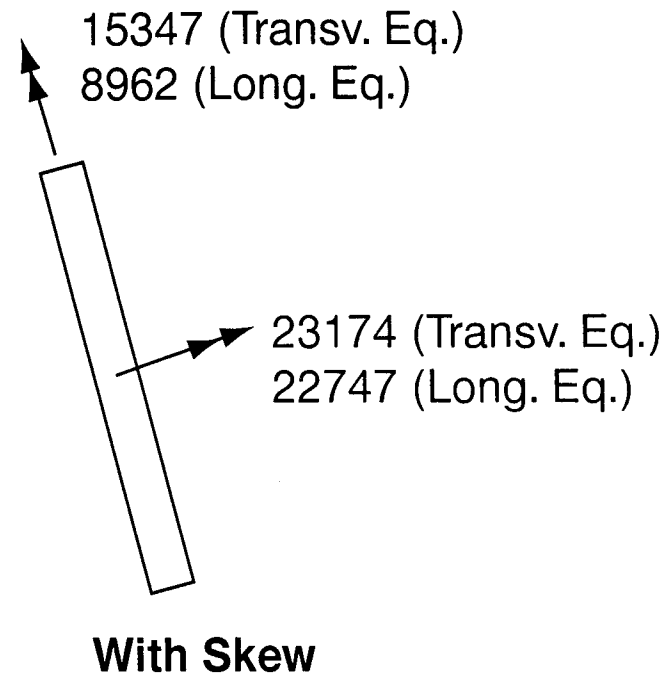
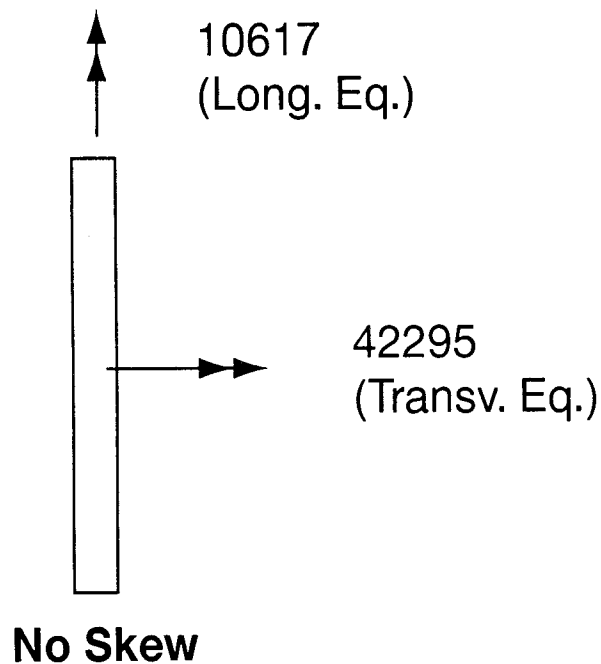


Example Pier No. 1 – Moments of Base of Wall



Moments in kip ft

Example Pier No. 2 – Moments of Base of Wall



Moments in kip ft

Example / Effects of Skew

Summary

- Coupling of Longitudinal and Transverse Forces Can Be Significant
- Coupling Very Sensitive to Relative Stiffness of Superstructure and Piers

Implications

- For Stiff Superstructure / Flexible Pier Bridges, Shear Block Forces Can Be Quite High
- Failure of Shear Blocks Will Induce Torsional Response (Worsens: Seating and Outer Column / Pier Response)

Minimizing Effects of Skew

- Elastomeric Bearing Pads, Which Can Have Omnidirectional Flexibility for Both Translation and Rotation, Can Help Minimize Effects of Skew
- For Example, See Design Example No. 2

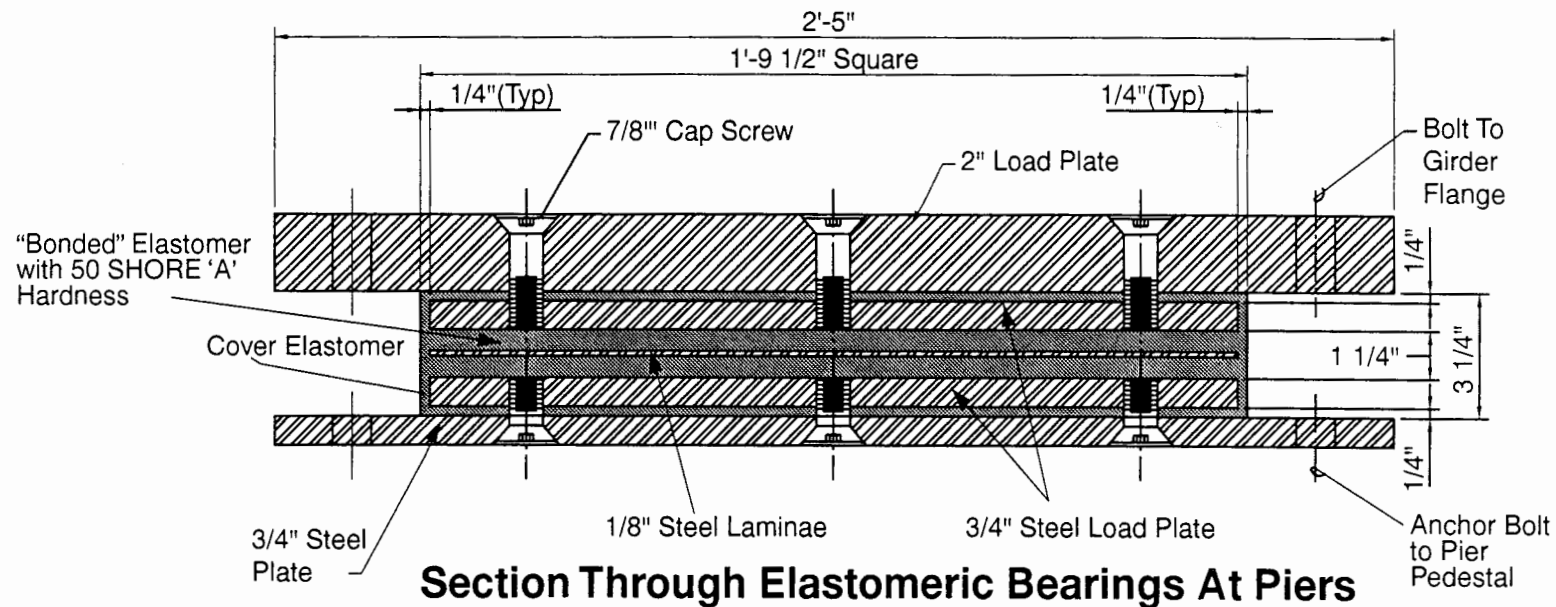
Session 4

Elastomeric Bearing and Modeling Design

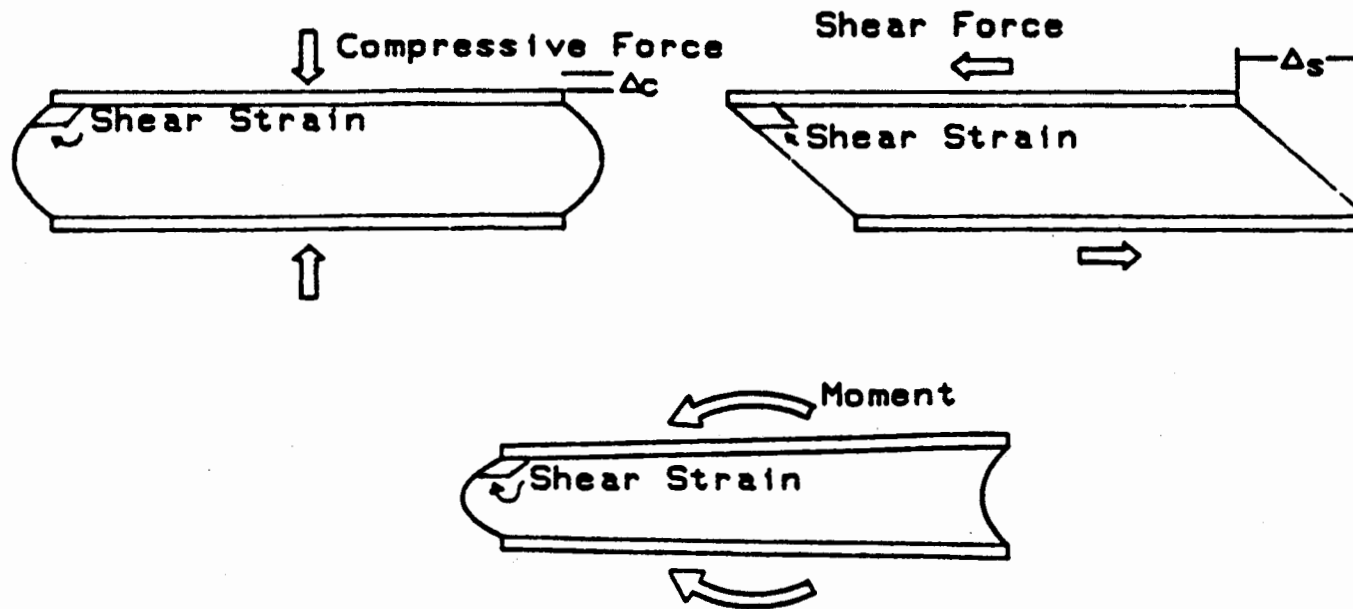
- **Concepts and Configuration**
- **Stiffness Calculations**
- **Limiting Strain**
- **Details**

(These Are Not Seismic Isolation Bearings)

Bearing Configuration



Conceptual Behavior



- All Loadings Induce Shear Strains

Roeder and Stanton (1990)

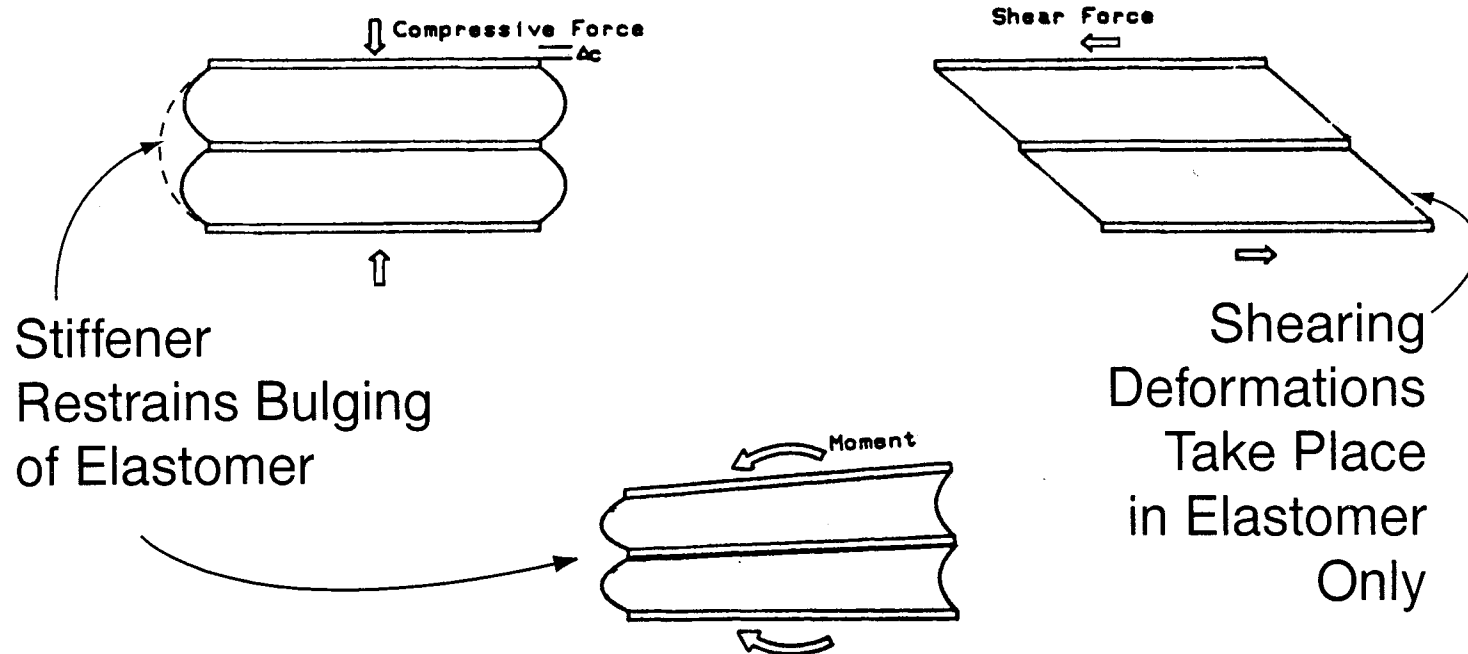
Session 4 Page 28 of 42

UMD-ITV

Seismic Bridge Design Applications

25 July 1996, NHI Course Code No. 13063

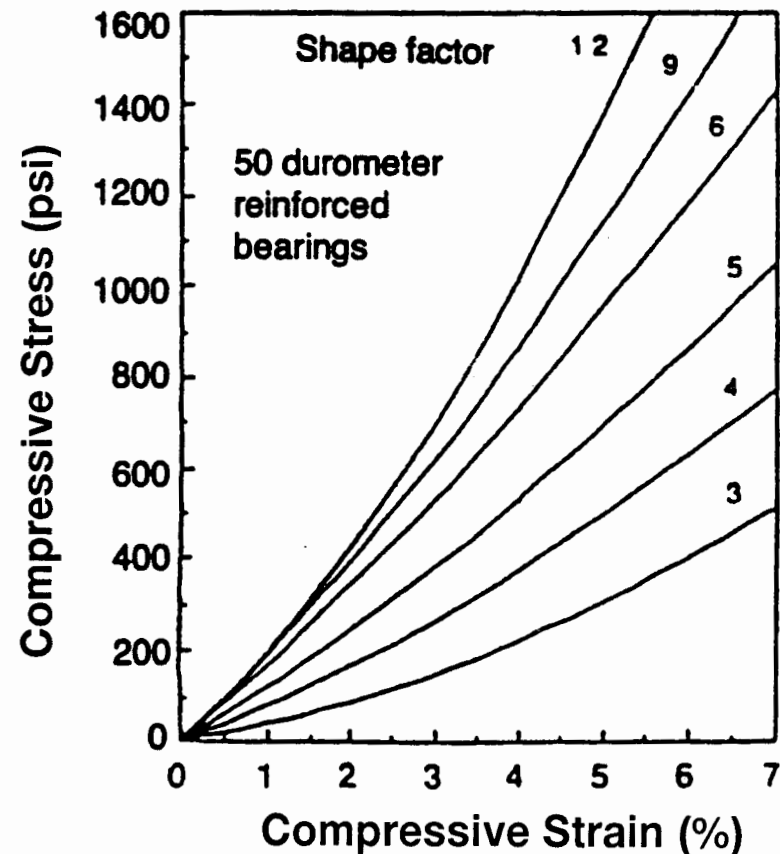
Behavior with Stiffeners



Properties of Elastomer

Hardness (Shore 'A')	Elastomer Shear* Modulus, G (psi)
50	95 - 130
60	130 - 200
70	200 - 300

* Coordinate with Supplier



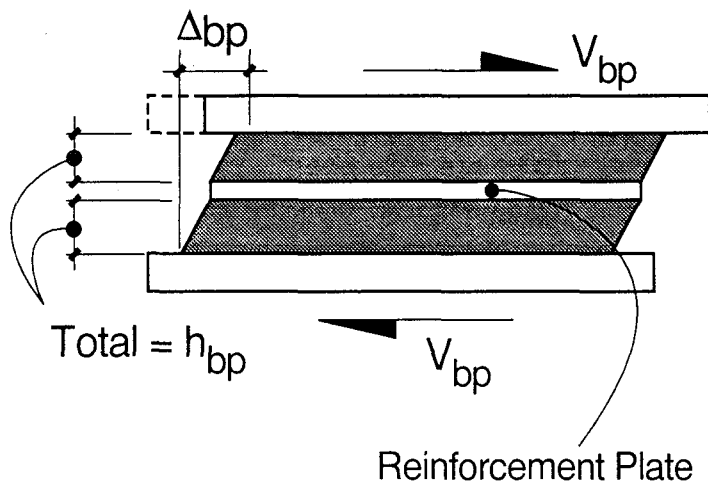
AASHTO (1995) (Division I)

Session 4 Page 30 of 42

UMD-ITV

Seismic Bridge Design Applications
25 July 1996, NHI Course Code No. 13063

Stiffness Calculation for Lateral Loads



$$K_h = \frac{V_{bp}}{\Delta_{bp}} = \frac{GA}{h_{bp}}$$

A = Area of Bonded Elastomer

h_{bp} = Total Height of Elastomer

(Do Not Include Reinforcement Plates)

Stiffness Calculation for Vertical Loads

- Shape of Bearing Affects Stiffness

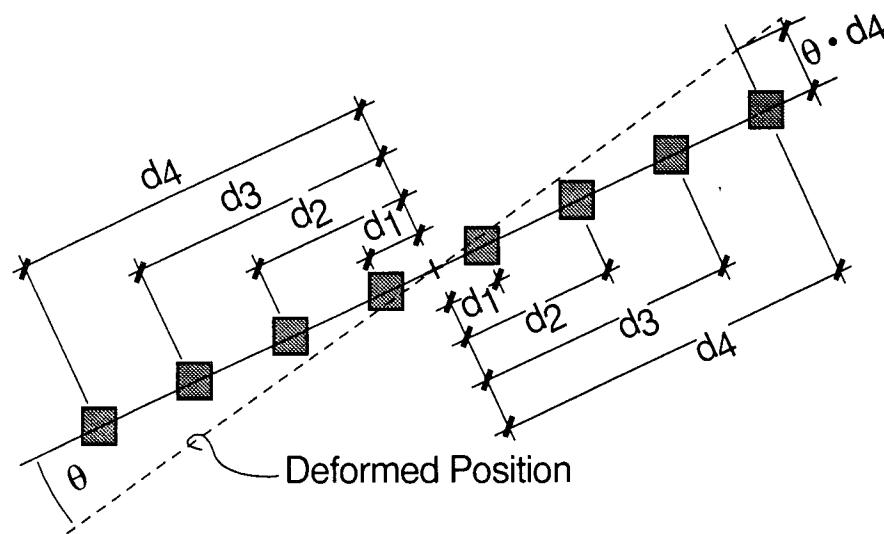
$$\text{Shape Factor, } S = \frac{\text{Plan Area}}{\text{Perimeter Area Free to Bulge}} = \frac{LW}{2h_{ri}(L + W)}$$

L = Length
W = Width

h_{ri} = Height of Layer

- Based on Compressive Stress and Shape Factor, Calculate Strain and Then Displacement
- Find Stiffness from Compression Force and Displacement

Rotational Stiffness of Group



Plan View
Bearing Pads on Skew Pier

$$K_{\text{rot}} = \frac{M}{\theta} = \sum_{i=1}^n K_{\text{brg}_i} d_i^2$$

K_{brg_i} = Individual Bearing
Translational
Stiffness

d_i = Distance from
Centroid to
Bearing i

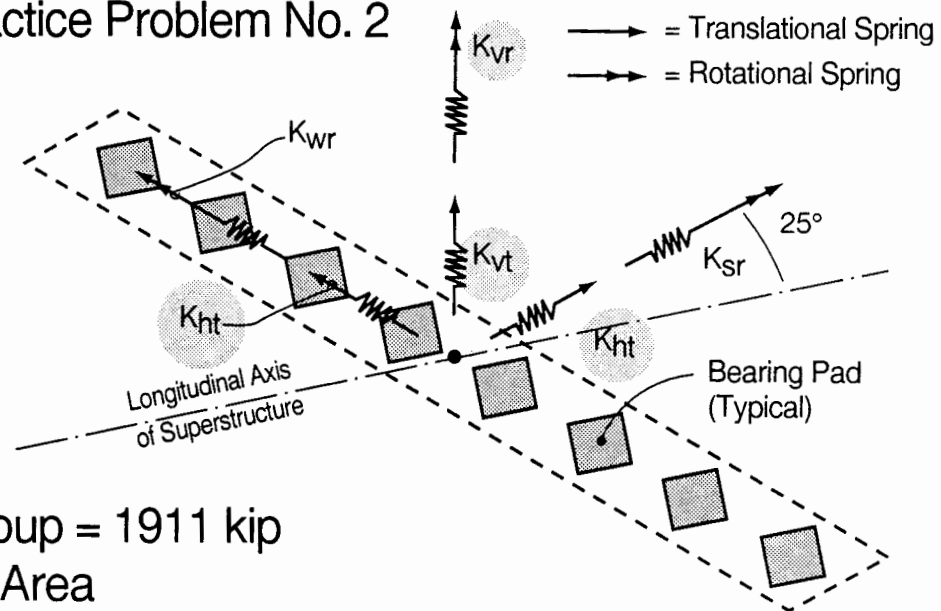
- Vertical Rotational
Stiffness Similar

Example / Elastomeric Bearing Stiffness (1 of 5)

- Consider Bearing Shown at Beginning of Section and 25° Skew Bridge of Practice Problem No. 2

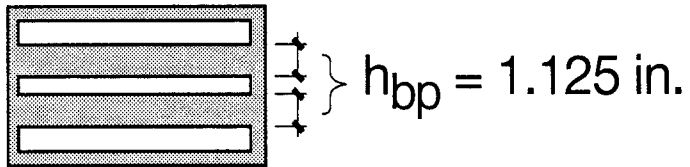
- Calculate Stiffness Shown in Shaded Bubbles

- Use $G = 115$ psi
Weight on Bearing Group = 1911 kip
21 in. x 21 in. Bonded Area



Configuration at Pier

Example / Elastomeric Bearing Stiffness (2 of 5)



- One Pad: $k_{ht} = \frac{GA_{bp}}{h_{bp}} = \frac{115(21)^2 12}{1.125 (1000)} = 541 \text{ kip/ft}$
- Eight Pads: $K_{ht} = 8 (541) = 4328 \text{ kip/ft}$
- Note that Stiffness Is the Same in All Directions

Example / Elastomeric Bearing Stiffness (3 of 5)

- Stress on Individual Bearings

$$\sigma = \frac{1911 (1000)}{8(21)^2} = 542 \text{ psi}$$

- Shape Factor

$$h_{ri} = \frac{1.125}{2} = 0.563 \text{ in.}$$

$$S = \frac{LW}{2h_{ri} (L+W)}$$

$$S = \frac{(21)^2}{2(0.563)(21+21)} = 9.3$$

- From AASHTO Plot (50 Durometer)

Compressive Strain $\epsilon_c = 0.025$ (Use Manufacturer's Data if Available)

Example / Elastomeric Bearing Stiffness (4 of 5)

- **One Pad**

$$k_{vt} = \frac{AE}{h_{bp}} \cdot \frac{A \sigma/\epsilon}{h_{bp}} = \frac{(21)^2 \left(\frac{0.542}{0.025} \right) (12)}{(1.125)}$$

$$k_{vt} = 102,000 \text{ kip/ft}$$

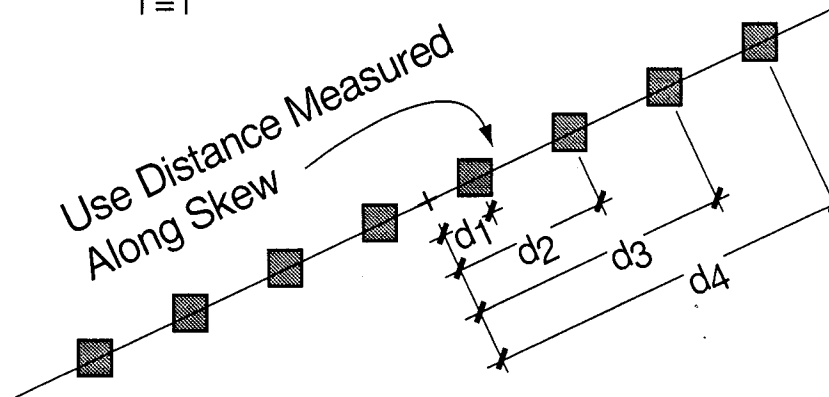
- **Eight Pads**

$$K_{vt} = 8(102,000) = 816,000 \text{ kip/ft}$$

Example / Rotational Stiffness About Vertical Axis (5 of 5)

$$K_{rv} = \sum_{i=1}^8 k_{ht} d_i^2 = 2 k_{ht} \sum_{i=1}^4 d_i^2$$

$$\begin{aligned} d_1 &= 4.5 \text{ ft} \\ d_2 &= 13.5 \text{ ft} \\ d_3 &= 22.5 \text{ ft} \\ d_4 &= 31.5 \text{ ft} \end{aligned}$$



Plan View

$$K_{rv} = 2(541)[4.5^2 + 13.5^2 + 22.5^2 + 31.5^2] = 1,841,000 \frac{\text{kip ft}}{\text{rad}}$$

Assessing Seismic Performance

- **Conventional (Division I)** → **Limit Service Shear Displacement**
(To 1/2 Elastomer Height)
- **Seismic Loadings** → **Assess Against Ultimate Resistance**
(Not Service Allowable)
- **Suggest AASHTO's Guide Specification for Seismic Isolation Design**
(Use Article 14.6, Seismic Load Combinations, Even Though We Are Considering Only Conventional Elastomeric Bearings in This Section)

Assessing Seismic Performance of Conventional Elastomeric Bearings

Limit Strains to: $0.75 \epsilon_U > \epsilon_{SC} + \epsilon_{eq} + \epsilon_{sr}$ AASHTO Seismic Isolation Guide Specification / §14.6

ϵ_U = Minimum Elongation-At-Break of Elastomer
(From AASHTO or Preferably Supplier)

Example, Table 18.2.3.1 Division II
50 Durometer Neoprene

$$\epsilon_U = 400\%$$

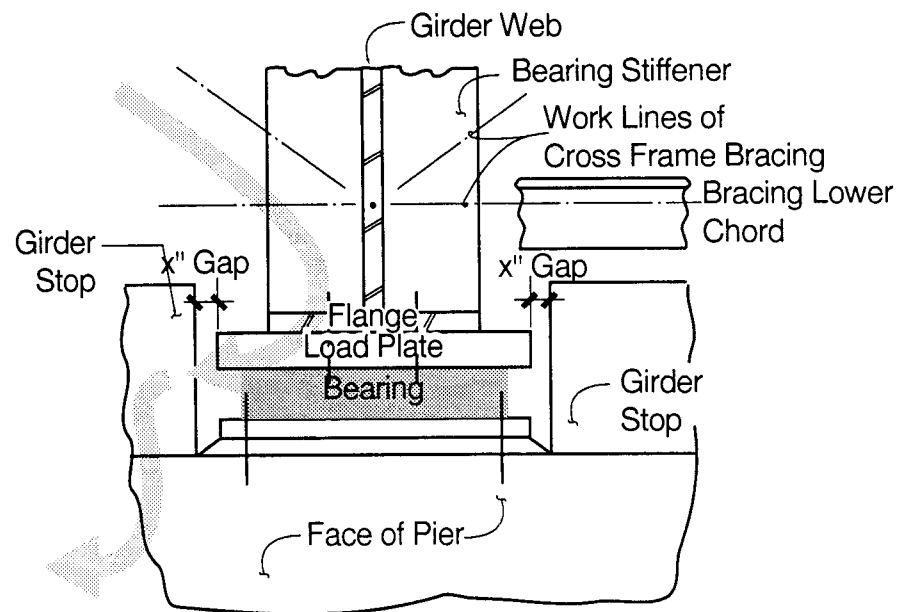
ϵ_{SC} = Shear Strain Due to Compression = $65 S \epsilon_C$ ← Compressive Strain

ϵ_{eq} = Shear Strain Due to Earthquake = $\Delta_{eq} / h_{elastomer}$

ϵ_{sr} = Shear Strain Due to Rotation = $\frac{B^2 \theta}{2h_{ri} \cdot h_{bp}}$ ← Load Direction Dimension

Fail-Safe Issues

- Consider an Additional Load Path in Case of Bearing Failure
- Engage Alternate Path After Bearing Deformation Occurs

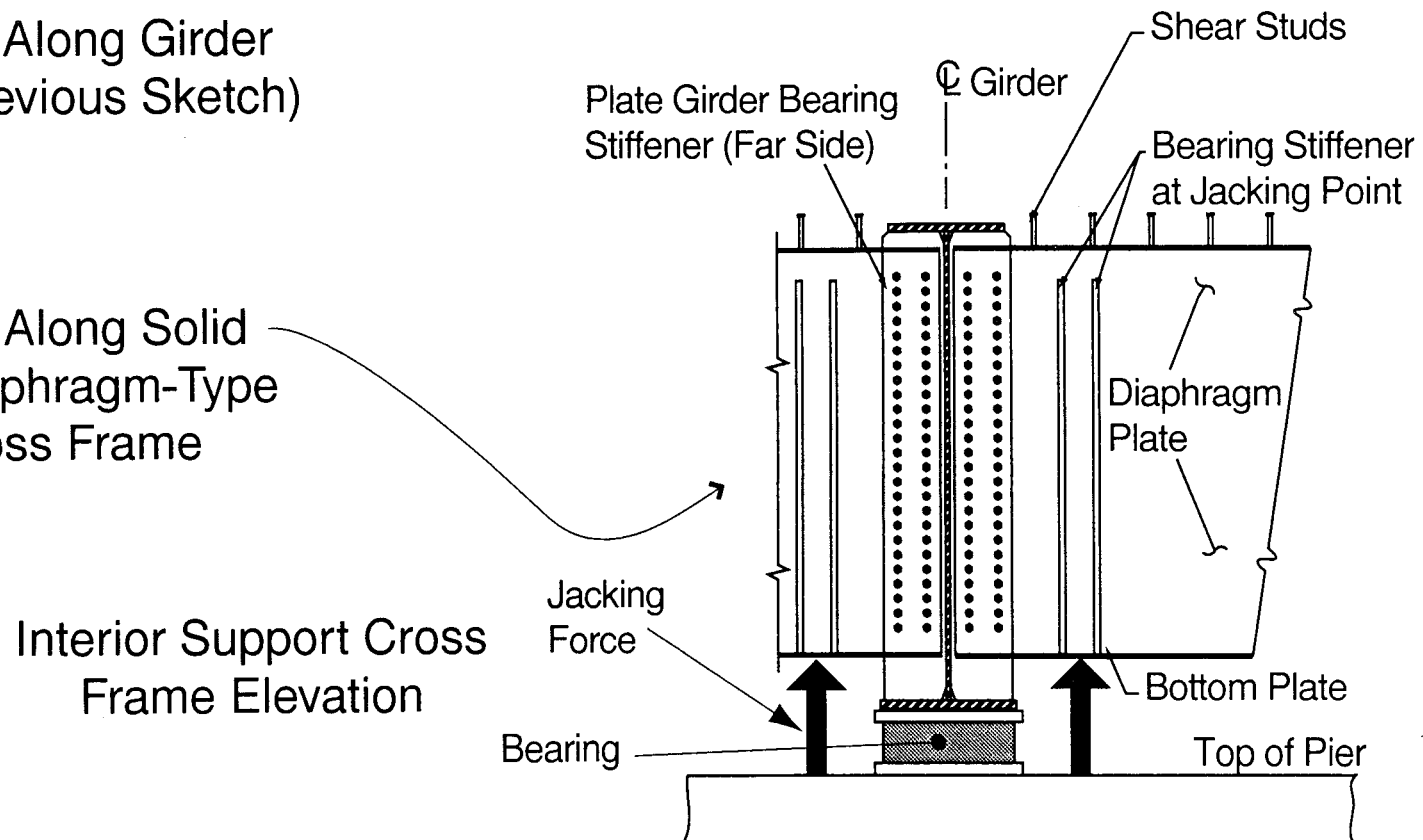


Consider Method of Bearing Replacement

- Lift Along Girder
(Previous Sketch)

or

- Lift Along Solid
Diaphragm-Type
Cross Frame



Session 5

Curved Box Girder Bridge Example

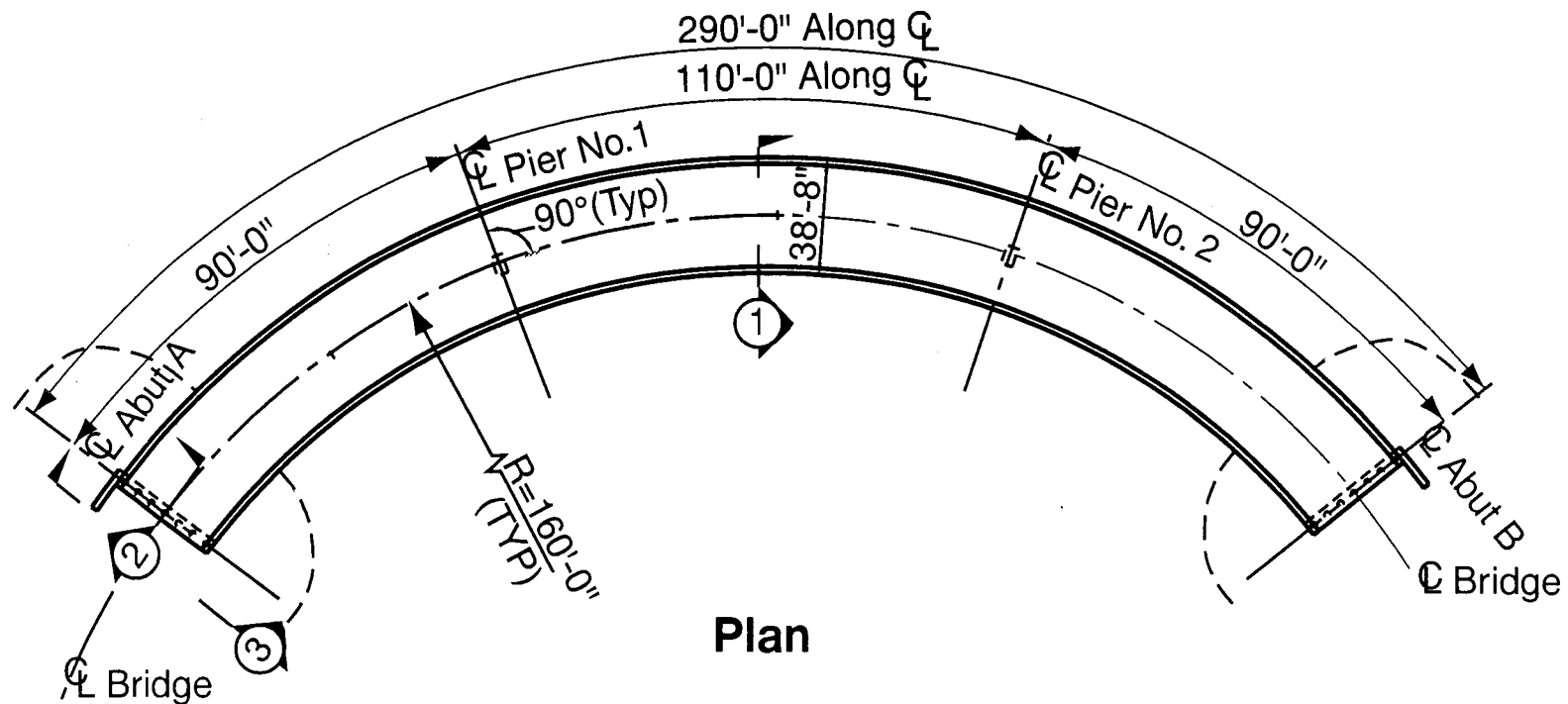
Session 5

- **Curved Structure Issues**
- **Piles**

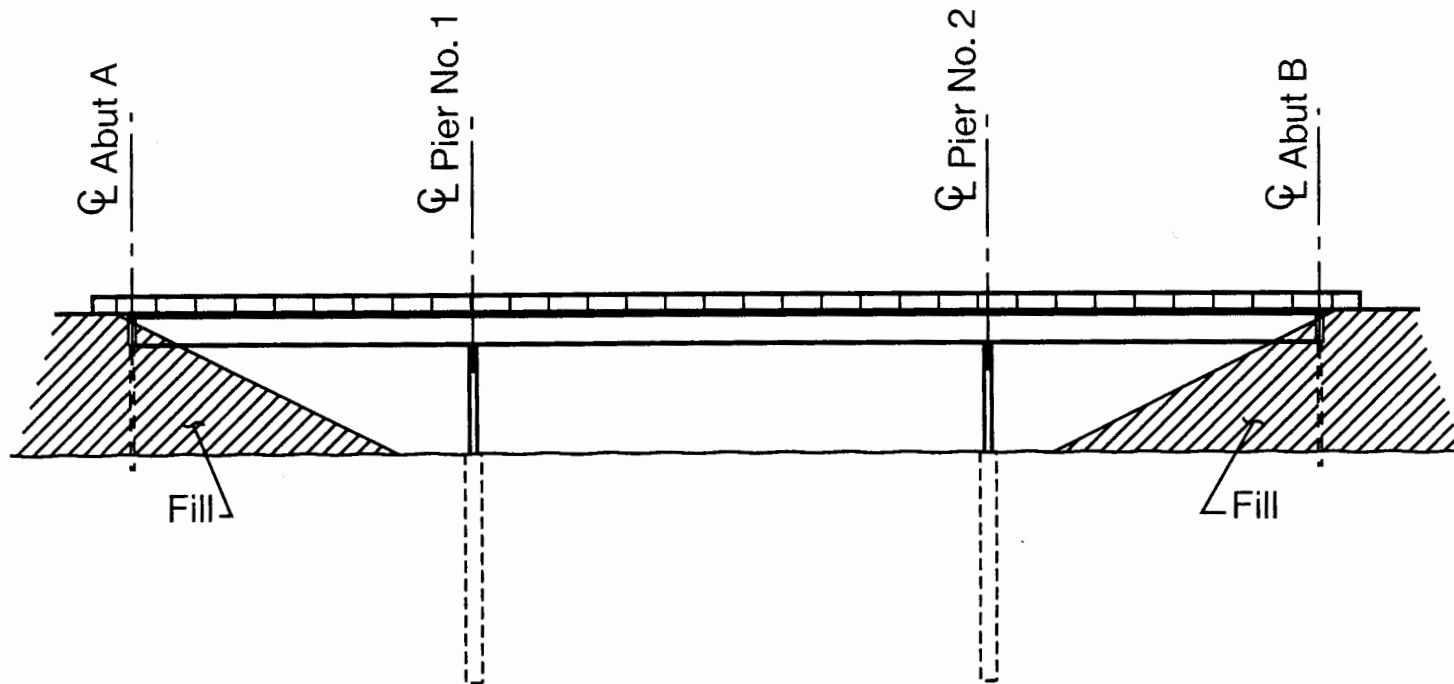
Session 6

- **Drilled Shafts**

Concrete Curved Box Girder Bridge / Plan

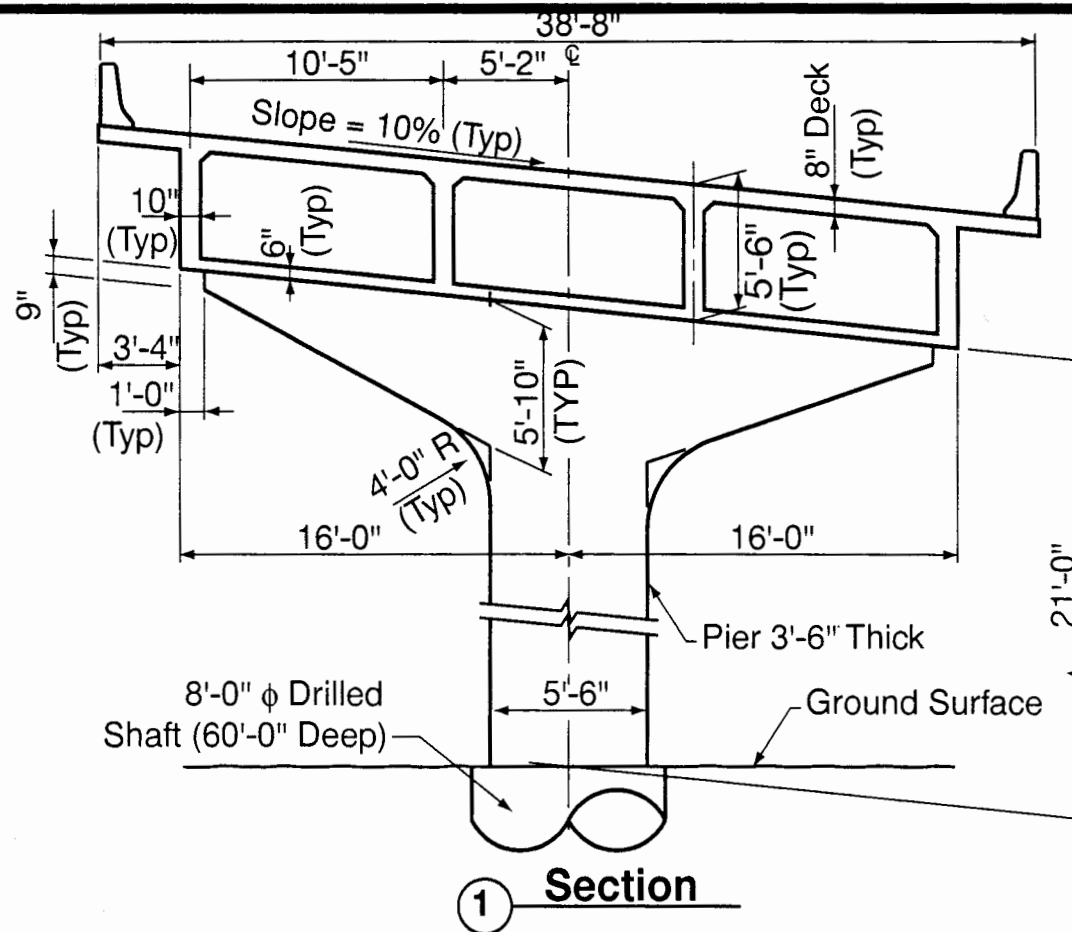


Concrete Curved Box Girder Bridge / Elevation

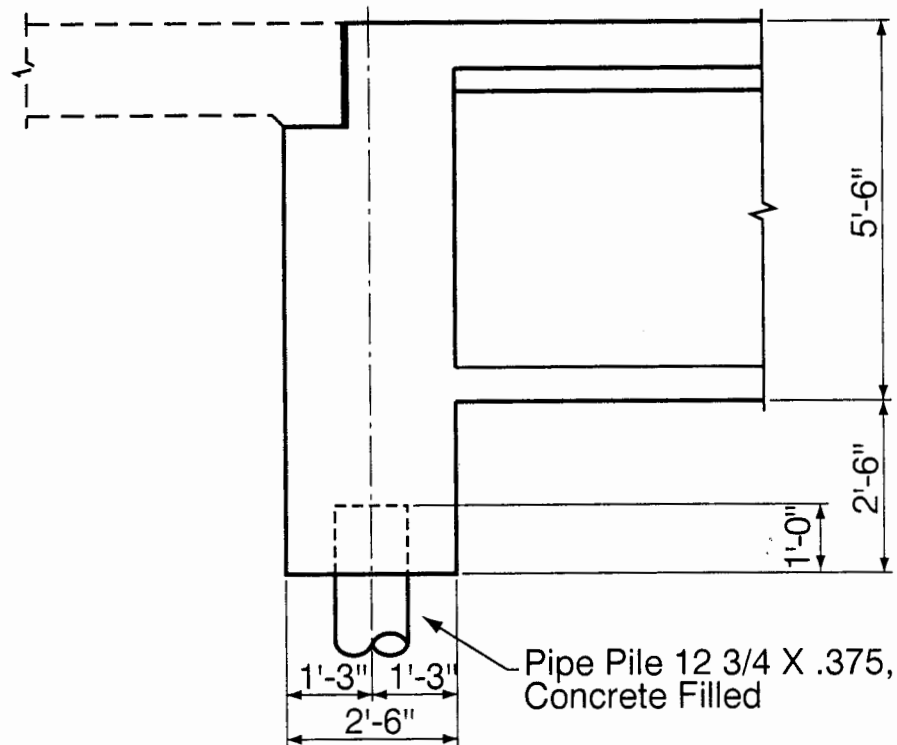


Developed Elevation

Concrete Curved Box Girder Bridge /Pier

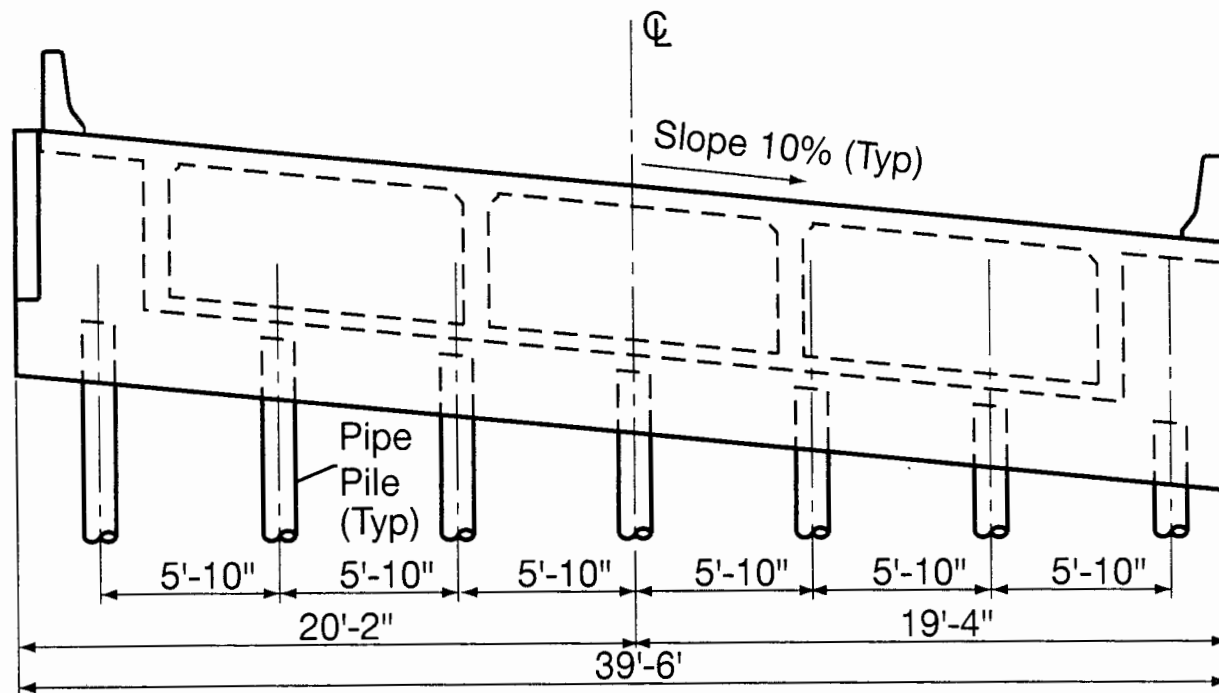


Concrete Curved Box Girder Bridge / Abutment



② Section

Concrete Curved Box Girder Bridge / Abutment



③ Elevation

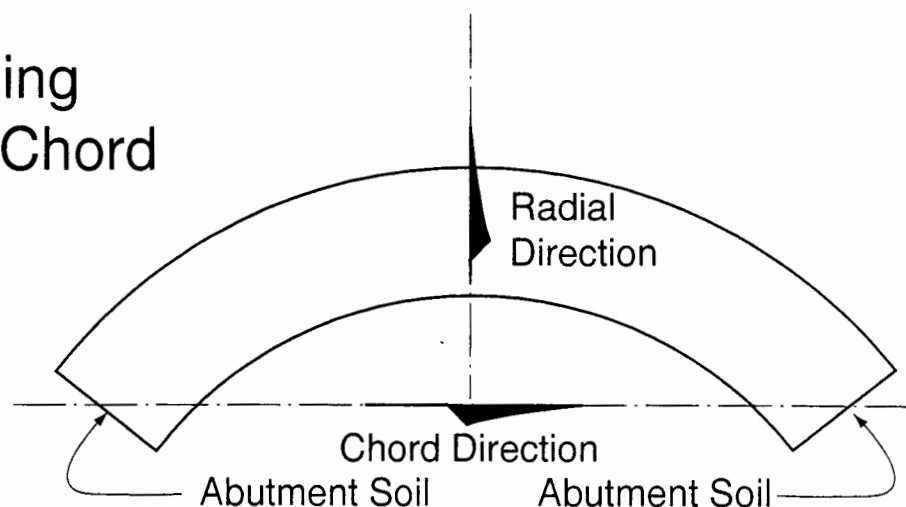
Session 5

Curved Structure Issues

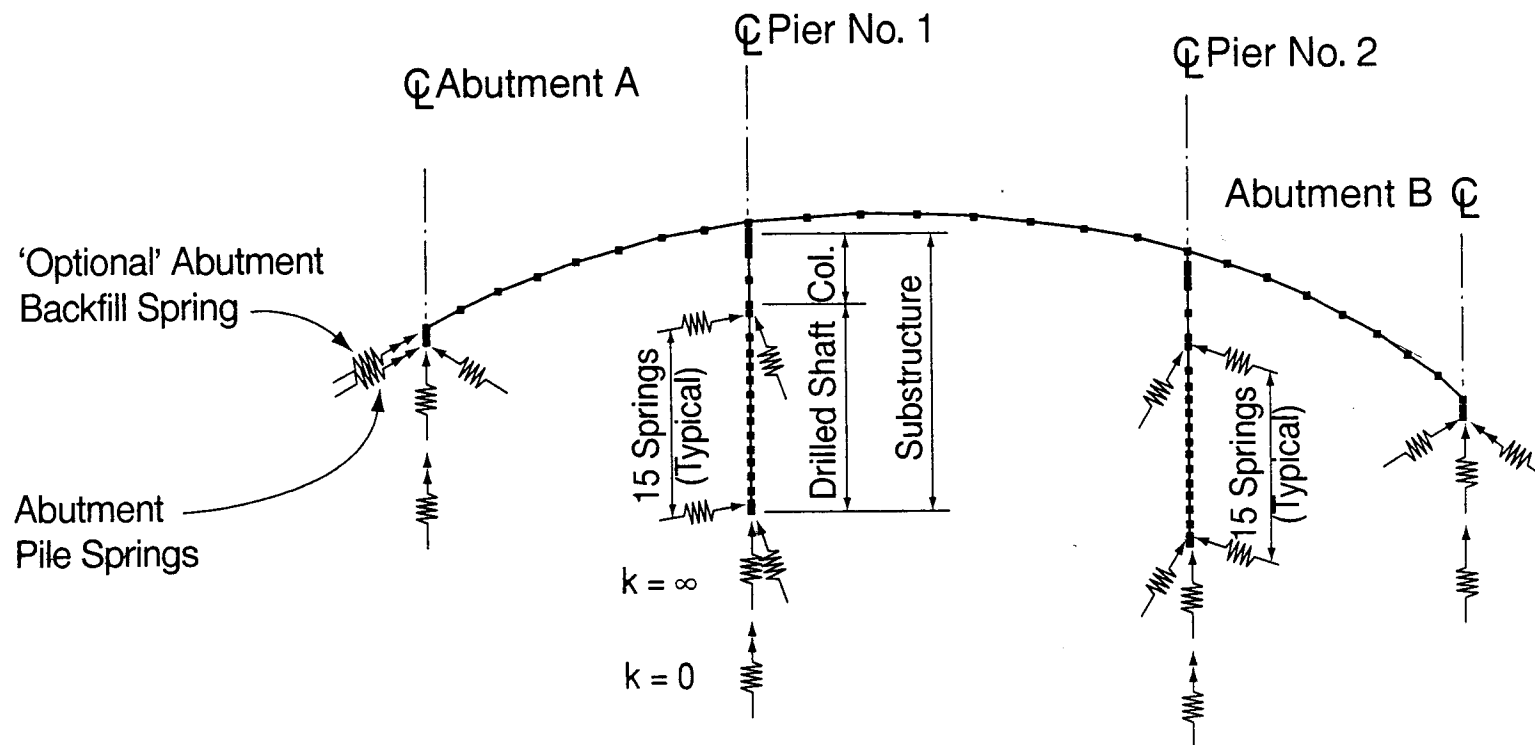
- **Loading Directions**
- **Conceptual Behavior**
- **Bounding Response**

AASHTO Loading Directions

- If Modal Analysis Is Used (Required if 'Not Regular')
 1. Earthquake Loading Along Chord
 2. Earthquake Loading Perpendicular to Chord
- Suggest the Same Loading Directions for Other Analysis Methods

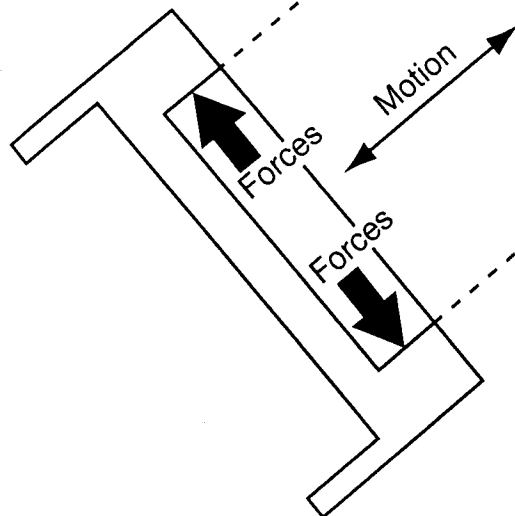


Seismic Analysis Model / Example Bridge



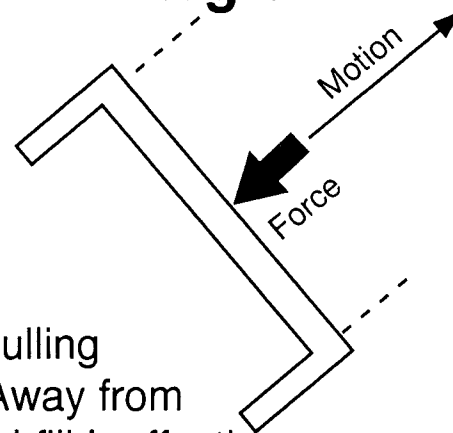
Effects of Abutment Restraint

Seat-Type with Shear Blocks



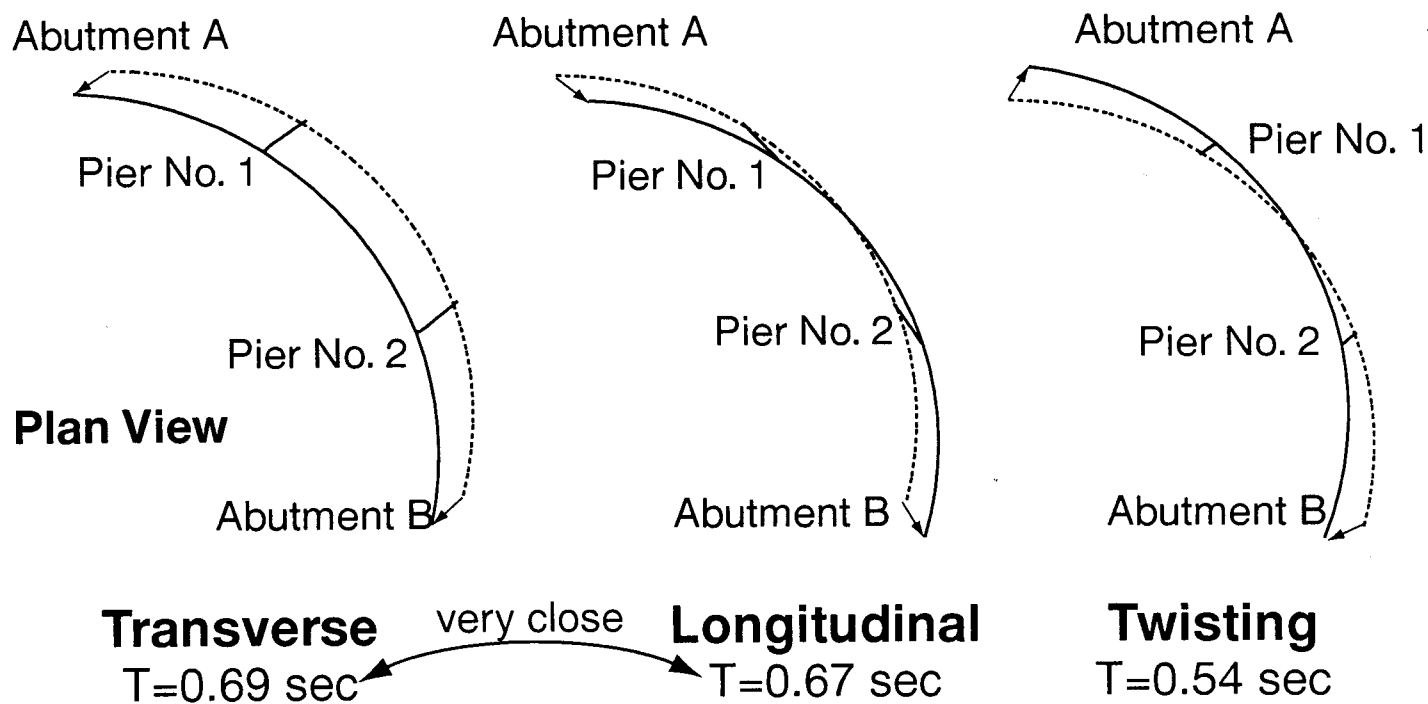
- Movement Will Heavily Load Shear Blocks

Integral

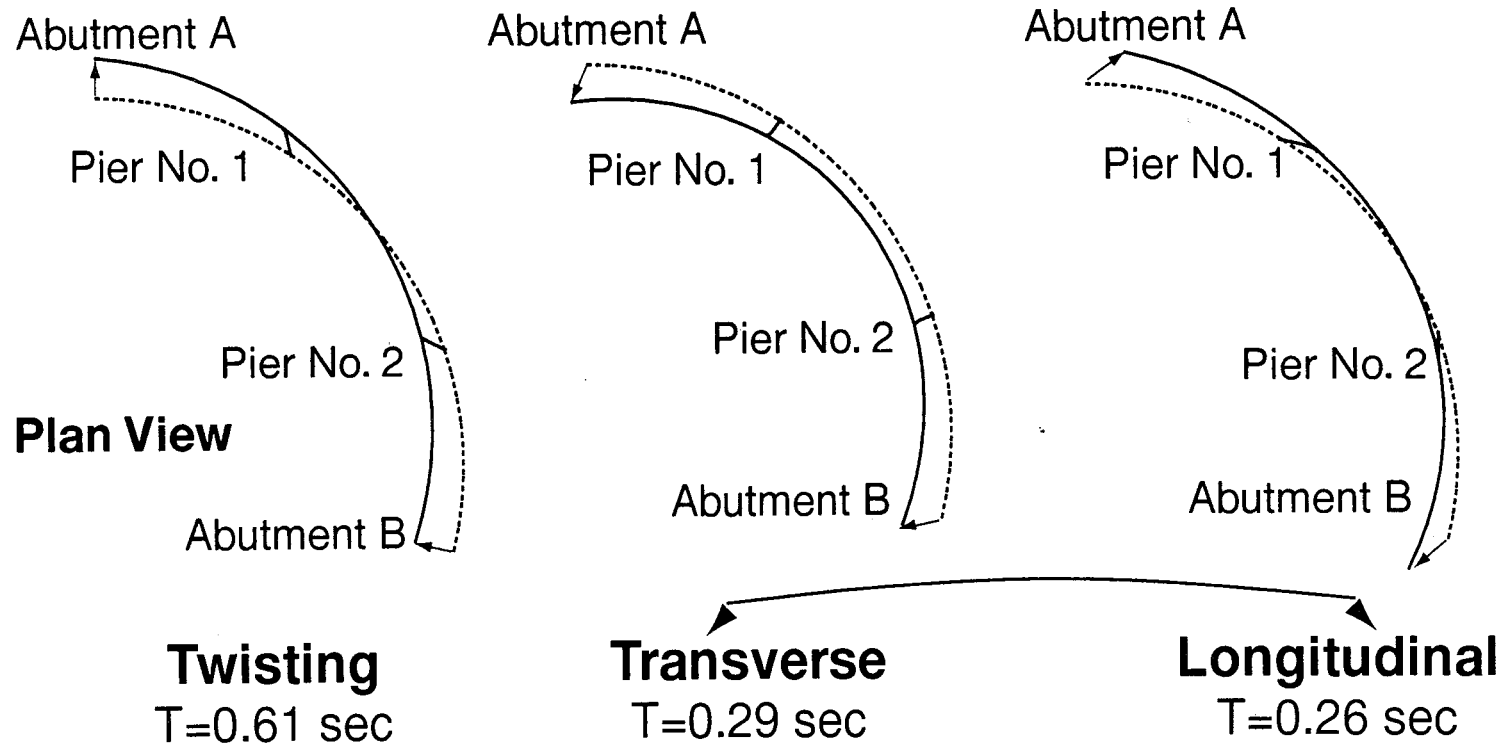


- Movement Pulling Diaphragm Away from Soil ~ Backfill Ineffective
- Movement Toward Soil Backfill Effective
- Use Bounding Analyses

Modal Behavior / No Backfill Considered



Modal Behavior / Including Backfill



Effects of Curve for Example Bridge

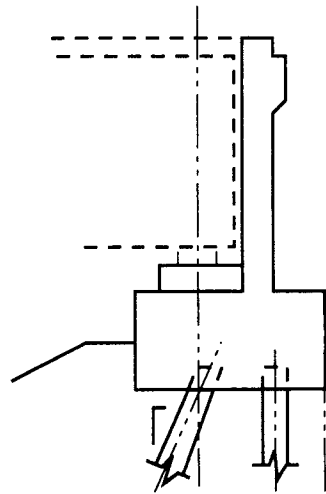
- Both Abutment Backfills Are Effective or Not Effective at the Same Time (Do Not Put $1/2 K$ to Each)
- No Backfill Case Controls
 - Piers / Drilled Shafts
 - Piles
- Backfill Included Controls
 - End Diaphragm
 - Backfill Soil
- Torsional Stiffness of Superstructure Is More Influential in Forces Developed

Session 5

Piles

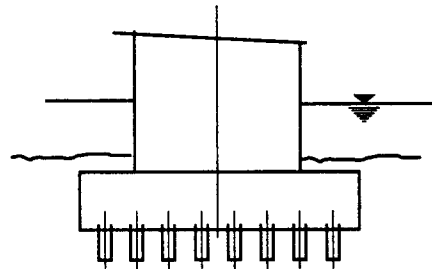
- **Configuration and Behavior**
- **Including Flexibility in Analysis**
- **Coupling Effects**
- **Nonlinear Effects**
- **Multiple Pile Groups/Axial Stiffness**
- **Design and Detailing**

Typical Configurations

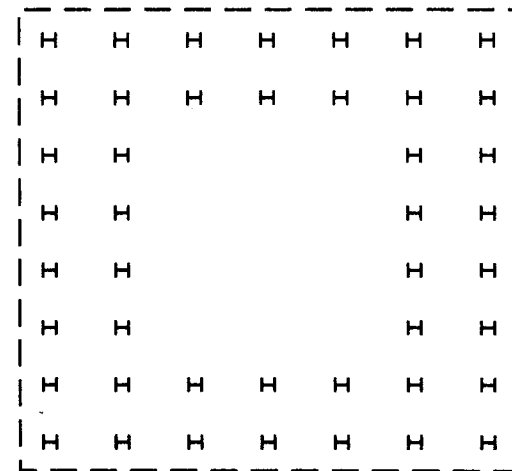


Piles Either Steel,
Concrete, or Timber

Abutment

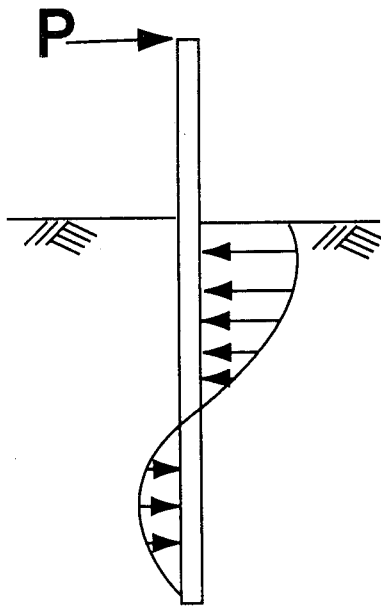


Pier Section

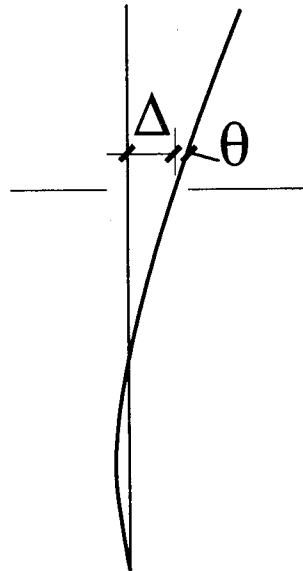


Pier Plan

Behavior Under Lateral Loading

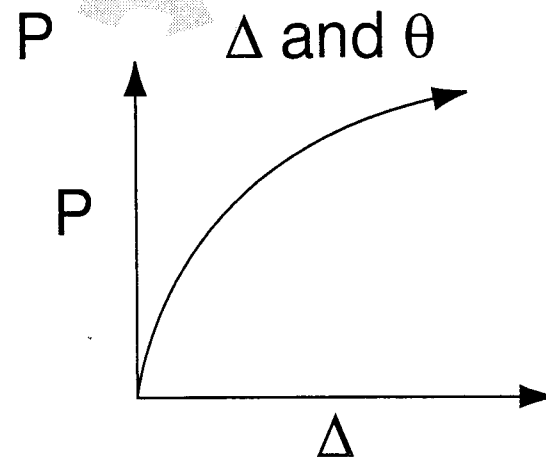


Forces on Pile

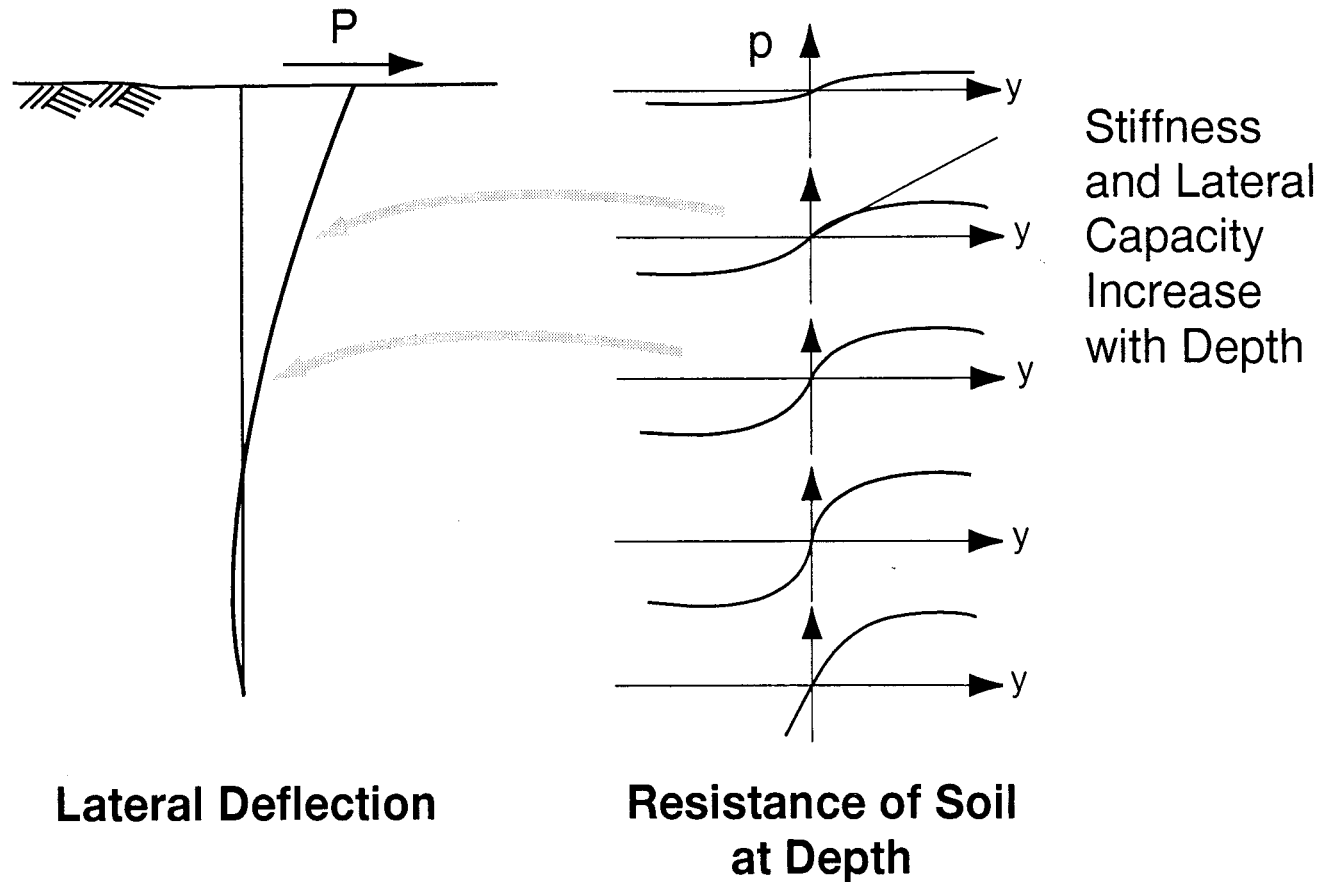


Pile Lateral Deflection

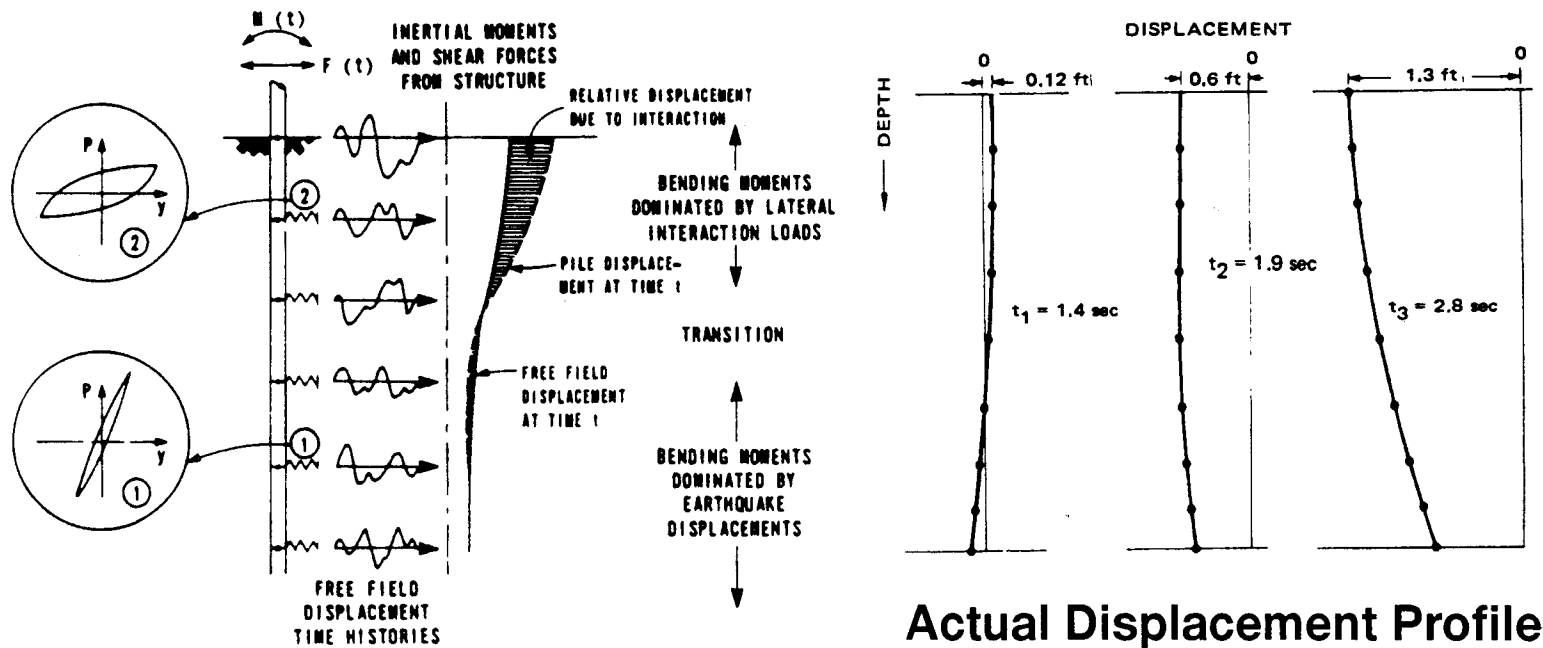
- Δ and θ Are “Coupled”



'p-y' Relations (Curves) for Piles

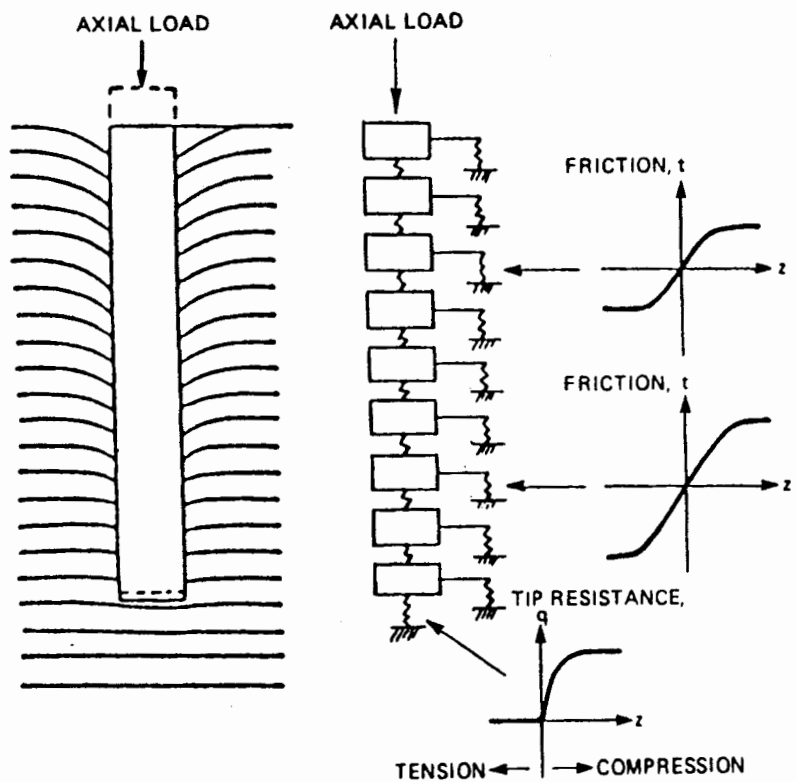


Consideration of the Free-Field Ground Motion

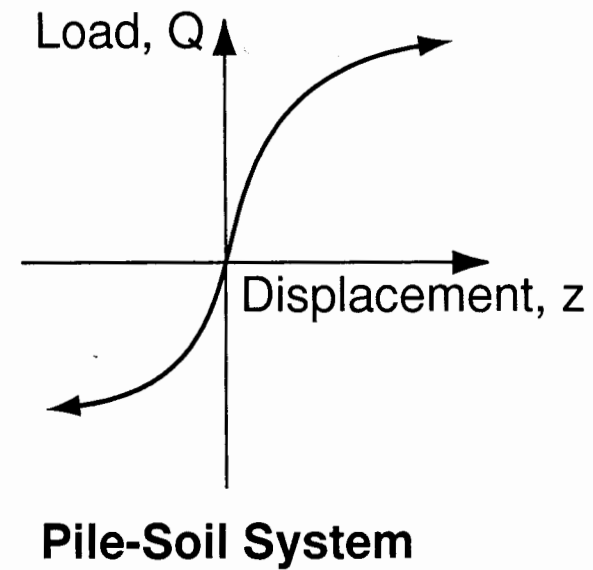


AASHTO (1995)

Behavior Under Vertical Loading



FHWA (1987)

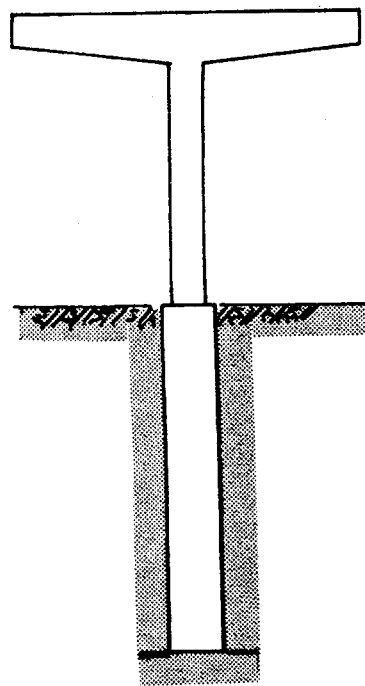


Session 5

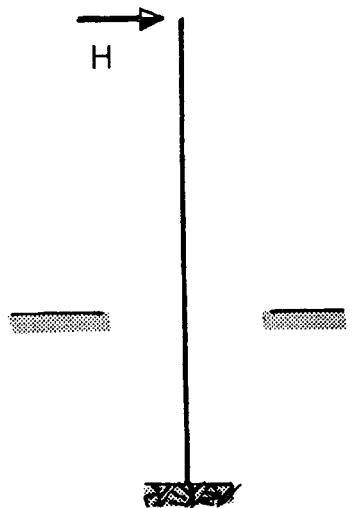
Piles

- Configuration and Behavior
- **Including Flexibility in Analysis**
- Coupling Effects
- Nonlinear Effects
- Multiple Pile Groups / Axial Stiffness
- Design and Detailing

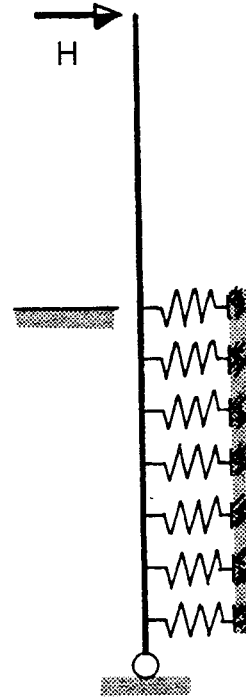
Analytical Models of Pile Foundations



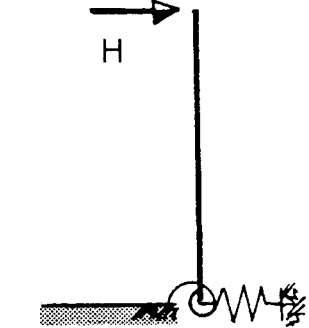
Bridge Pile System



**Equivalent
Cantilever Model**

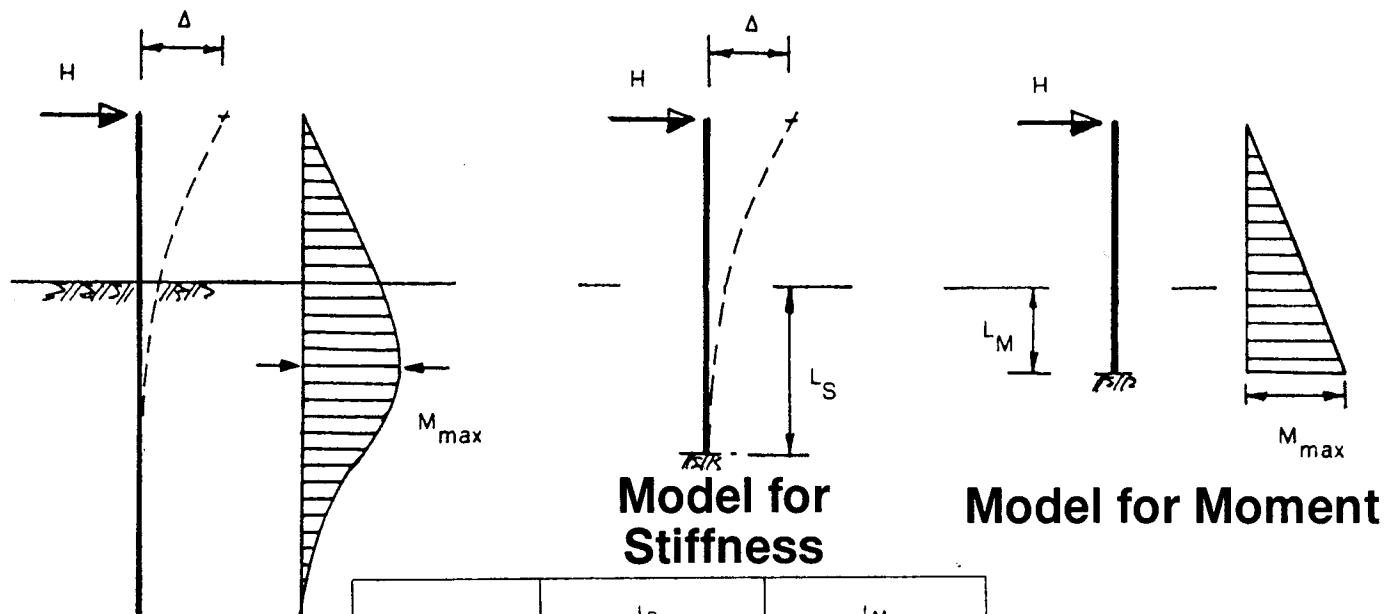


**Equivalent
Soil Spring Model**



**Equivalent Base
Spring Model**

Equivalent Cantilever Method



Actual Pile

Model for Stiffness

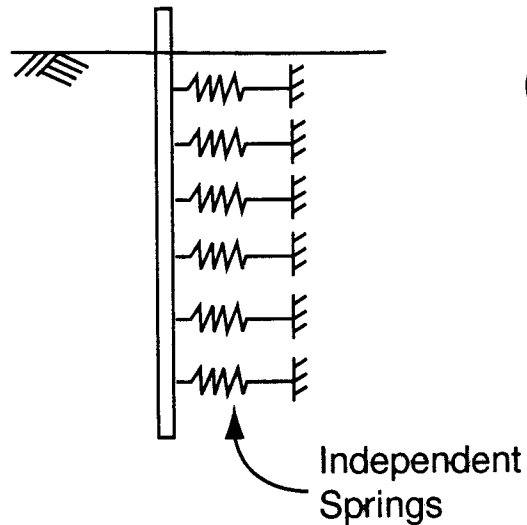
Model for Moment

	L_S	L_M
Cohesive Soil Constant K_h	$1.4 \sqrt[4]{\frac{EI}{K_h}}$	$0.44 \sqrt[4]{\frac{EI}{K_h}}$
Cohesionless Soil Constant n_h	$1.8 \sqrt[5]{\frac{EI}{n_h}}$	$0.78 \sqrt[5]{\frac{EI}{n_h}}$

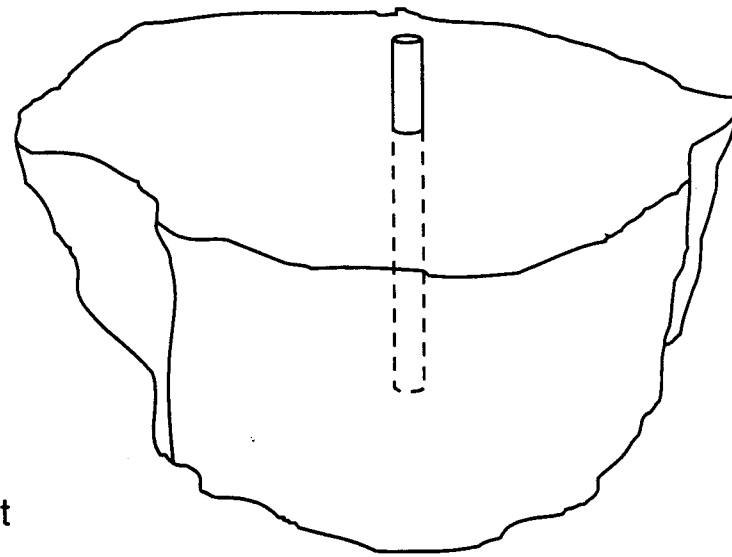
FHWA (1987)

Determining Piles-Soil Stiffness

Most
Common



Subgrade Reaction Method

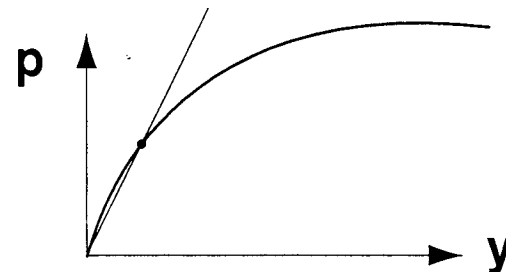


**Elastic Continuum
(Half-Space)**

Subgrade-Reaction Method (Linear Elastic)

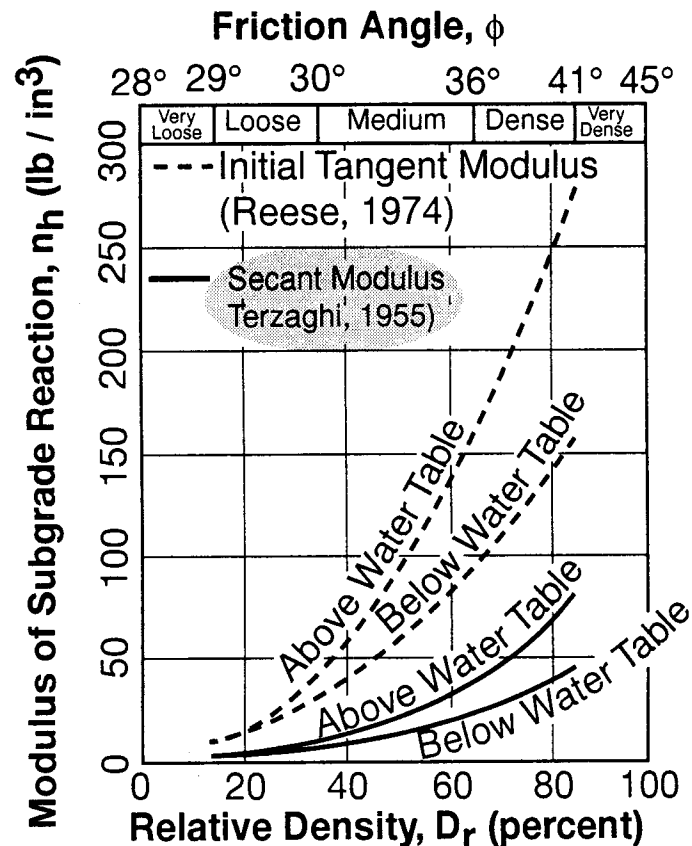
- **Basis** (Assumptions)

- Known Modulus of Subgrade Reaction, n_h
- Modulus, Function of Depth and Lateral Stiffness Is Independent of the Pile Diameter (Cohesionless and Cohesive)
- Stiffness Typically Is Secant and Applies for About 1/3 of Ultimate Capacity



References: FHWA/RD-86/102 (1986)
NAVFAC DM7.02 (1986)
Poulos and Davis (1980)

Modulus of Subgrade Reaction / Cohesionless



- **Modulus at Depth z:**

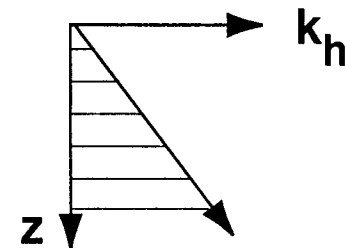
$$k_h = n_h \frac{z}{D} \quad (\text{kip/ft}^3)$$

D = Diameter

- **Spring Stiffness:**

$$K_h = k_h DH$$

H = Tributary Height



FHWA (1986)

Modulus of Subgrade Reaction / Cohesive

- Modulus at Depth

$$k_h = k_0 + k_1 z$$

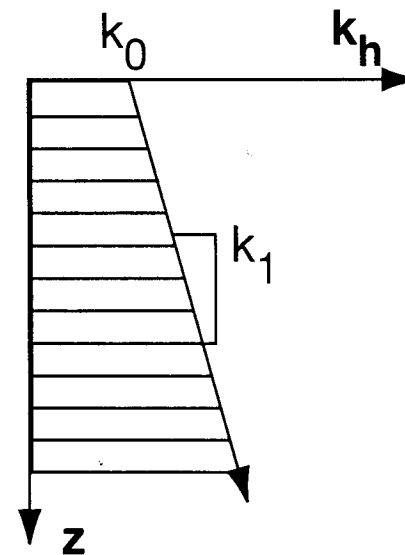
$$k_0 = 0.6 c / \epsilon_c$$

$$k_1 = \frac{0.2}{\epsilon_c} \left(\gamma + \frac{0.25 c}{D} \right)$$

c = Undrained Shear Strength

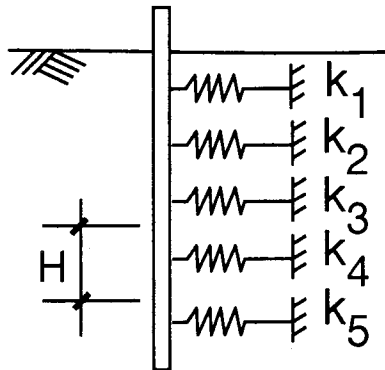
γ = Effective Unit Weight

ϵ_c = Strain Amplitude at 1/2
Peak Deviatoric Stress



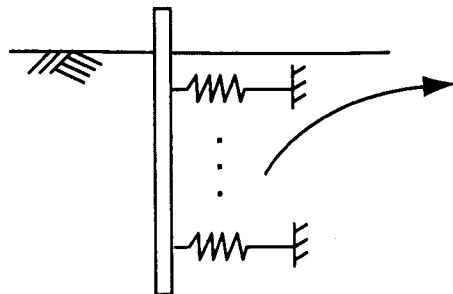
FHWA (1986)

Including Stiffness



DIRECT

- Use Equations for Subgrade Method and Calculate K_1, \dots etc.
- Include K 's in Model Along with Pile



INDIRECT

- Use Existing (Linear Elastic) Solutions that Give Spring Stiffness at Ground Surface

Example of 'Indirect' Method

- **Use Influence Charts (NAVFAC DM7.02, for Example)**

1. Find n_h for Soil Type

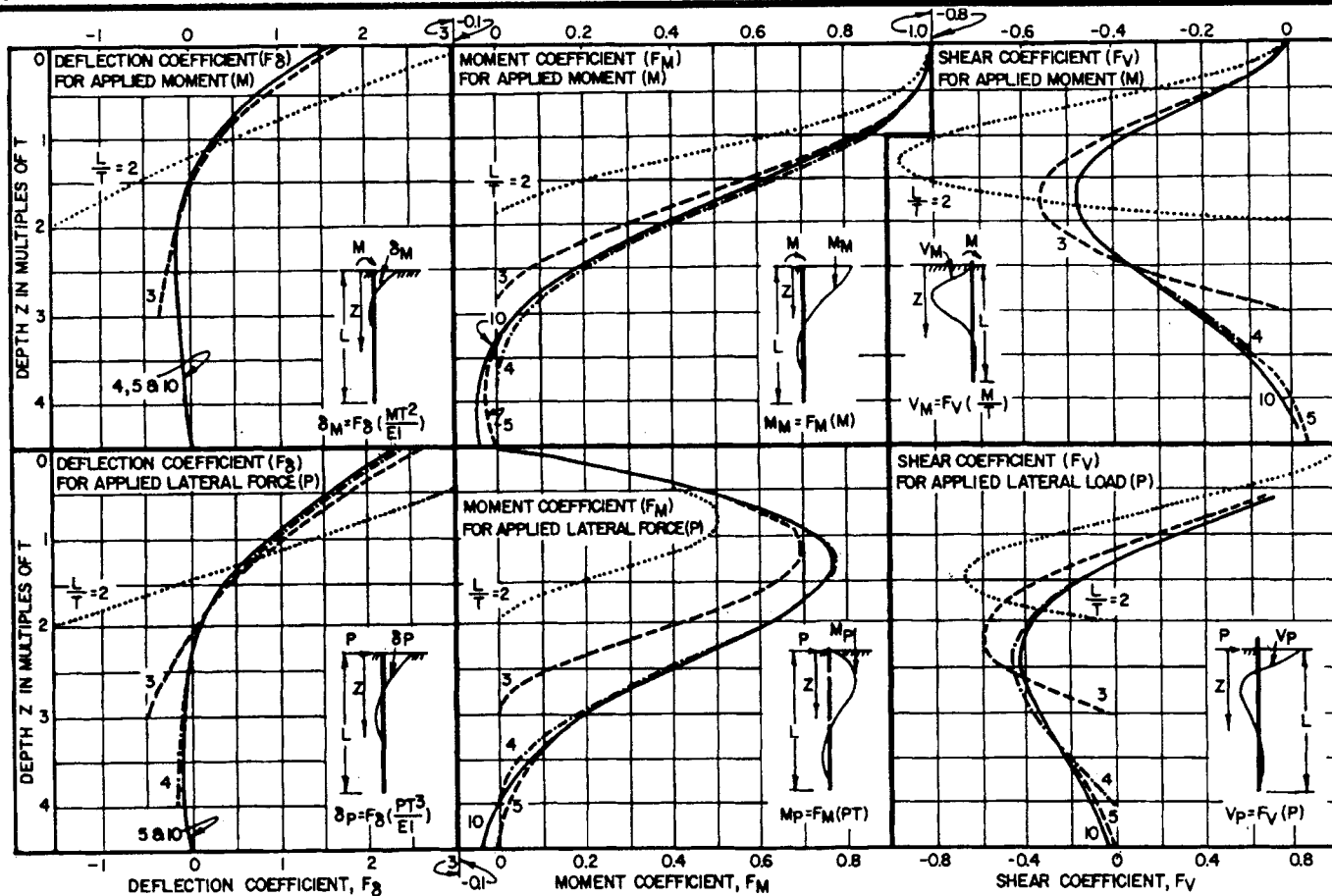
2. Determine Characteristic Length, $T = \left(\frac{EI}{n_h} \right)^{1/5}$

3. Calculate L / T (L =Pile Length)

4. Use Charts to Calculate Stiffness, Moment, and
Shear — Free or Fixed Head Piles

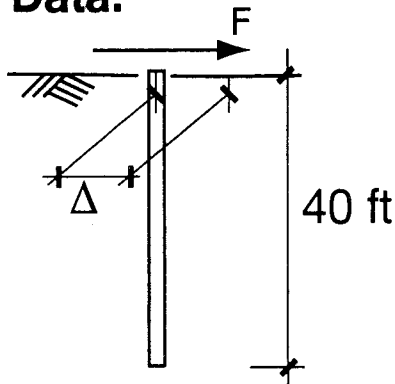
(Use Superposition — Treat Forces and Moments
Applied to Pile Separately)

NAVFAC DM7.02 Coefficients / Free Head



Example / 'DM7' Method (1 of 3)

Data:



12 in. Concrete-Filled Pipe Pile / Free Head /

$I = 406 \text{ in}^4$ (Pipe + Concrete - Upper Bound)

$E_s = 29000 \text{ ksi}$

Soil (Cohesionless) $\phi \approx 33^\circ$ ($n_h = 23 \text{ pci}$)

Required: Lateral Translational Stiffness

$$\text{Characteristic Length, } T = \left(\frac{EI}{n_h} \right)^{1/5} = \left(\frac{29000(406)}{0.023} \right)^{1/5} = 55.1 \text{ in.}$$

Example / 'DM7' Method (2 of 3)

$$\frac{L}{T} = \frac{40(12)}{55.1} = 8.7$$

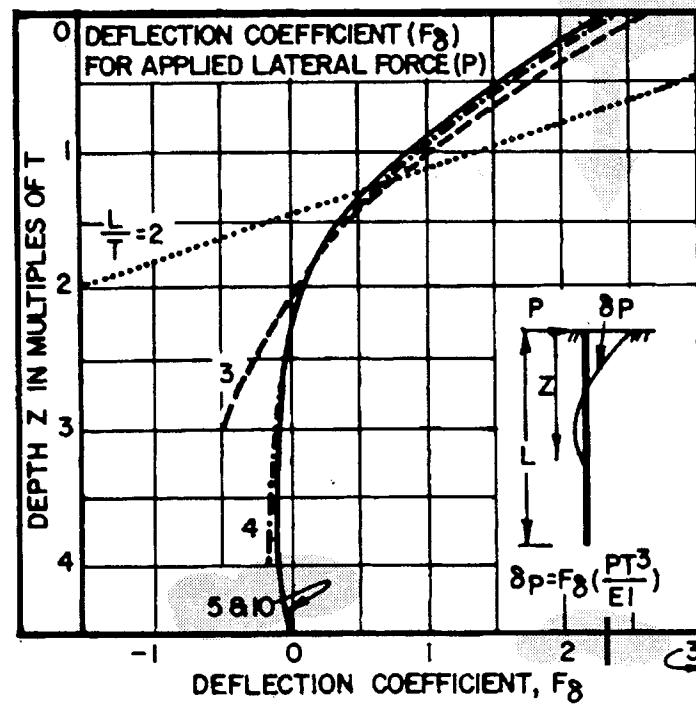
For Stiffness, Use:

$$z=0 \text{ ft} \rightarrow F_{\delta} = 2.3$$

$$K = \frac{P}{\delta_P} = \frac{EI}{F_{\delta} T^3}$$

$$K = \frac{(29000) 406 (12)}{2.3 (55.1)^3}$$

$$K = 367 \text{ kip / ft}$$



Example / Check Using 'Equivalent Cantilever' (3 of 3)

• **Cantilever Length**

$$L_s = 1.8 \sqrt[5]{\frac{EI}{n_h}} = 1.8 \sqrt[5]{\frac{29000(406)}{0.023}}$$

$$L_s = 99.3 \text{ in.}$$

• **Stiffness**

$$K = \frac{3EI}{L_s^3} = \frac{3(29000)406(12)}{(99.3)^3} = 433 \text{ kip / ft}$$

vs. 367 kip / ft

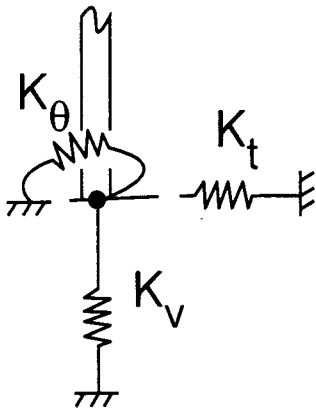
Session 5

Piles

- Configuration and Behavior
- Including Flexibility in Analysis
- **Coupling Effects**
- Nonlinear Effects
- Multiple Pile Groups / Axial Stiffness
- Design and Detailing

Coupling Effects / Overview

No Coupling



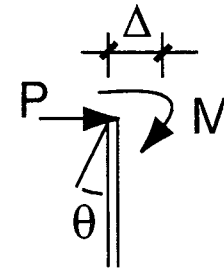
- Individual Springs

$$P = K_t \Delta_t$$
$$M = K_\theta \theta$$
$$V = K_v \Delta_v$$

Coupling (P and M)

$$P = K_{tt} \Delta + K_{t\theta} \theta$$

$$M = K_{\theta t} \Delta + K_{\theta\theta} \theta$$



- Apply P Alone $\rightarrow \Delta$ and θ
- Apply M Alone $\rightarrow \Delta$ and θ
- Include in Model with Either Stiffness or Flexibility Matrix for Foundation Node

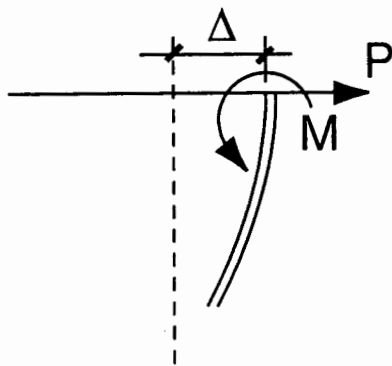
Calculating Coupled Stiffnesses (1 of 3)

- **Desired** K_{tt} , $K_{t\theta}$, $K_{\theta t}$, $K_{\theta\theta}$

Coupling Terms

- **Obtain These By**

1. Hold $\theta = 0$ / Apply $\Delta = 1$ / Calculate P and M^*



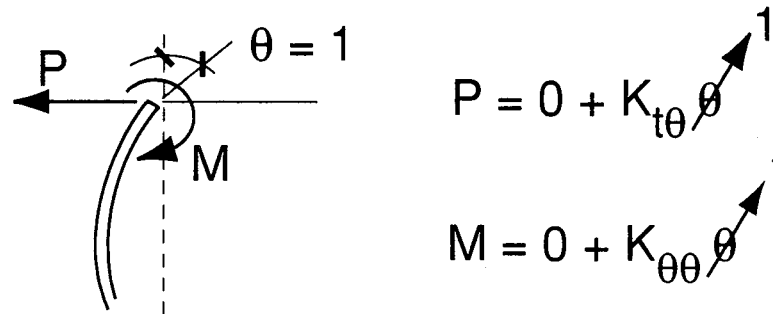
$$P = K_{tt}\Delta + K_{t\theta}\theta = K_{tt}$$

$$M = K_{\theta t}\Delta + K_{\theta\theta}\theta = K_{\theta t}$$

*Use Fixed-Head Charts Provided at End of Section

Calculating Coupled Stiffnesses (2 of 3)

2. Hold $\Delta = 0$ / Apply $\theta = 1$ / Calculate P and M



(See Outline of Method on Next Page)

3. Check / If Linear Elastic $\rightarrow K_{t\theta} = K_{\theta t}$
- **Analysis Programs Use These Coefficients**
(These Are Terms of "6 x 6 Matrix")

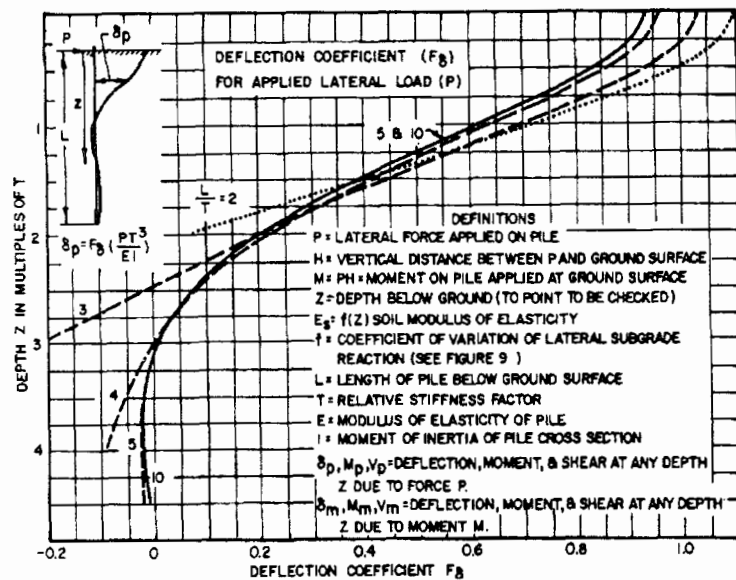
Calculating Coupled Stiffnesses (3 of 3)

Outline for Calculating $K_{t\theta}$ and $K_{\theta\theta}$

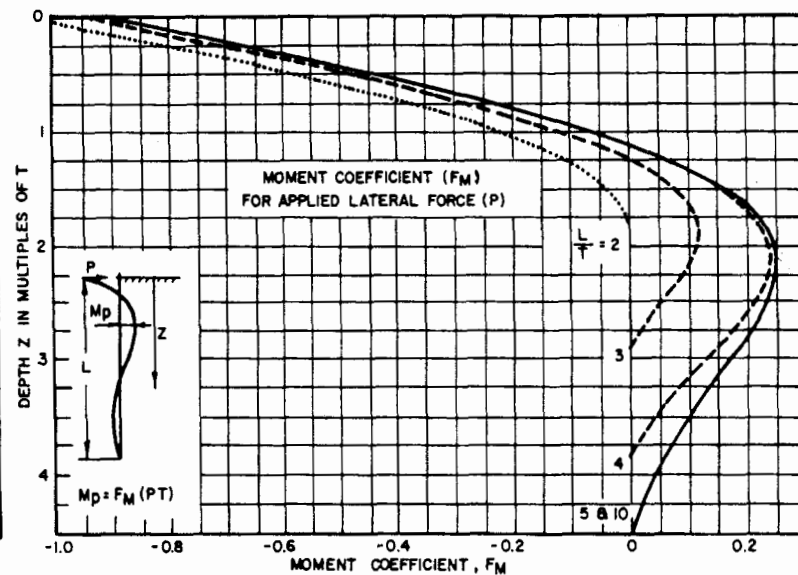
1. Apply Only P (Free Head)
 - Calculate Δ and θ (Slope) at Surface
(Charts for Slope Given at End of Section)
2. Apply Only M (Free Head)
 - Calculate Δ and θ at Surface
3. Form Superposition of Scaled P & M to Give $\theta = 1$ and $\Delta = 0$

Influence Coefficient / Fixed Head

NAVFAC DM7.02 (1986)

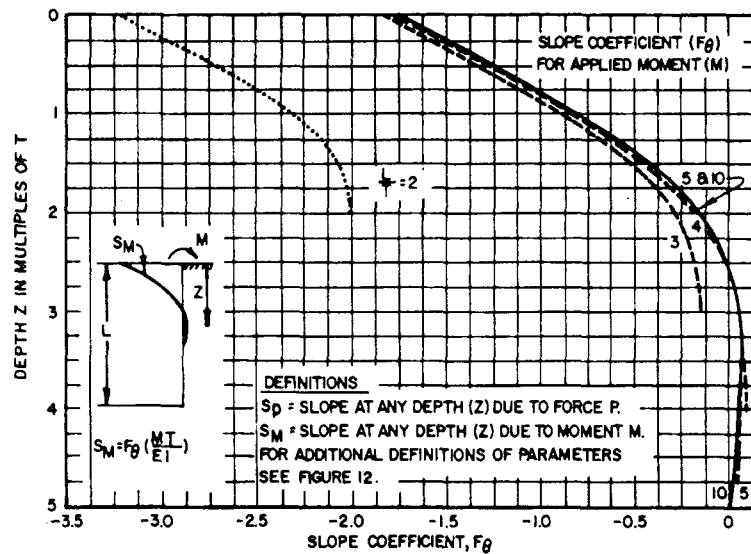


Deflection for Applied Load

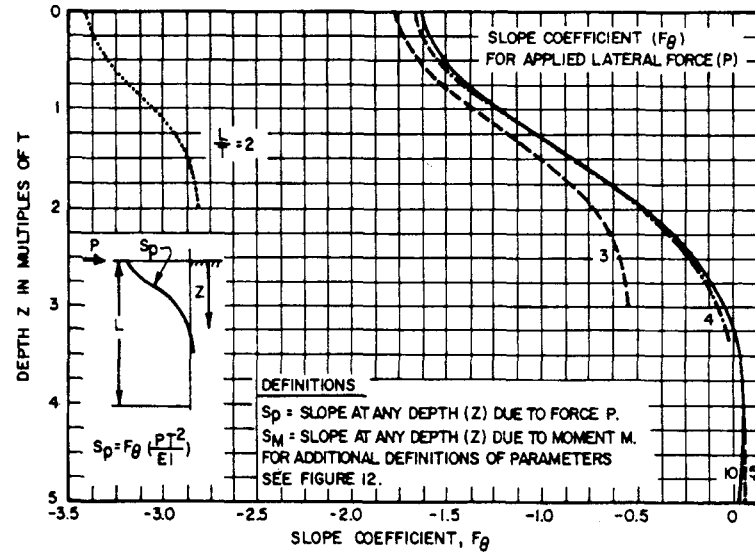


Moment for Applied Load

Slope (Rotation) of Piles / NAVFAC DM7.02



Slope for Applied Moment



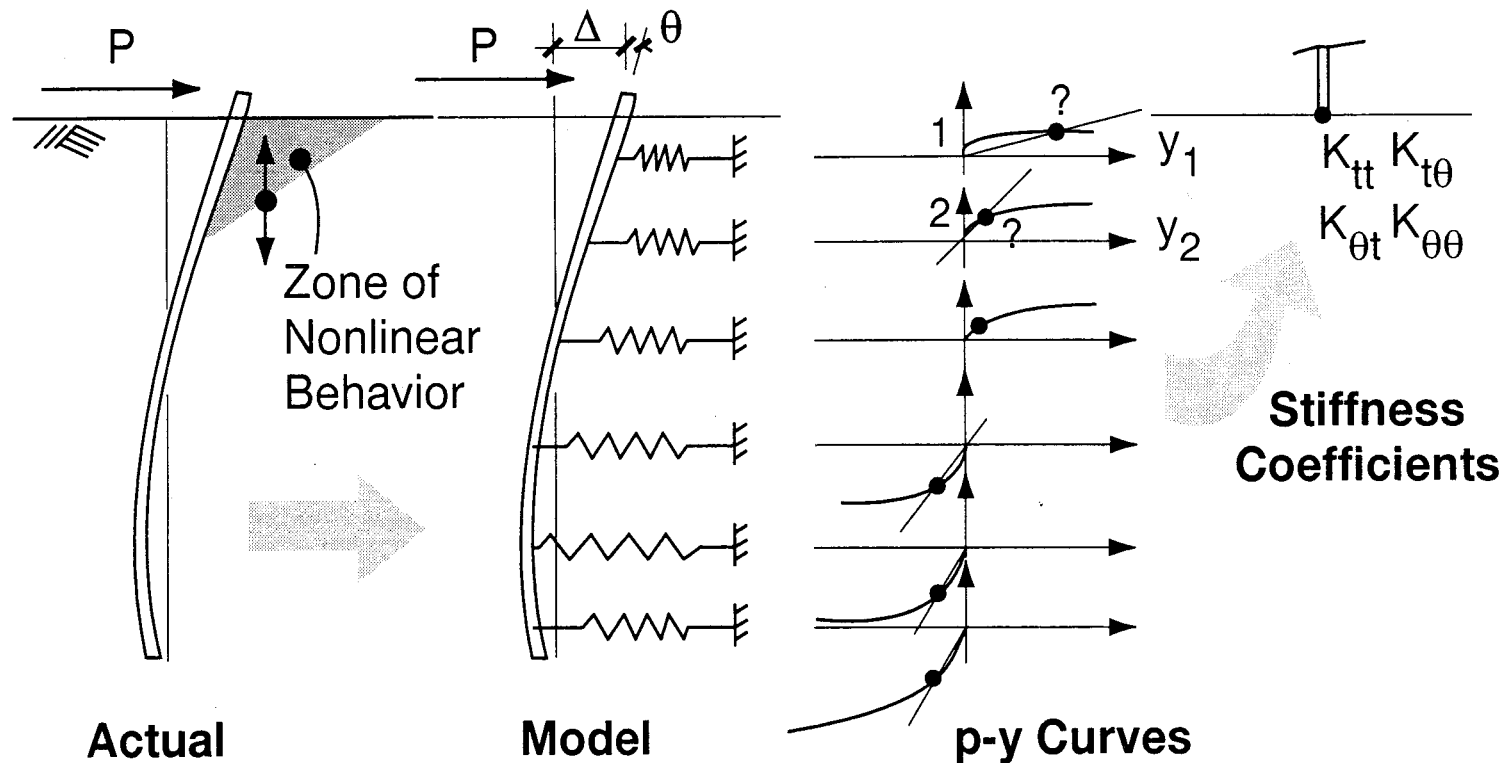
Slope for Applied Load

Session 5

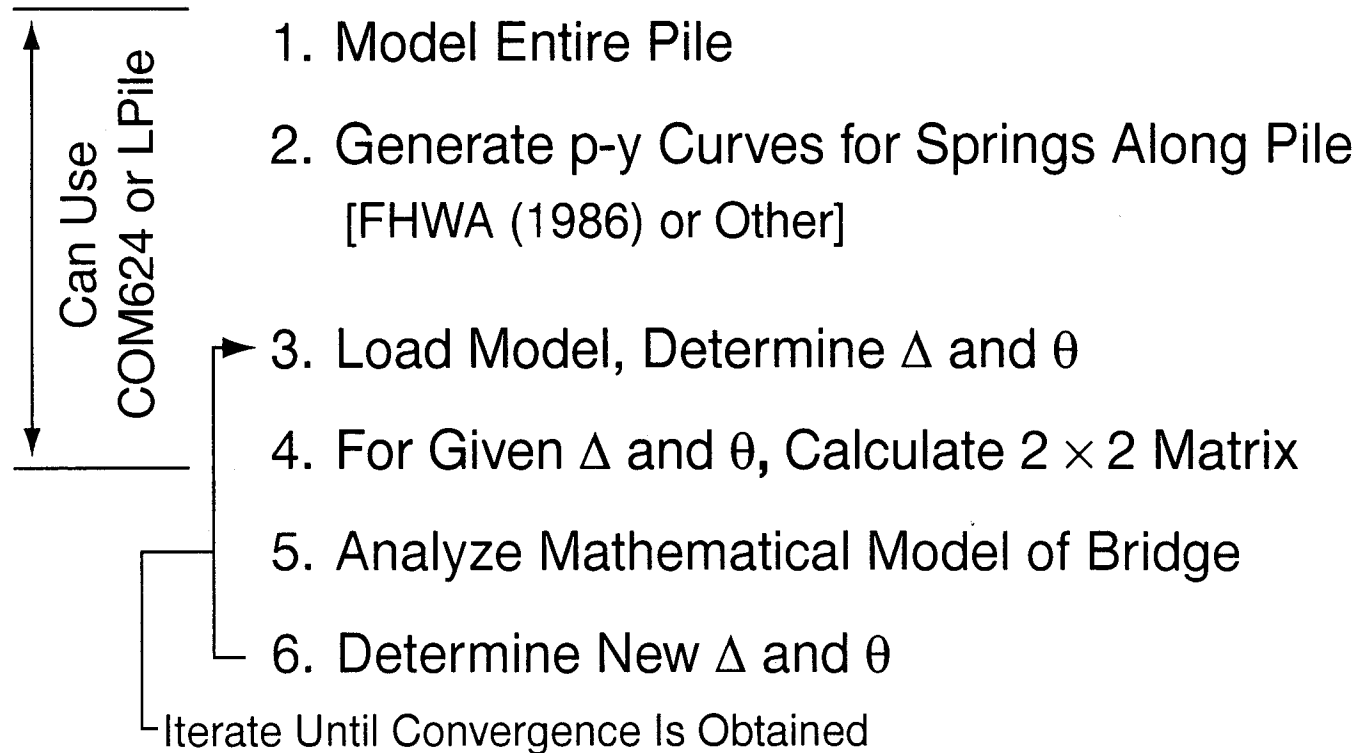
Piles

- Configuration and Behavior
- Including Flexibility in Analysis
- Coupling Effects
- **Nonlinear Effects**
- Multiple Pile Groups / Axial Stiffness
- Design and Detailing

Nonlinear Effects of Soil



Developing Stiffness for Nonlinear Case



Session 5

Piles

- Configuration and Behavior
- Including Flexibility in Analysis
- Coupling Effects
- Nonlinear Effects
- **Multiple Pile Groups / Axial Stiffness**
- Design and Detailing

Effects of Closely Spaced Piles

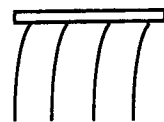
- **Group Effects**

<u>Pile Spacing in Direction of Loading</u>	<u>Reduction for Subgrade Modulus, n_h</u>
8D	1.00
6D	0.70
4D	0.40
3D	0.25

D = Pile Diameter

Stiffness for Pile Groups / Rigid Cap

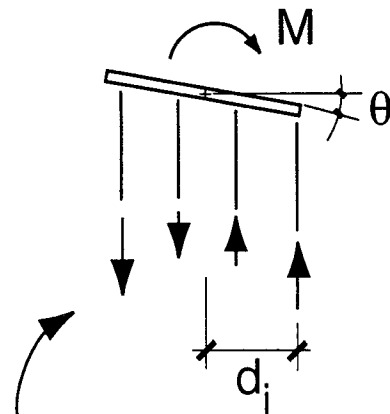
- Translation



$$K = nK_t$$

n Piles

- Rotation

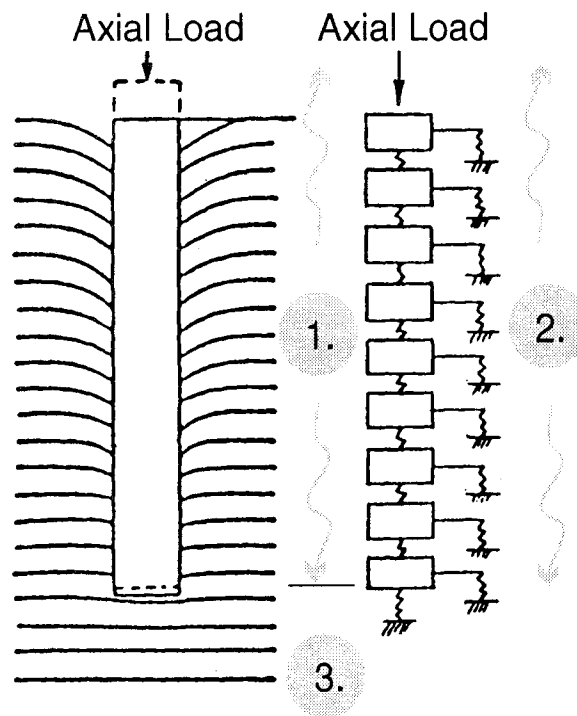


$$K_{\theta \text{ group}} \approx \sum_{i=1}^n K_{\text{axial}} d_i^2 = \frac{M}{\theta}$$

Axial K Most Important

Axial Stiffness Components

Vertical Loading Behavior



FHWA (1986)

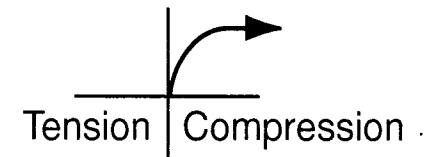
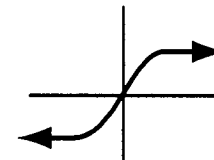
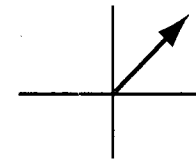
Components of Flexibility

1. Pile Stiffness

2. Side Friction

3. End Bearing

Force / Deformation



Axial Stiffness of Piles

1. Pile Stiffness — $\frac{AE}{L}$

2. Side Friction — $f = f_{\max} \left(2\sqrt{\frac{z}{z_c}} - \frac{z}{z_c} \right)$

(No Universal Agreement,
'a Way to Do It')

f_{\max} = Maximum
Unit Friction

z = Slip

z_c = Critical Slip (0.2 in)

3. End Bearing — $q = \left(\frac{z}{z_c} \right)^{1/3} q_{\max}$

(No Universal Agreement,
'a Way to Do It')

q_{\max} = Maximum
Tip Resistance

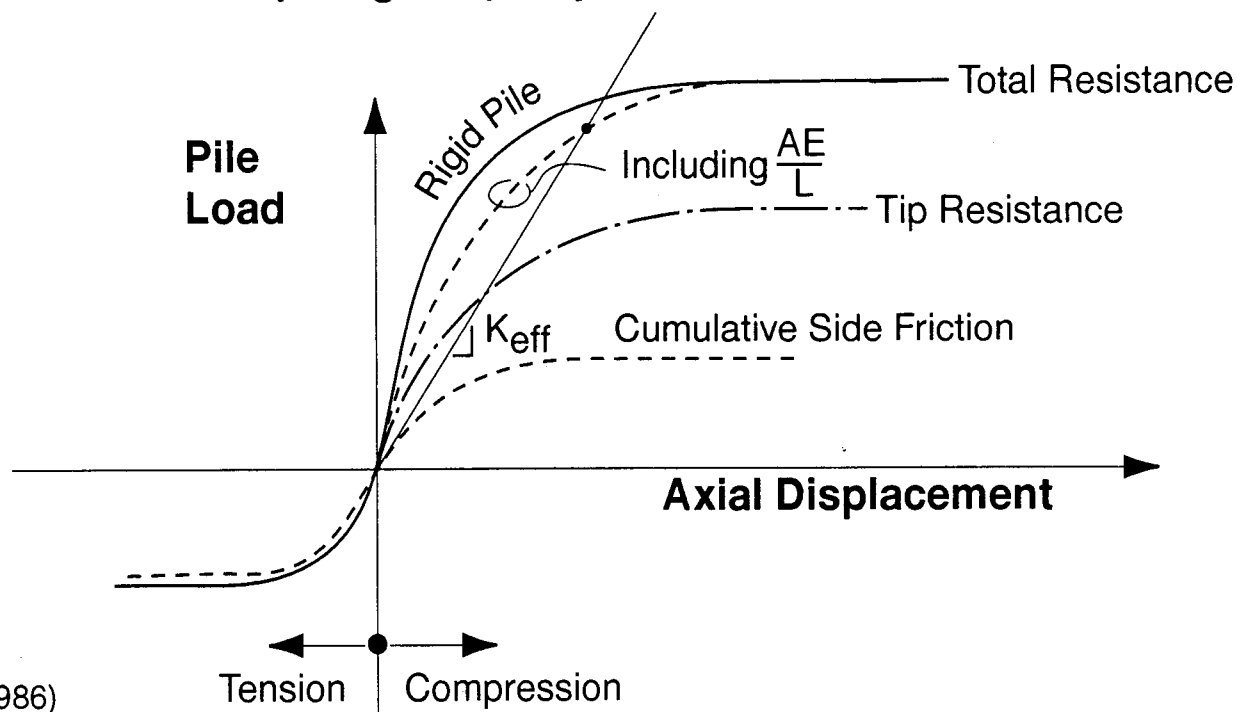
z = Deflection at Tip

z_c = Critical Displacement
at $q_{\max} \sim 0.05$ Diameter

FHWA (1986)

Axial Stiffness of Piles (continued)

Sum (Integrate) Expressions to Obtain:



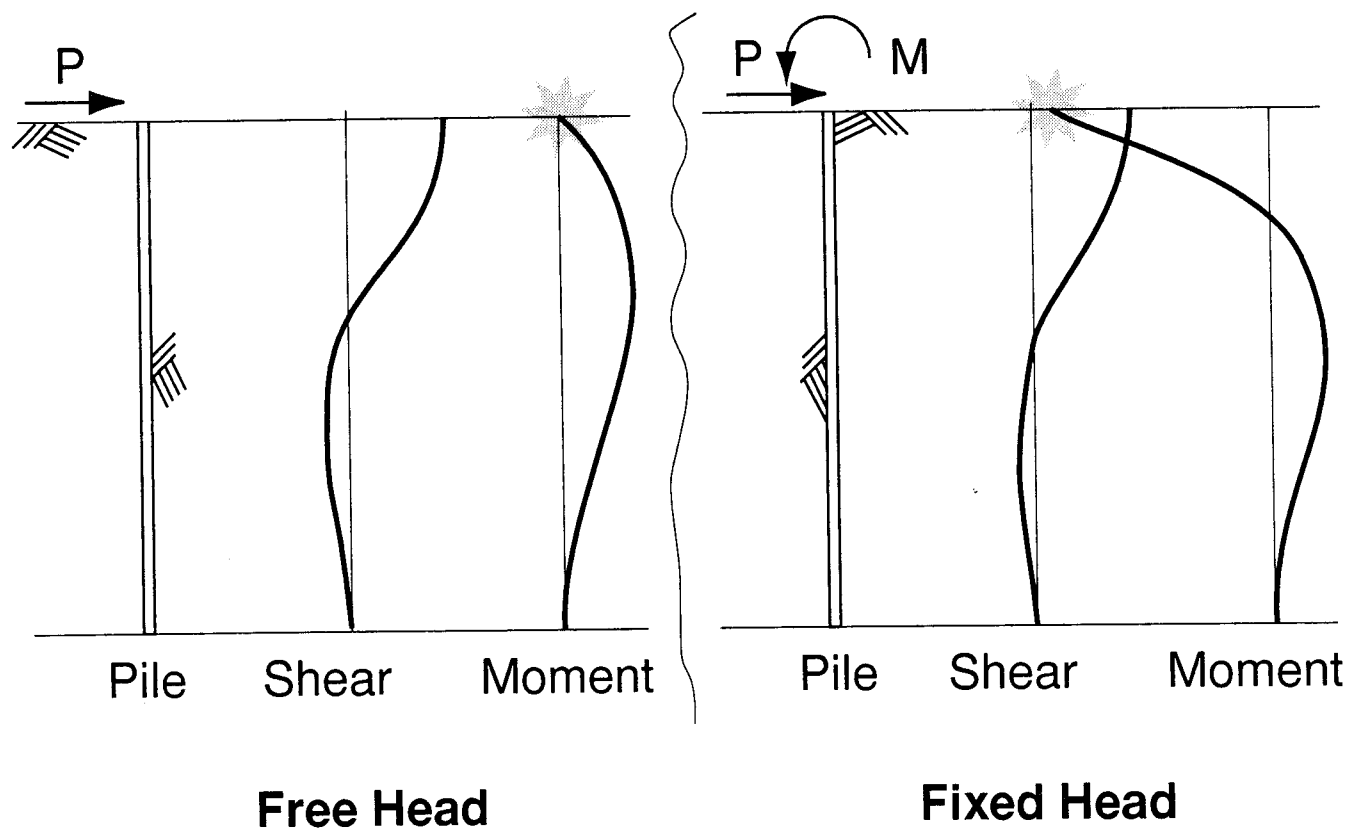
FHWA (1986)

Session 5



Piles

- Configuration and Behavior
- Including Flexibility in Analysis
- Coupling Effects
- Nonlinear Effects
- Multiple Pile Groups / Axial Stiffness
- **Design and Detailing**

Internal Force Distributions (Elastic)



Effect of Head Condition

- **Performance Objective**  Damage Should Be Detectable
∴ Not in Foundation
- **Design**  Elastic or Plastic Hinging Forces

Fixed Head — Large Moment / Concentrated Near
Top of Pile
∴ Potential for Plastic Hinging

Free Head — Largest Moment at Depth /
Distributed Curvatures

Division I-A Requirements (1 of 6)

Overview

- Capacity Protect / $R = 1.0$ or Hinging Forces
 - Tie Piles and Cap Together
 - Provide Ductility at Top of Pile
-

SPC B / 6.4.2 (C)

- Design to Carry All Forces

Plus

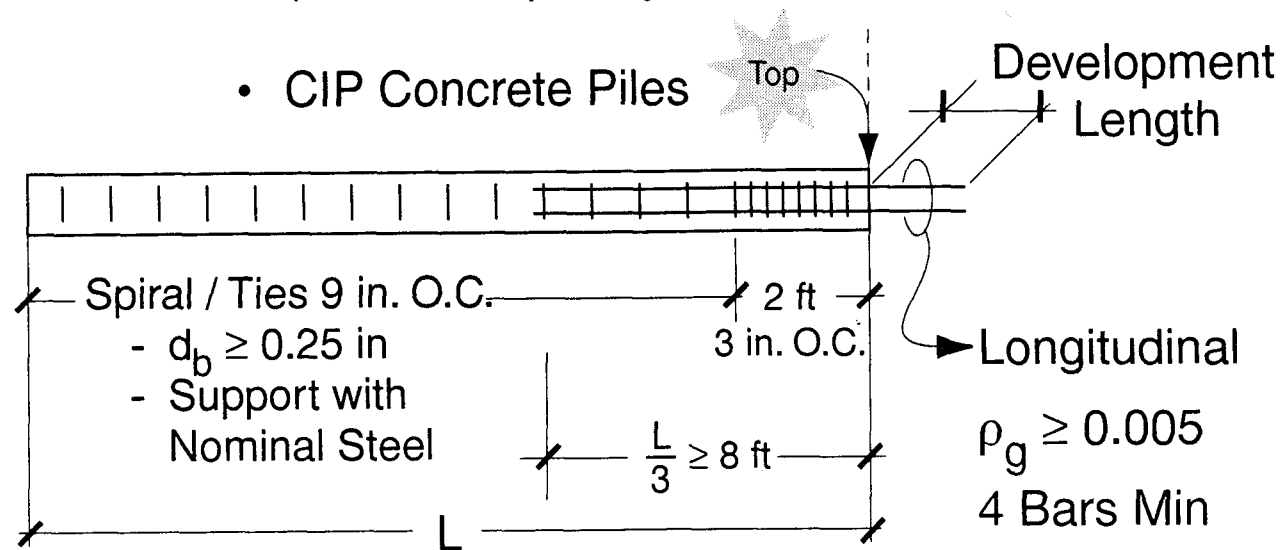
- Timber and Steel — Uplift Capacity $\geq 10\%$ of Allowable Pile Load

Division I-A Requirements (2 of 6)

SPC B / 6.4.2 (C) (continued)

- Concrete-Filled Pipe Pile — 4 Dowels / $\rho = 0.01$
(Note: Completely Free Head Not Realistic)

- CIP Concrete Piles



Division I-A Requirements (3 of 6)

SPC B / 6.4.2 (C) (continued)

- Precast Piles
 - $\rho_g \geq 0.01$ (4 Bars Min) Over Entire Length
 - Spiral / Ties $\geq \#3$
 - Spacing as for CIP Piles
- Precast — Prestressed Piles
 - Same Ties as for Precast Piles

Division I-A Requirements (4 of 6)

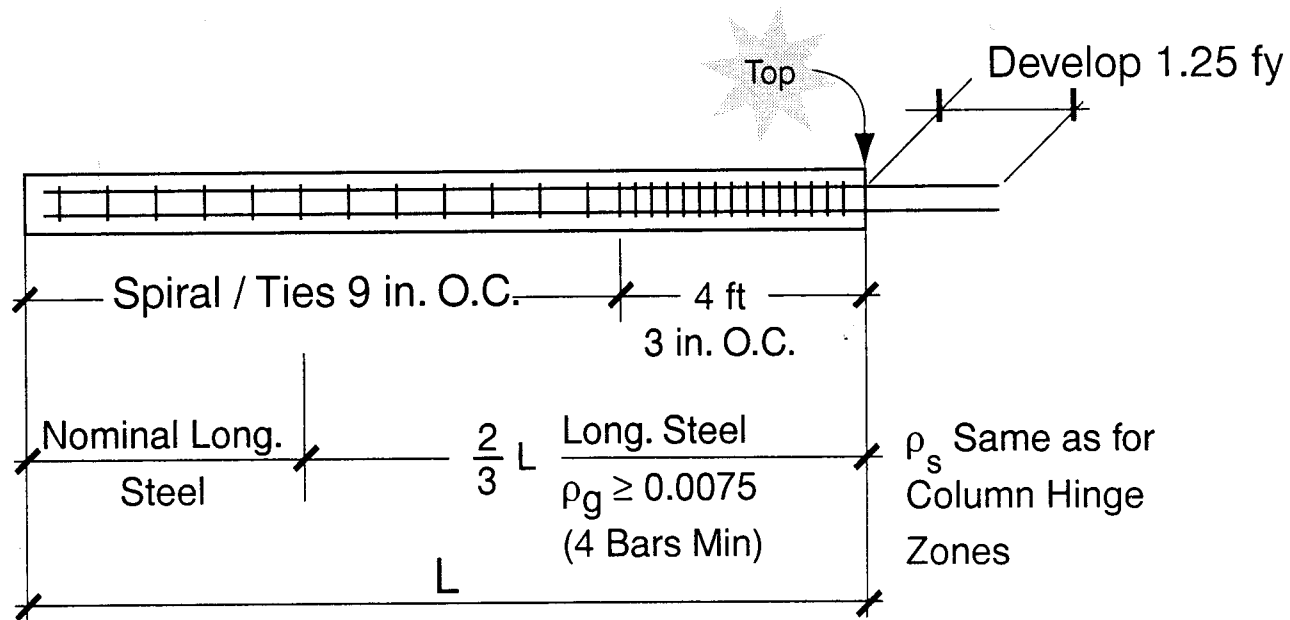
SPC C and D / 7.4.2 (C)

- Same as SPC B
- Concrete Piles
 - Anchor to Cap to Develop $1.25 f_y$ of Pile Longitudinal Bars
- Potential Plastic Hinge Zones
 - Same Confinement as for Columns!
 - $2D_{pile}$ or 24 in. at Top or Other Possible Hinge Zones

Division I-A Requirements (5 of 6)

SPC C and D / 7.4.2 (C) (continued)

- CIP Concrete Piles

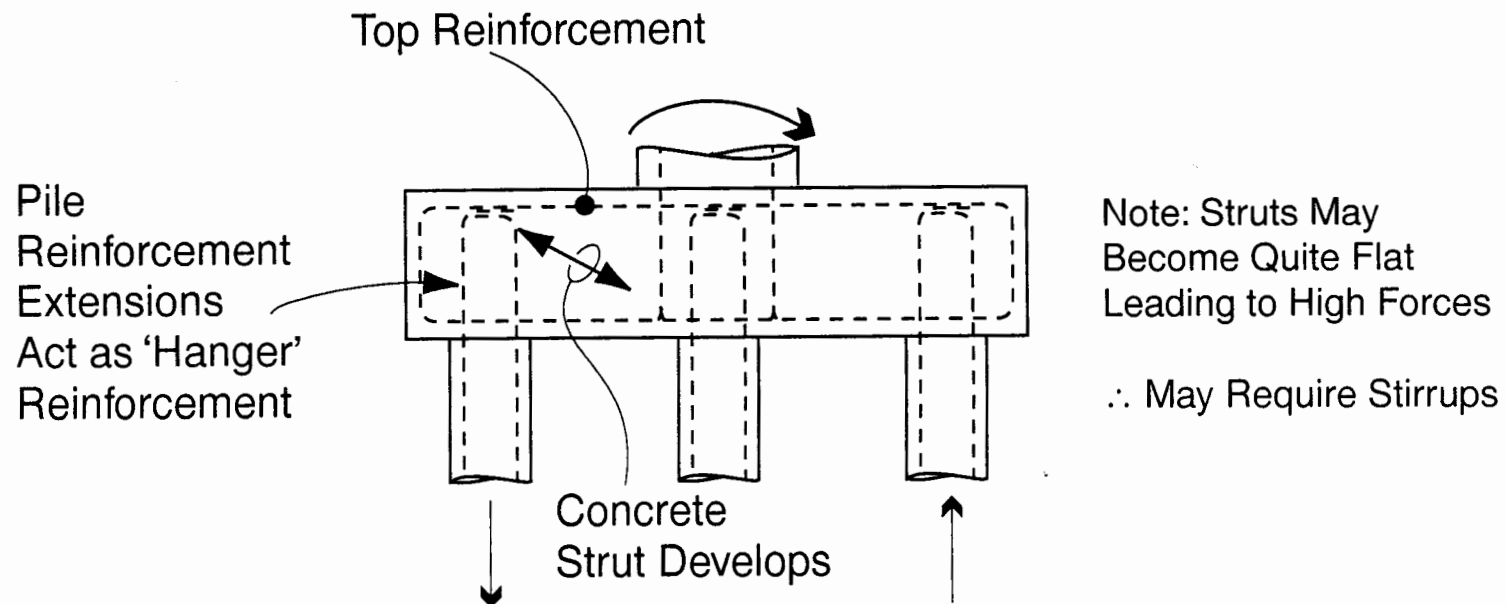


Division I-A Requirements (6 of 6)

SPC C and D / 7.4.2 (C)

- Precast Piles
 - $\rho_g \geq 0.01$ (4 Bars Min) Over Entire Length
 - Spiral / Ties $\geq \#3$
 - Spacing as for CIP Piles
- Precast — Prestressed Piles
 - Same Ties as for Precast Piles

Pile Cap Considerations for Uplift Forces



Session 6

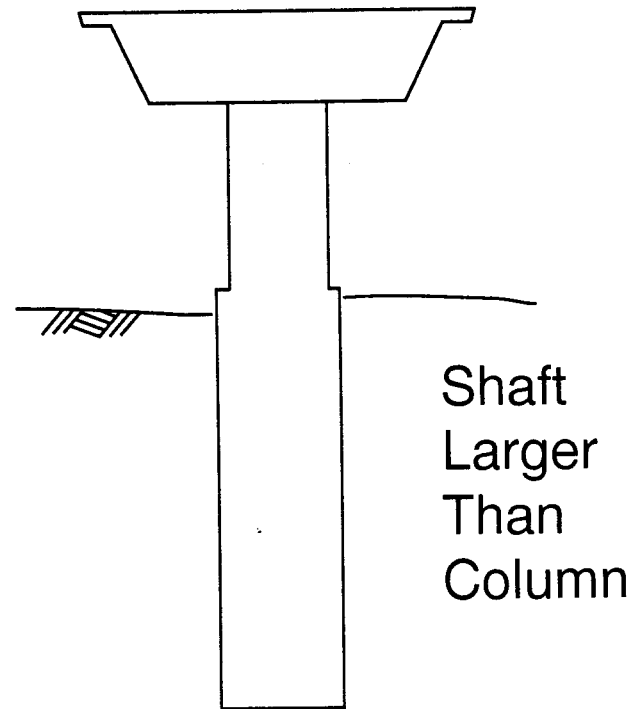
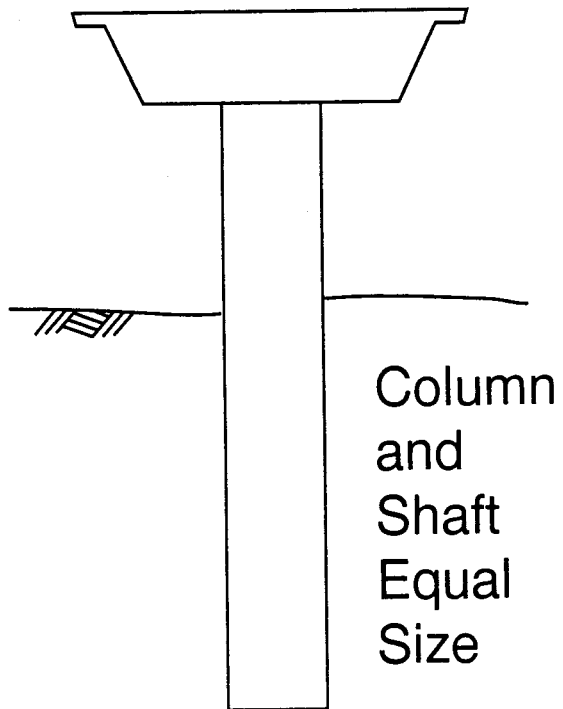
Curved Box Girder Bridge Example

Drilled Shaft*

- **Behavior and Stiffness**
- **Design and Detailing**

* Also Called Pile Shafts, etc.

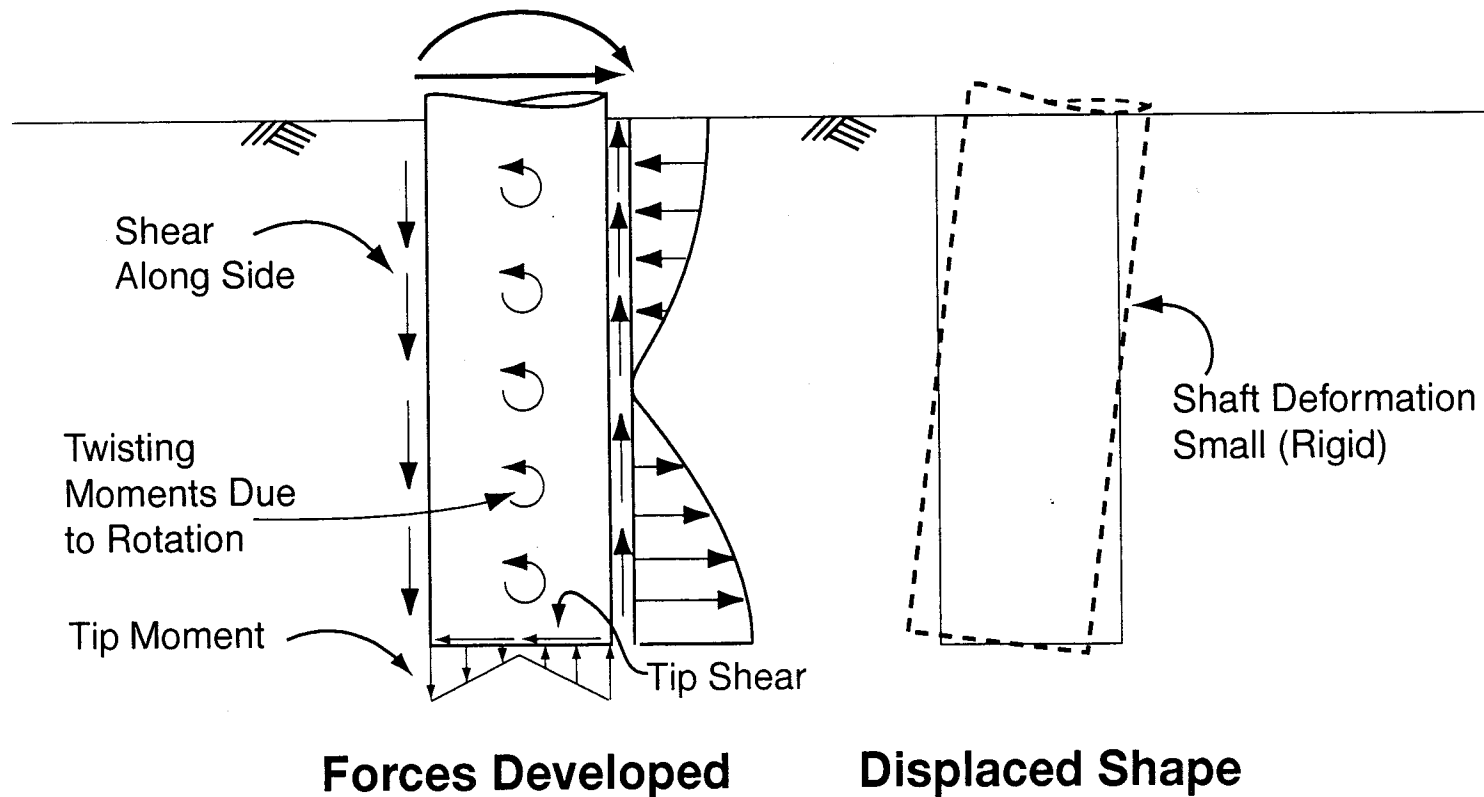
Configurations



Drilled Shaft Behavior

- Lateral Behavior Similar to Piles
- Length / Diameter (or L / T) Smaller Than Piles
 - Stiffness Less Than Longer Elements of Same Diameter
 - Lateral Stiffness More Sensitive to (L / T)
 - Coupling Between Displacement and Rotation More Important
- Larger Diameters Lead to Additional Mechanisms for Resistance

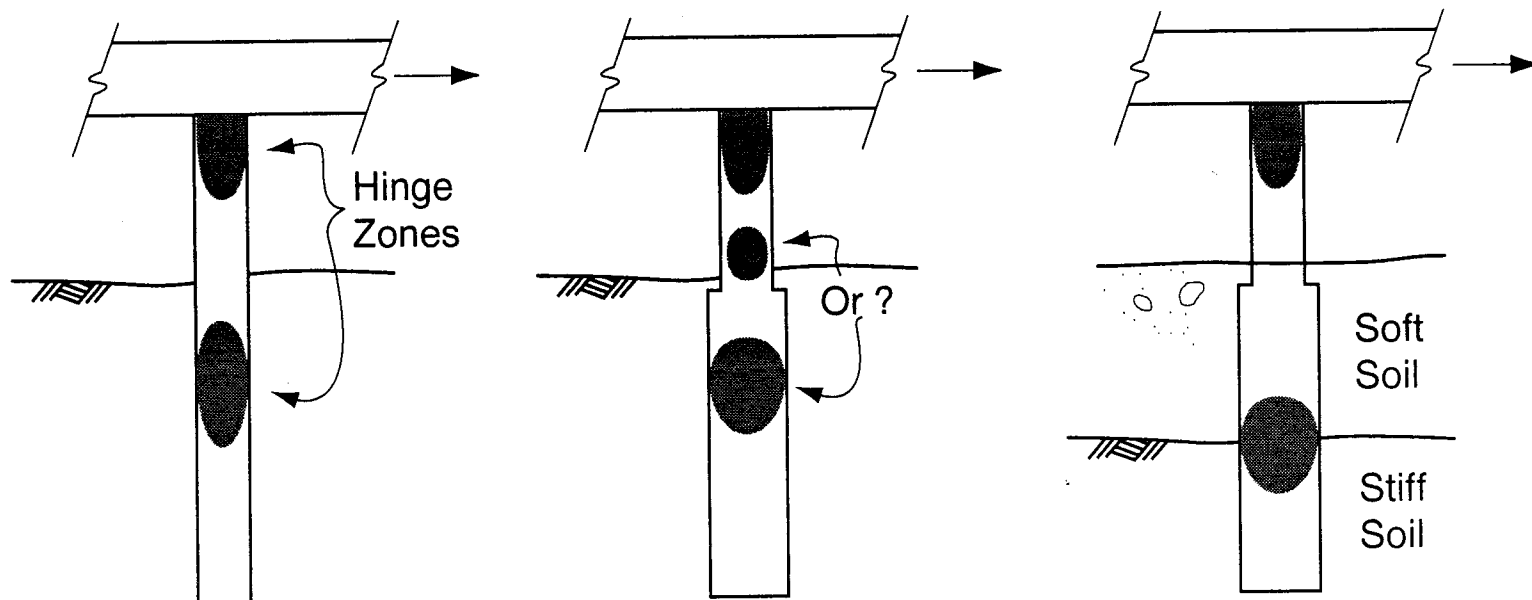
Mechanisms of Lateral Resistance



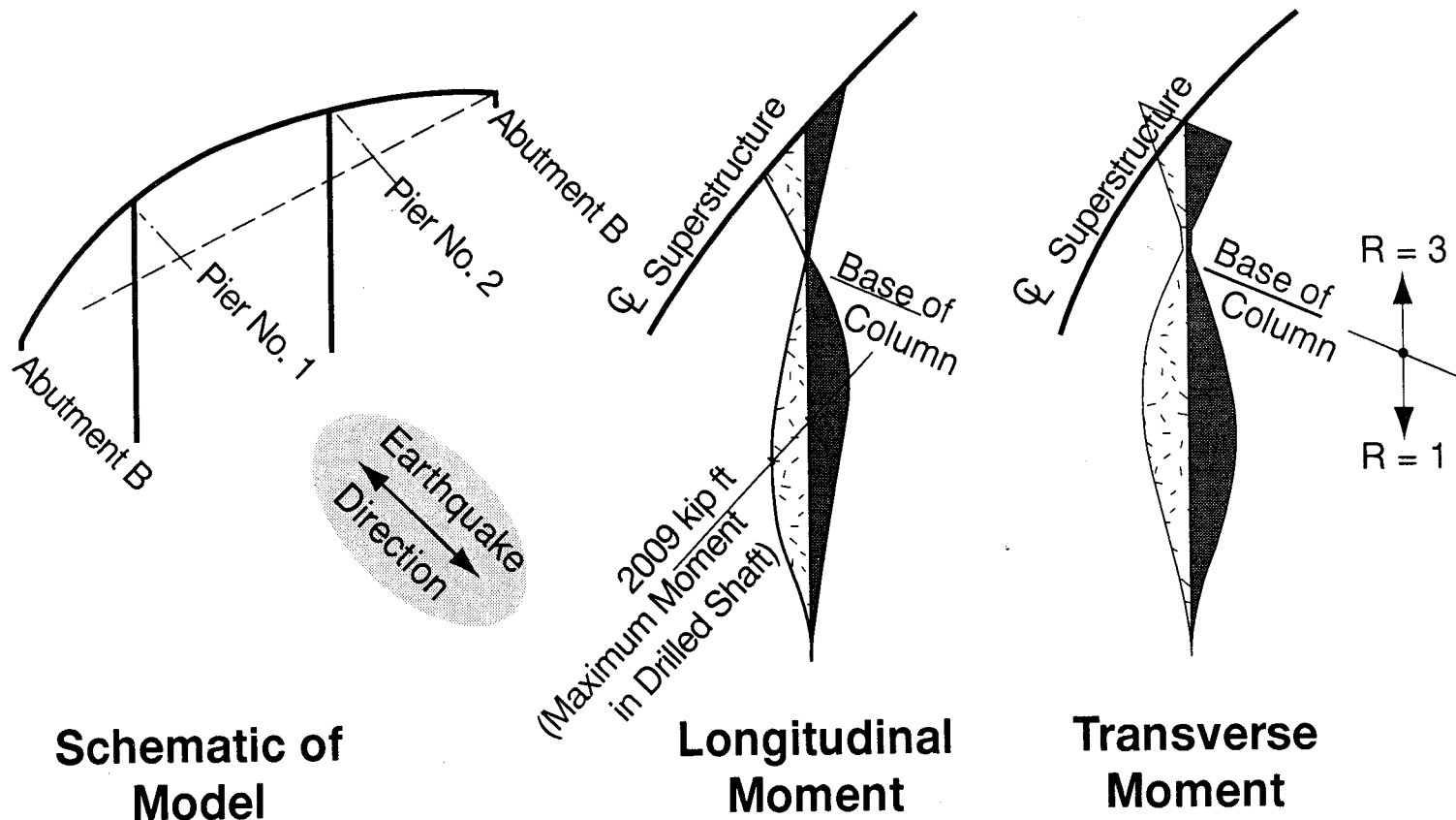
Developing Stiffness of Drilled Shafts

- Use Same Approach as for Piles
- Neglect Additional Resistance Mechanisms
(May Underpredict Strength)
- Include Coupling Effects (More Critical Than with Piles)
- Some Methods Are Under Development for Including
All Resistance Mechanisms
(Approaches May Change in the Future)

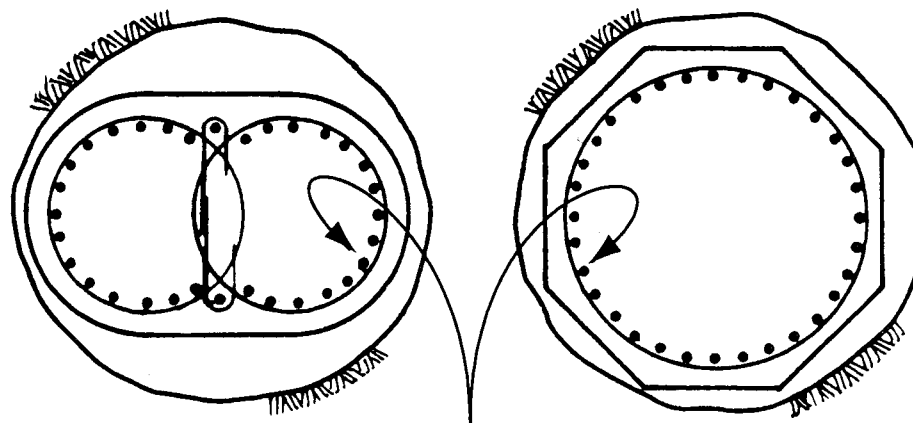
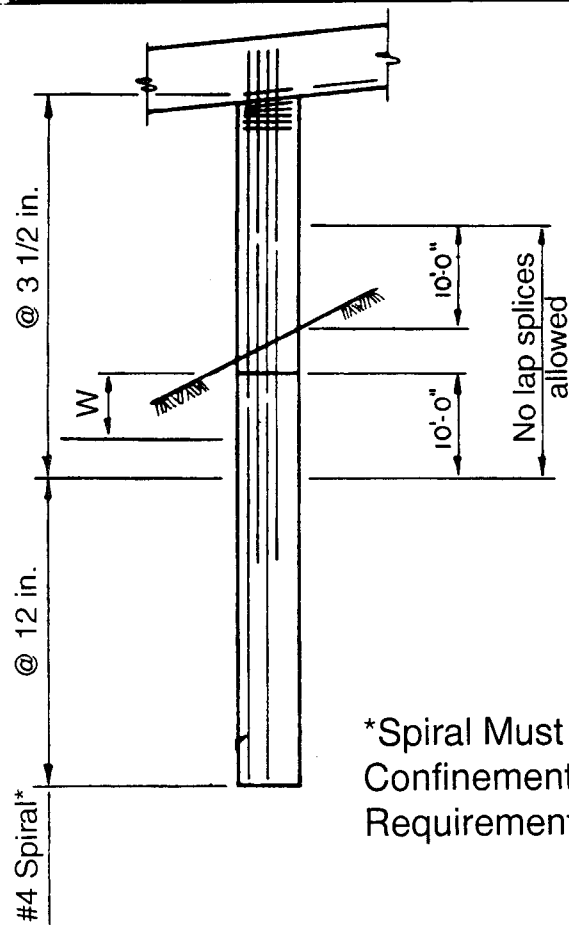
Plastic Hinging Behavior



Example / Distribution of Elastic Moments



Detailing Issues/ 'Same Size' Columns and Shafts

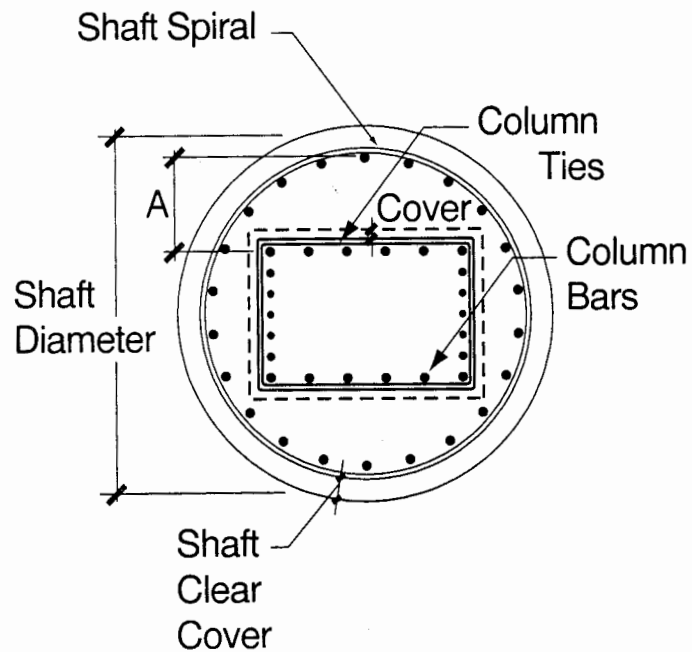


Reinforcement Pattern Extending into
CIDH Pile to Be the Same as in Column

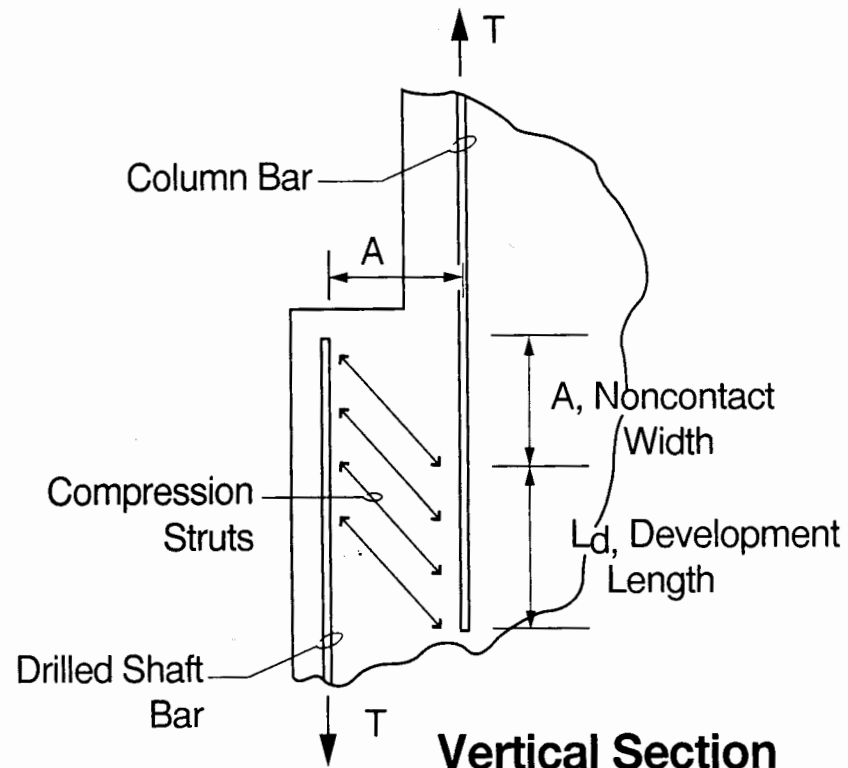
*Spiral Must Comply with
Confinement and Shear
Requirements

Caltrans (1995)

Detailing Issues/ Shafts Larger Than Columns

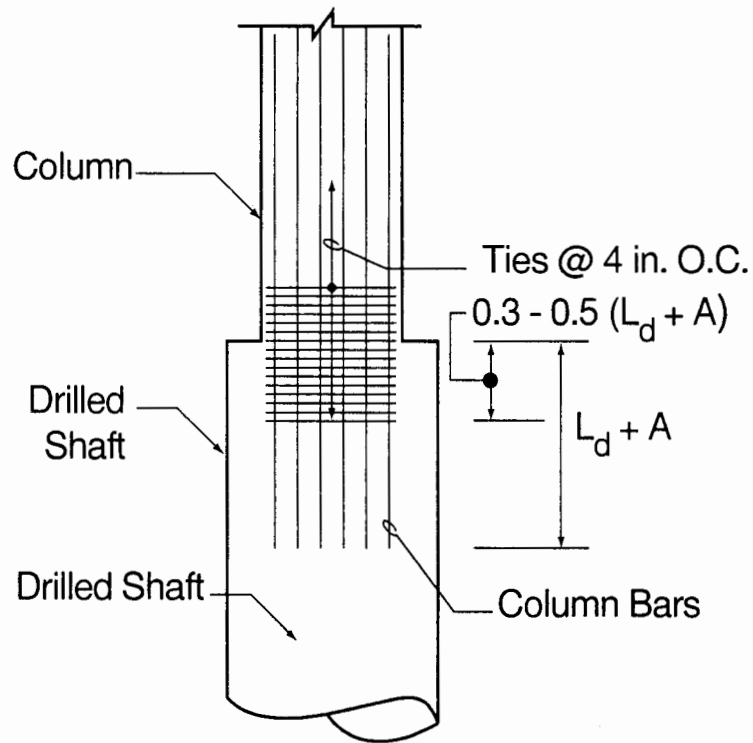


Horizontal Section

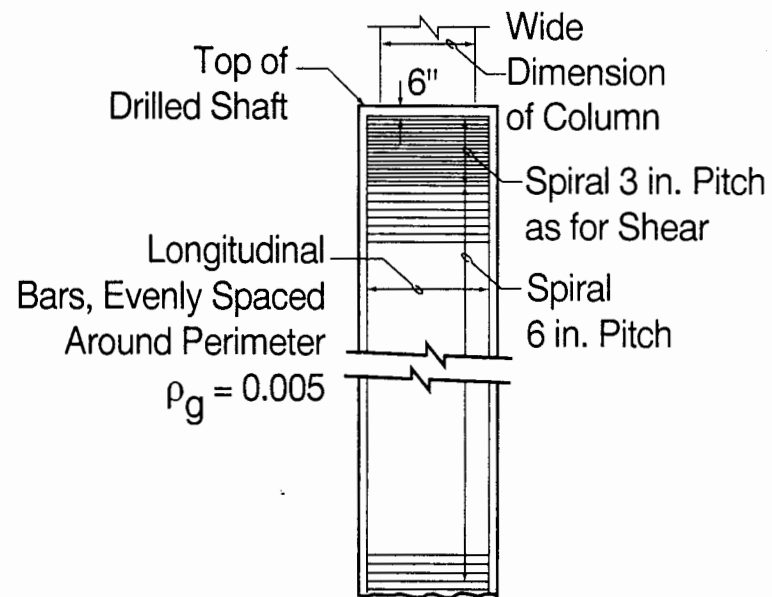


Vertical Section

Detailing Issues/ Shafts Larger Than Columns



Section at Connection



Shaft Reinforcement

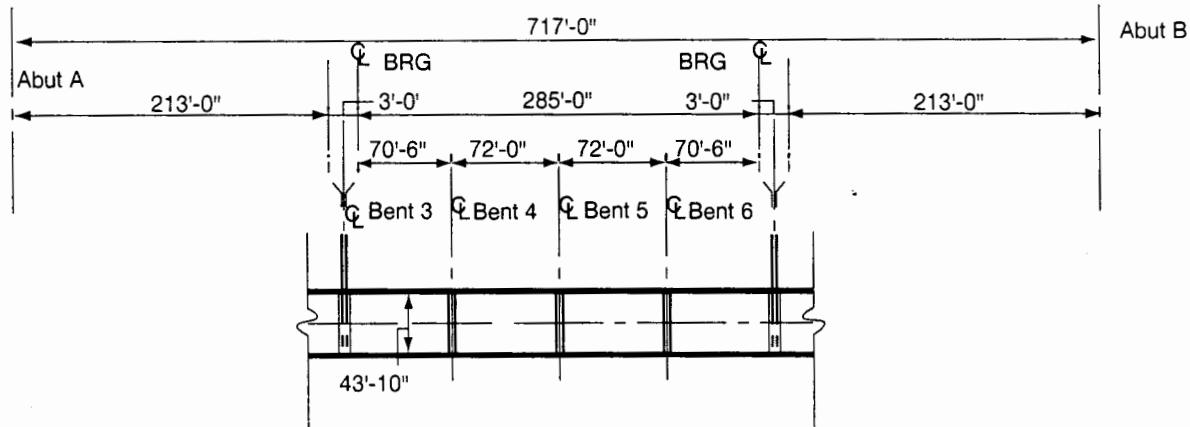
Session 6

Pile Bent Bridge Example

Pile Bent Issues

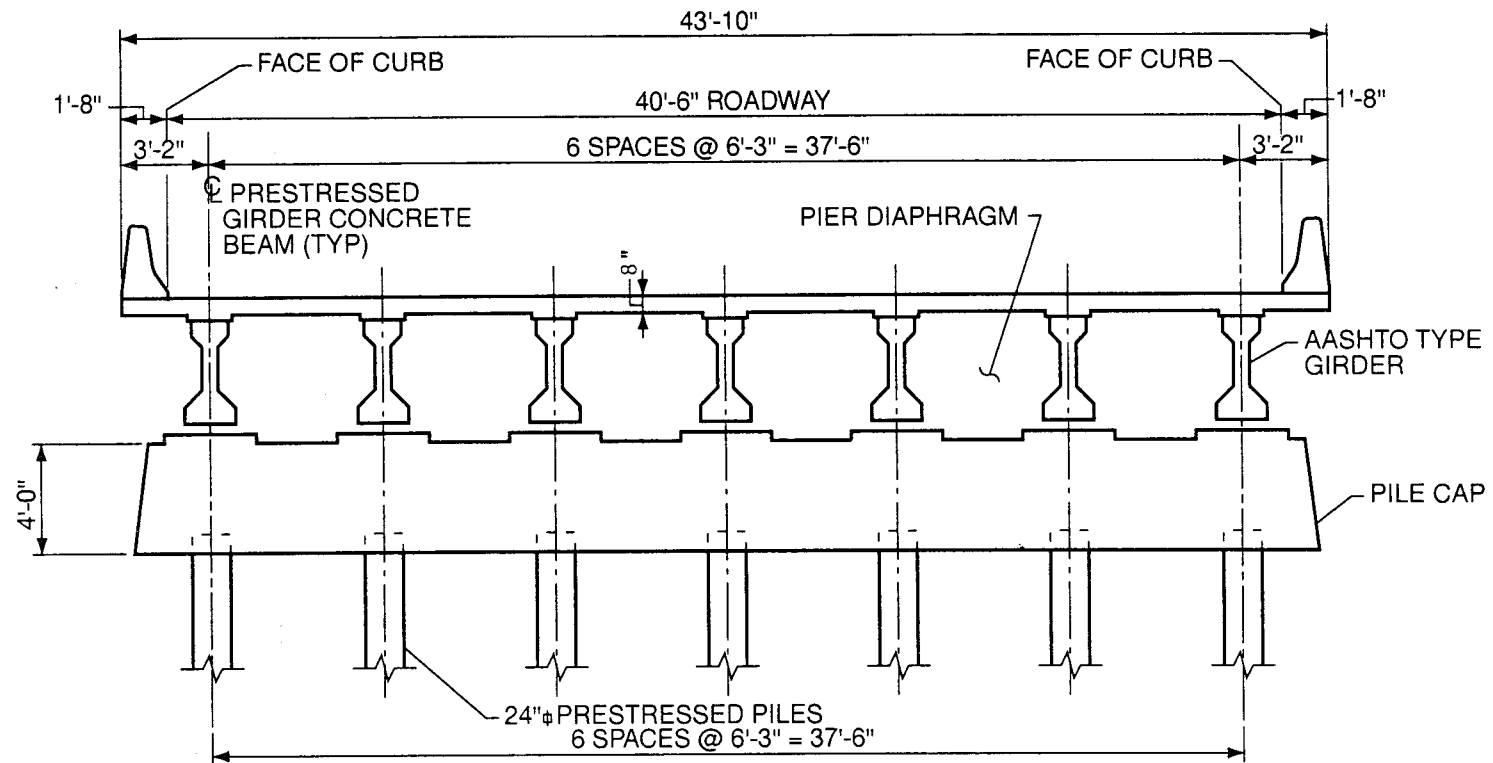
- **Description**
- **Behavior**
- **Stiffness Considerations**
- **Design Considerations**

Elevation



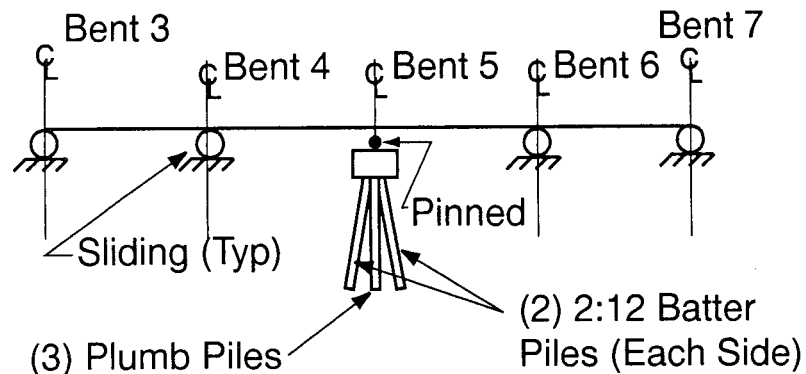
Plan of Center Unit

Pile Bent Bridge / Bent Elevation



Section

Typical Configuration / Lateral Load Transfer

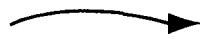


Longitudinal Structural Model

- All Longitudinal Inertial Loads Taken by Bent No. 5
- All Other Bents Assumed to Have Sufficient Seat Widths
- Stiffness of and the Load Taken by Bent No. 5 Very Dependent on Number and Slope of Batter Piles

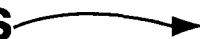
Developing the Stiffness of Pile Bents

Plumb Piles



- Methods for Piles (Previously Discussed) May Be Used
- Account for Clear Height Above Mudline

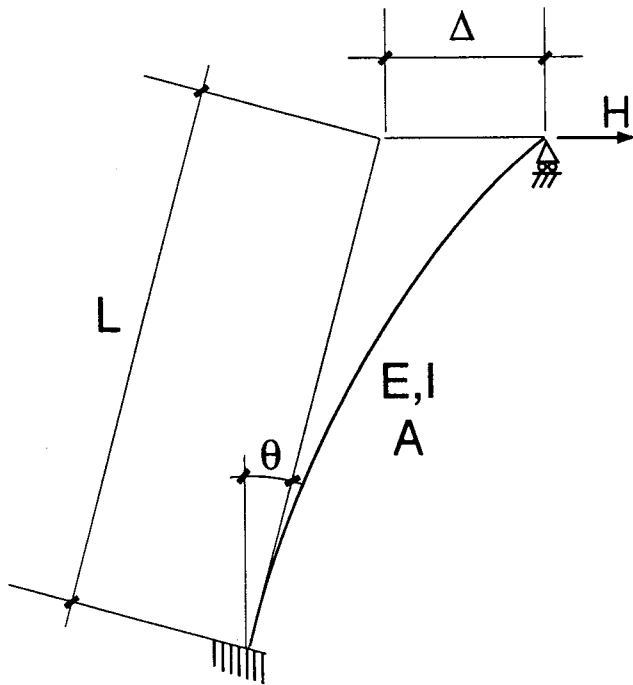
Battered Piles



- Separate Flexural and Axial Effects
- Standard Pile Methods for Flexure
- Axial Stiffness and Capacity Much More Important

Lateral Stiffness of Battered Pile

Consider One Pile of a Two Battered Pile Pair



$$K = \frac{H}{\Delta} = \frac{3EI}{L^3} \cos^2 \theta + \frac{AE}{L} \sin^2 \theta$$

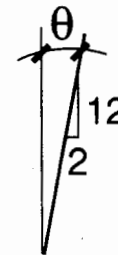
- No Rotational Restraint at Cap
- If Cap Fixed $3 \rightarrow 12 \frac{EI}{L^3}$
- No Axial (Soil) Deformation Below Pile
- If Add Flexibility Beneath Pile

$$\frac{AE}{L} = K_{\text{eff}} = \frac{1}{1/(AE/L) + 1/K_{\text{soil}}}$$

Example / Lateral Stiffness of 2:12 Batter Piles (1 of 3)

- 24 in. Square Prestressed Concrete Pile

$$\begin{array}{lll} E = 4030 \text{ ksi} & L = 60 \text{ ft} & \theta = 9.46^\circ \\ A = 40 \text{ ft}^2 & I = 1.33 \text{ ft}^4 & \end{array}$$



- Use Different Effective Length to Fixity for Flexure and Axial Contributions

$$\begin{array}{ll} L_f = 25 \text{ ft} & \text{Based on Equivalent Cantilever for Plumb Pile} \\ L_a = 41.7 \text{ ft} & \text{Based on Skin Friction and No Tip Displacement} \end{array}$$

Example / Lateral Stiffness of 2:12 Batter Piles (2 of 3)

- Flexural Contribution to Lateral Stiffness

$$K_f = \frac{3EI}{L_f^3} \cos^2 \theta + \frac{3(4030)144}{(25)^3} \cos^2 (9.46^\circ) = 144 \frac{\text{kip}}{\text{ft}}$$

- Axial Contribution to Lateral Stiffness

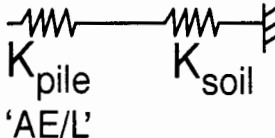
$$K_a = \frac{AE}{L_a} \sin^2 \theta = \frac{4.0(4030)144}{41.7} \sin^2 (9.46^\circ) = 1504 \frac{\text{kip}}{\text{ft}}$$

Even @ 2:12 $K_a \sim 10 K_f$

Example / Lateral Stiffness of 2:12 Batter Piles (3 of 3)

- Include (Approximately) the Surrounding Soil Flexibility
From Geotech: Soil $\Delta \sim 0.25$ in at 600 kip maximum load

$$K_{\text{soil}} = \frac{600}{0.25} = 2400 \text{ kip/in}$$

- Assume \longrightarrow 

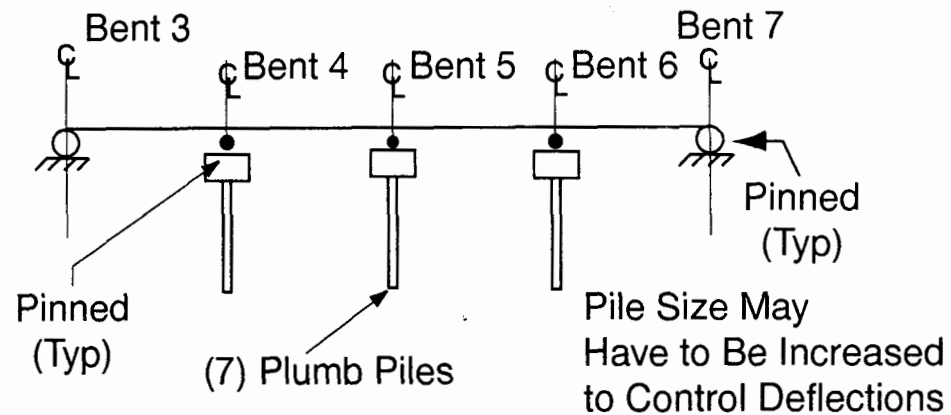
$$K_a = \frac{1}{\frac{1}{\frac{4.0(4030)144}{41.7}} + \frac{1}{2400(12)}} \sin^2 (9.46^\circ) = 513 \frac{\text{kip}}{\text{ft}}$$

$K_a \sim 3.6 K_f$

Considerations for Batter Pile Designs (1 of 3)

- High Axial Stiffness Will Attract Large Seismic Forces
- In Some Cases, May Consider Using All Plumb Piles

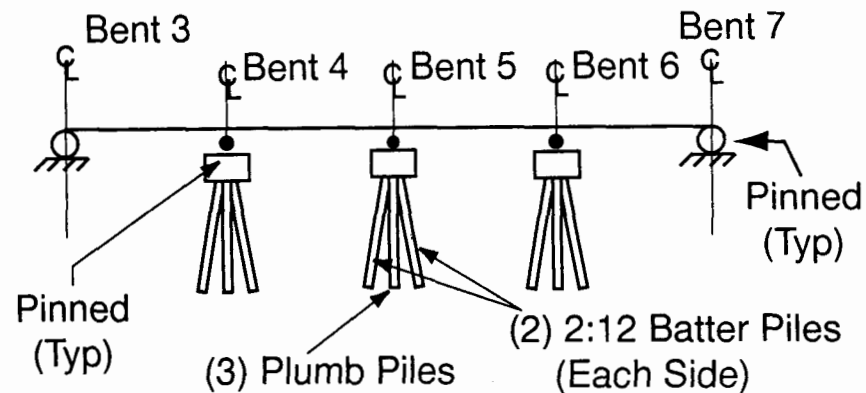
For Instance:



Considerations for Batter Pile Designs (2 of 3)

- More Than One 'Braced' Bent Per Frame May Be Required

For Instance:



R Factors for Pile Bents

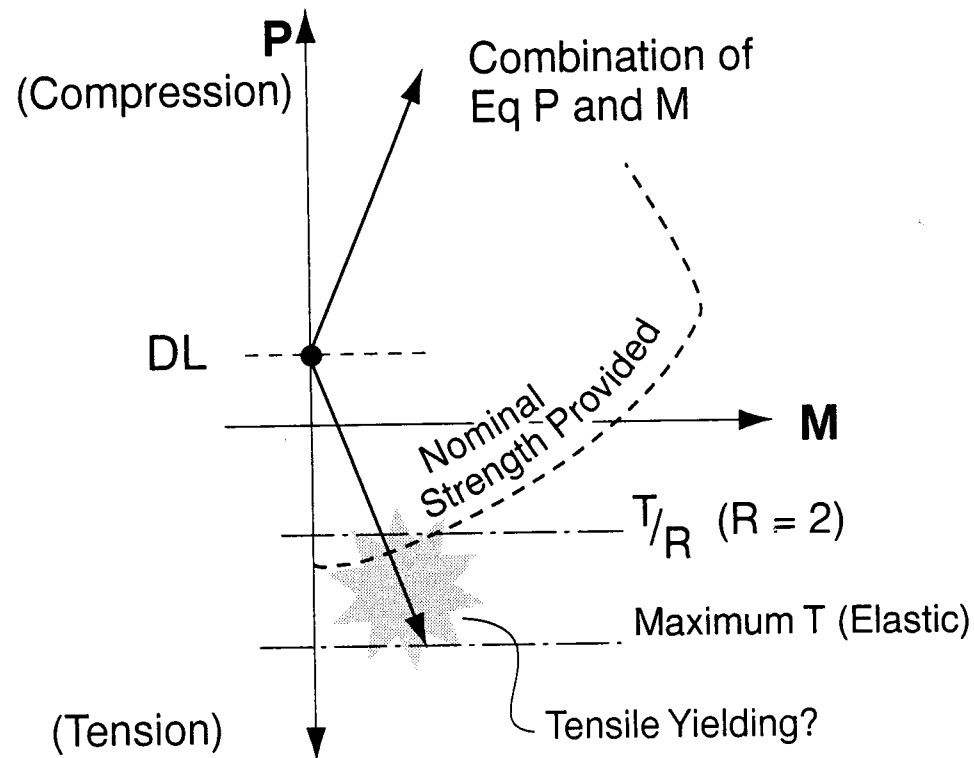
AASHTO Division IA, Table 3

	Concrete Piles	Steel Piles
All Piles Vertical (Plumb)	3	5
Some Piles Battered	2	3

SPC B: Do Not Divide Above Factors by 2 for “Foundations”

SPC C and D: Use $R = 1$

Axial Force Issues



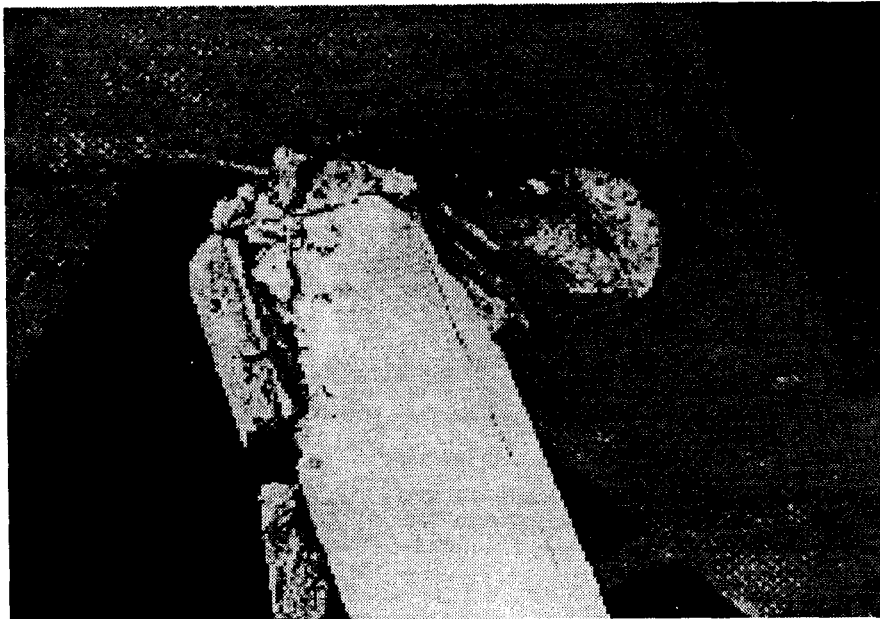
Consequences of Inadequate Tensile Strength / Batter Piles



Loma Prieta, 1989

EERI (1990)

Consequences of Inadequate Confinement / Plumb Piles



Loma Prieta, 1989

EERI (1990)

Considerations for Batter Pile Designs (3 of 3)

- Ductile Performance Is Associated with Plastic Hinging
- Axial Yielding Not Considered a Viable Ductile Mechanism
- Consider Designing with Elastic Forces?
(At Least For Axial Forces in Pile)
- Large Axial Forces Transferred to Soil May Result in Residual Displacements
- Does Bridge Collapse? — Probably Not
- Is Bridge Serviceable After Earthquake? — Probably Not

Examples / Results for Center Frame of Bridge

Options:

1. One Bent with Batter Piles
2. All Plumb Piles
3. All Bents Have Battered Piles

Concrete Pile Options	Units	Longitudinal Direction			Transverse Direction
		Option 1	Option 2	Option 3	
Total Stiffness, K	kip/in.	587	258	1761	583
Period, T	sec	0.74	1.17	0.45	0.40
Total Seismic Shear, V	kip	550	447	845	225
Elastic Deflection, Δ	in	0.94	1.73	0.48	0.39
Max. Pile Tension	kip	-590		-238	
Max. Pile Compression	kip	846		494	
Max. Pile Moment, with R = 3	kip ft		340		192
Pile Tension Strength	kip	-213		-213	
Pile Compressive Strength	kip	767		767	
Pile Moment Strength	kip ft		370		370

Summary

- **Option No. 2** All Plumb Piles, Works Well
- **Option No. 3** Batter Piles in All Bents, Is Workable
- **Option No. 1** Batter Piles in One Bent, Does Not Work,
too Much Load Is Attracted to too Few Batter Piles

Conclusions

- Batter Piles Tend to Attract High Seismic Loads
- An All-Plumb Pile Solution May Be Better, Even if Pile Size Needs to Be Increased to Provide Adequate Stiffness
- If Batter Piles Are Used, Many Batter Piles May Be Necessary to Resist Seismic Loads

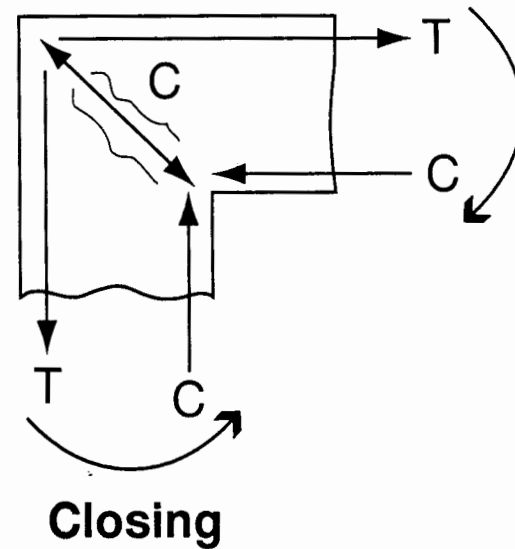
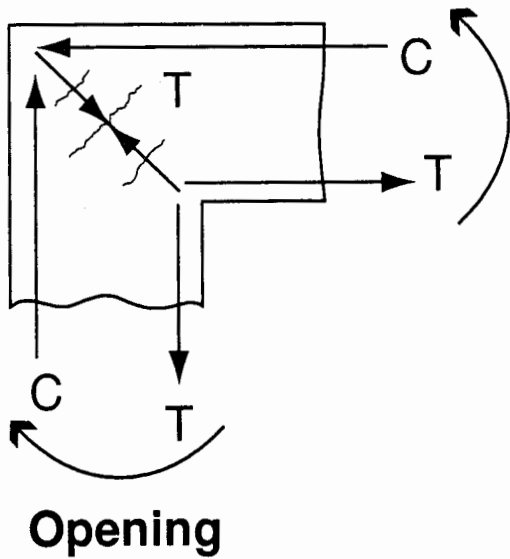
Session 6

Other Topics

Joint Design

- **Behavior**
- **Design Forces**
- **Shear Forces**

Behavior of Joints / Knee Joints



T = Tension
C = Compression

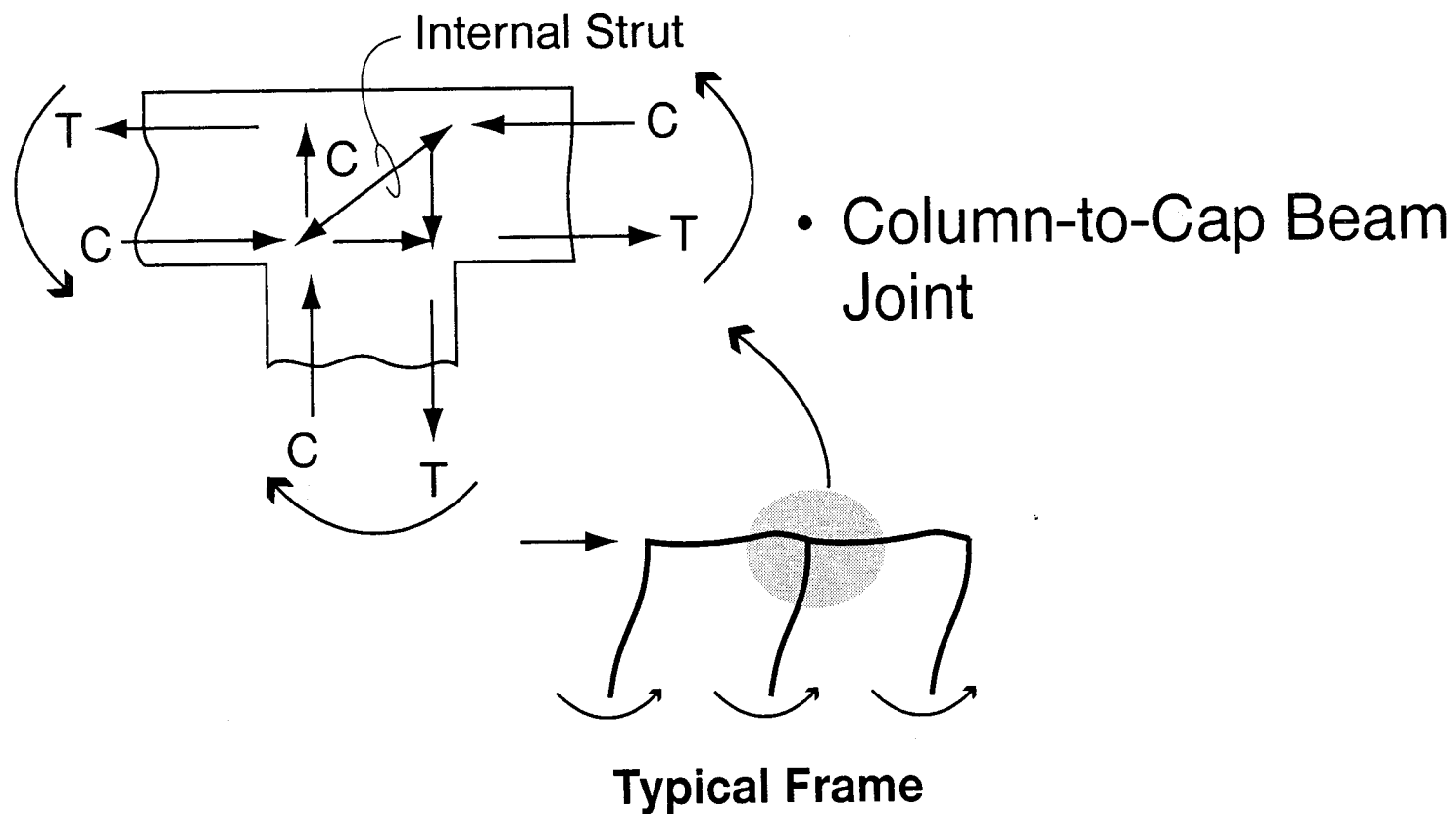
Knee Joint Damage



Loma Prieta, 1989

EERI (1990)

Behavior of Tee-Joints



Design Practice

Empirical Joint Design Procedure

- Limit Magnitude of Average Joint Shear Stress
(Limit Based on Experimental Data)
- Provide 'Minimum' Joint Confinement
Steel Hoops to Preserve Integrity

Calculating Shear Forces

- **Option 1 Use Approximations**

$$V_j = \frac{M_p}{b_e h_b h_c}$$

Where

b_e = Effective Joint Width

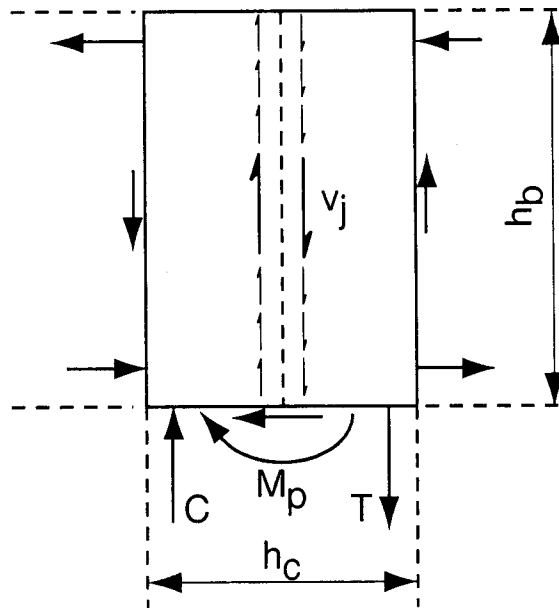
h_b = Beam Depth

h_c = Column Width

- **Option 2 Use Free Body Diagram with All Forces**

See Priestley, Seible, Calvi (1996)

Free Body of Joint



Approximations

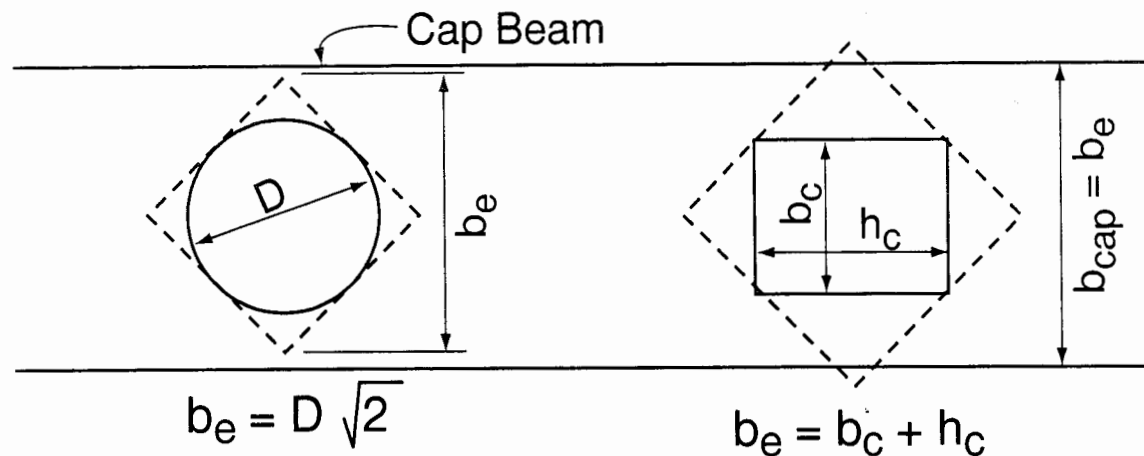
$$T \cong C \cong M_p / h_c$$

$$v_j \cong T / (b_e \cdot h_b)$$

$$v_j \cong \frac{M_p}{b_e h_b h_c}$$

Effective Joint Width

Circumscribe a Square About the Column



But: b_e not $> b_{cap}$

Plan View

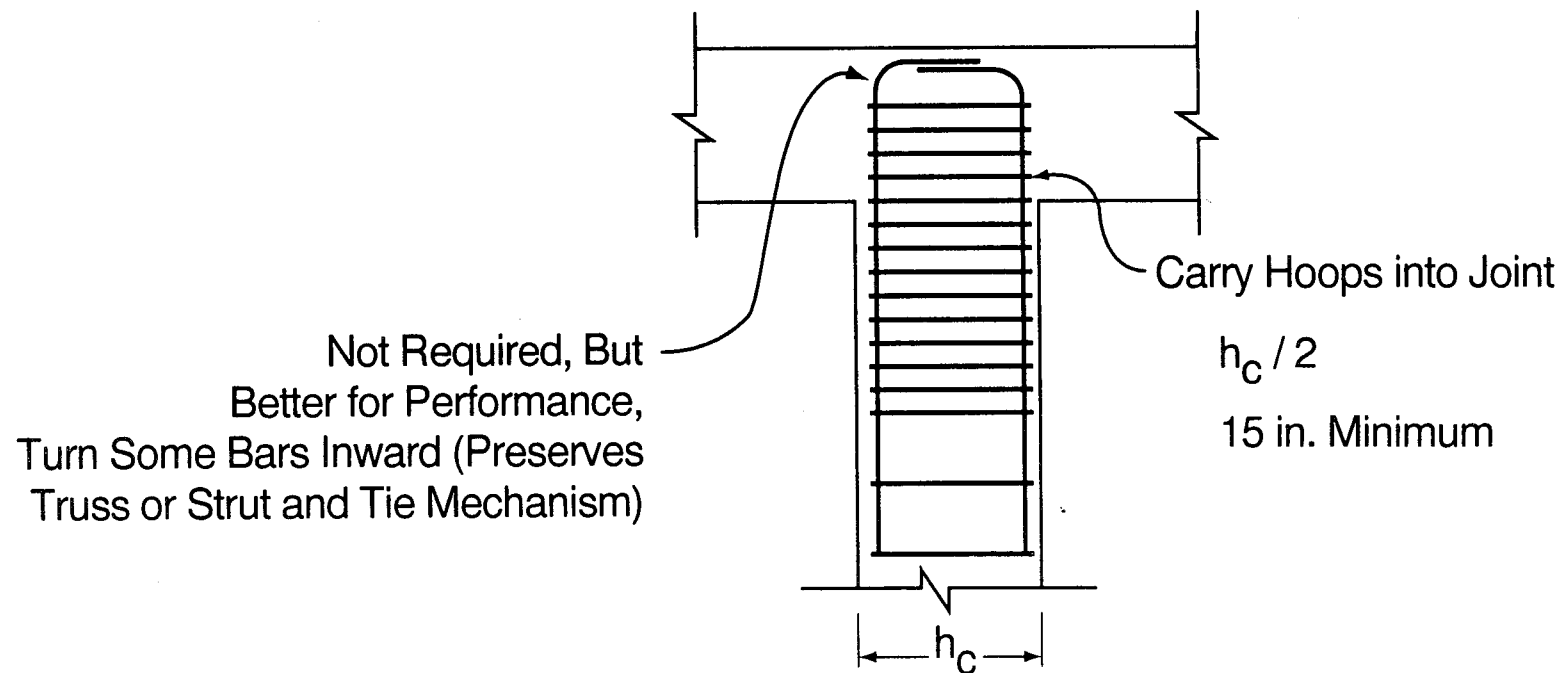
Limiting Joint Shear Stress / Division I-A

- **SPC C and D** $v_j \leq 12 \sqrt{f'_c}$ Normal Weight Concrete
 $v_j \leq 9 \sqrt{f'_c}$ Light Weight Concrete

General Comments

- Current Method Provides No Increase Based on Amount of Confinement Steel, Which Is the Plastic-Hinge Confinement Steel Carried One-Half of Column Dimension into Adjoining Member, Not Less Than 15 in.
- If Stress Limit Not Met, Increase Cap Beam Size
- Other Methods in Development
 - Truss Models
 - Limiting Principal Tension in Joint

Detailing Considerations



Session 7

Other Topics

Existing Bridge Assessment and Retrofit

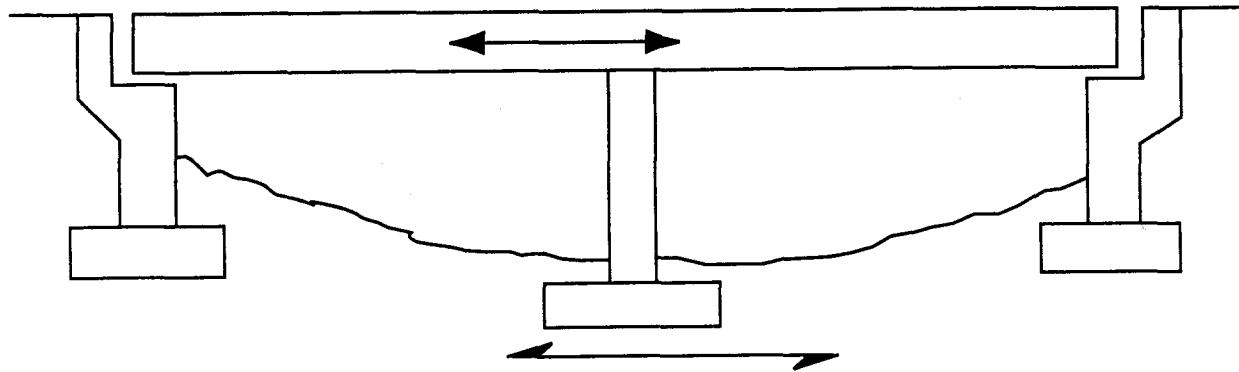
- **Expected Performance**
- **Actual Behavior**
- **Assessment Methodologies**
- **Comparison of New Design and Retrofit Practice**

Performance Objectives

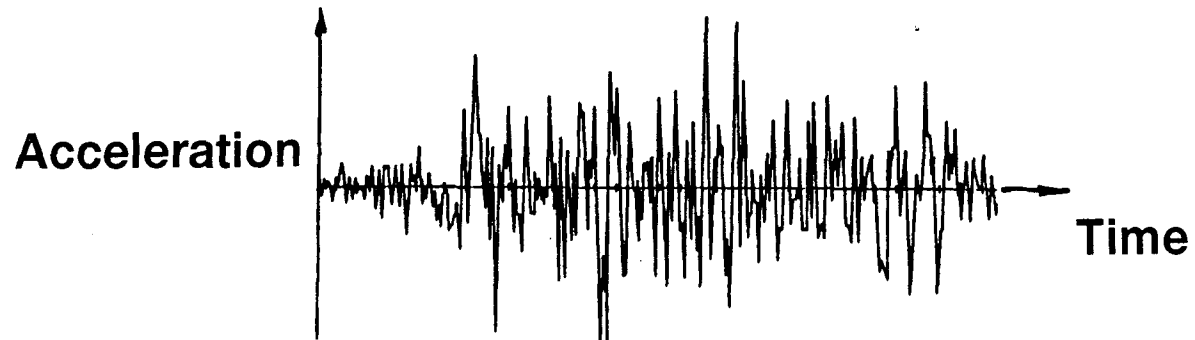
What Do We Expect from Our Bridges?

- Small to Moderate Earthquakes \rightarrow Elastic Response
No Significant Damage
- Large, Infrequent Earthquakes \rightarrow Inelastic Response
Damage Occurs, Detectable
No Collapse

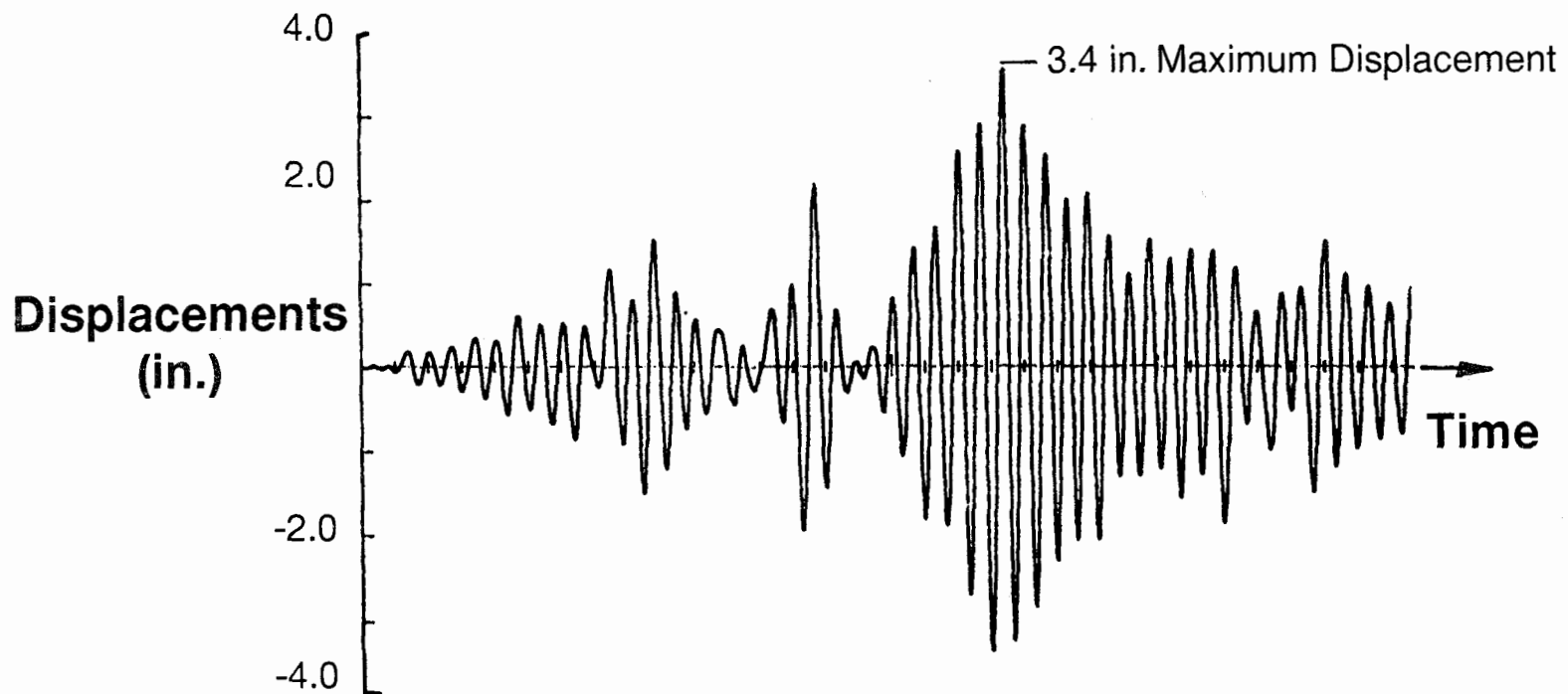
Conceptual Example



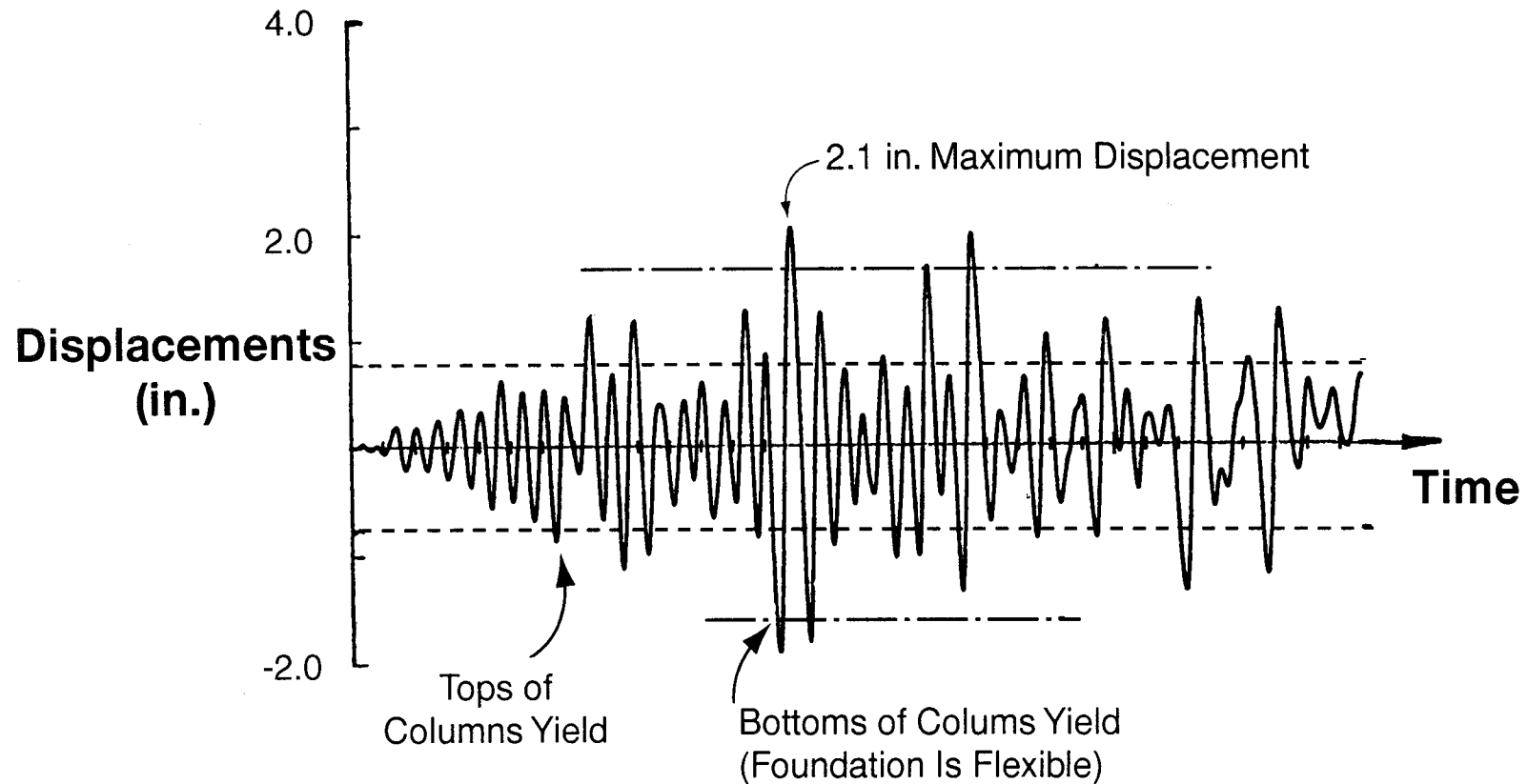
Longitudinal Earthquake Loading



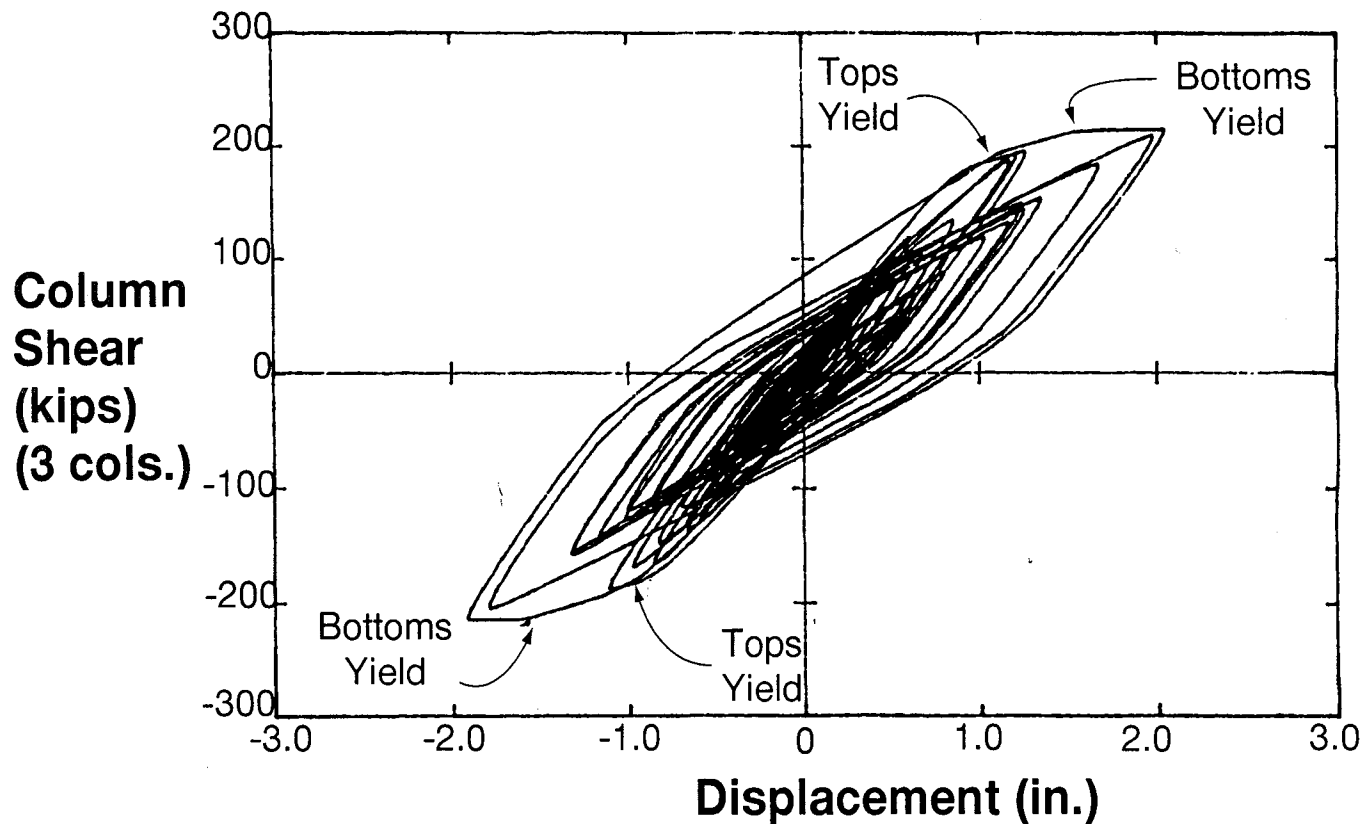
Response if Structure Remains Elastic



Response with Column Yielding



Shear in Column vs. Displacement

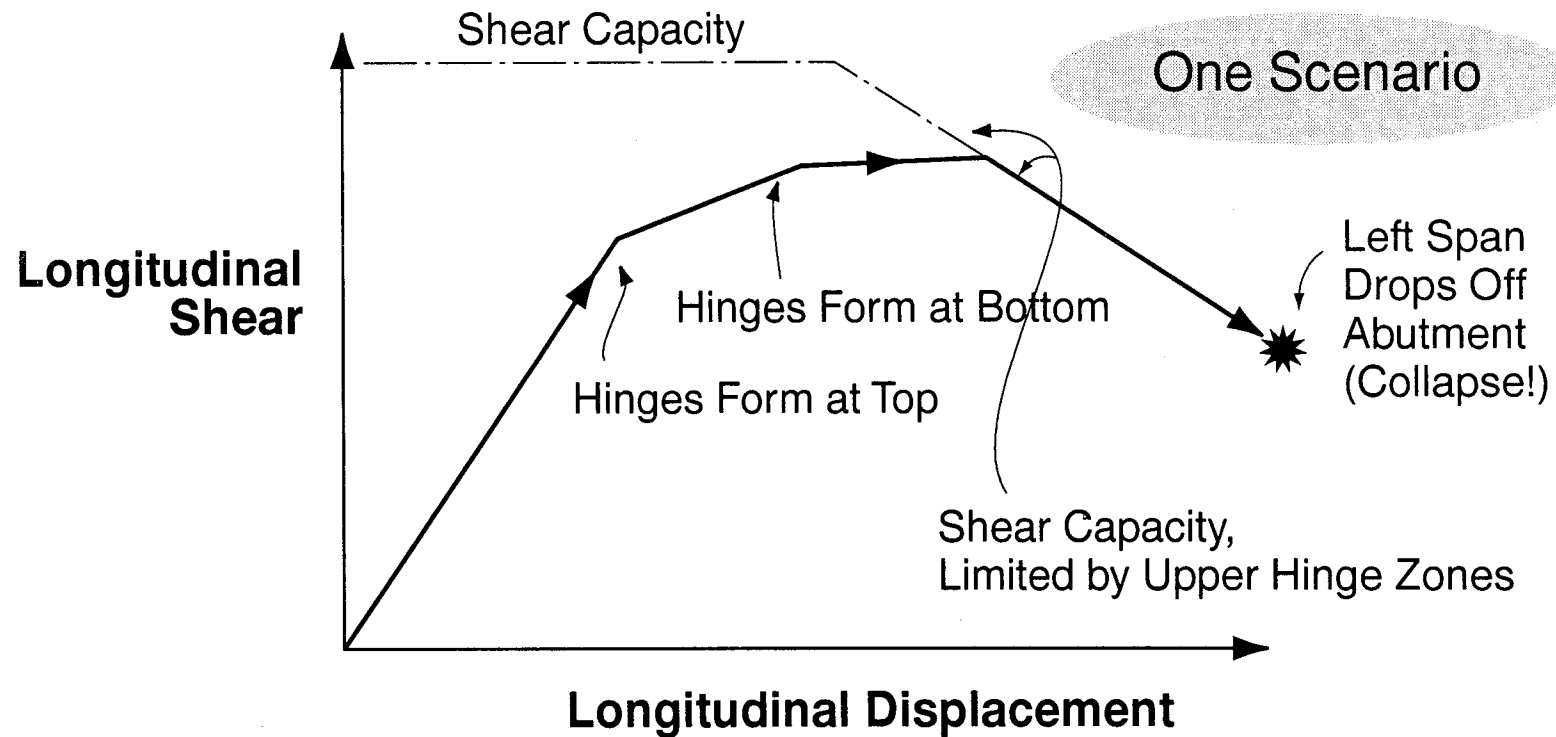


What Happened

- ## What Did Not Happen

- Abutment Gap Did Not Close
- Footing Did Not Overturn
- Footing Soil OK
- Splice at Bottom OK
- No Shear Failure { Columns { Hinges
 Joints Middle

Quasi-Static Look at Behavior (Envelope)



Issues and Failure Modes to Consider

- Displacements at Abutments
- Displacements at Interior Expansion Joints
- Forces in Restrainers (If Present)
- Column Hinge Confinement (Plastic Hinge Rotation Capacity)
- Shear Strengths — Columns, Hinges, Footings, Joints, etc.
- Anchorage and Development / Splices
- Footing, Yielding, Overturning, Sliding
- Foundation Strength / Liquefaction

Assessment Methodologies

- Capacity / Demand Ratio Method
- Lateral Strength Method (FHWA)

Plastic Collapse Mechanism
Pushover

Capacity / Demand Ratio Method (1 of 3)

- Analyze Bridge Elastically to Obtain Demands
- Calculate Member / Item Capacities

($\phi = 1.0$, Nominal Ultimate Values)

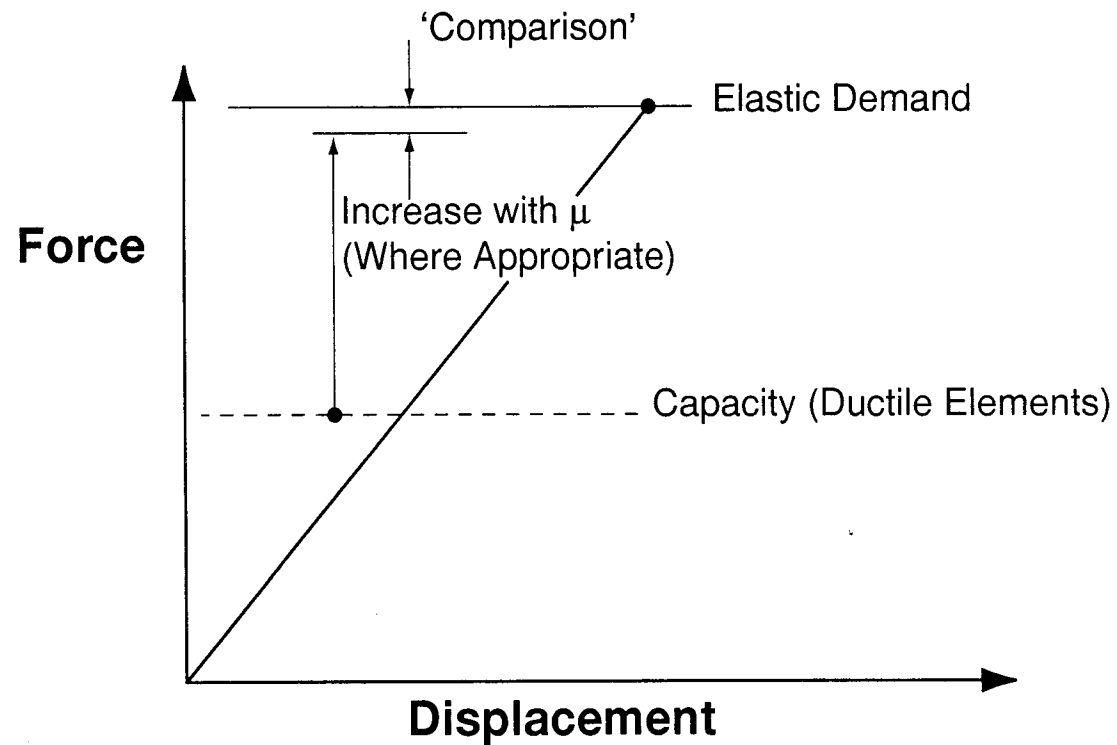
- Form C/D Ratio
- Increase Ratios for Ductile Elements

Using Ductility Indicator, μ

$$\frac{C}{D} < 1.0 \rightarrow \text{Failure}$$

- Estimate Damage / Failure Likelihoods
(Lowest C/D First, etc.)

Capacity / Demand Ratio Method (2 of 3)



Capacity / Demand Ratio Method (3 of 3)

Advantages

- Simple Analysis
- Quick Ranking of Element Performance
- Relatively Comprehensive Comparisons Developed

Disadvantages

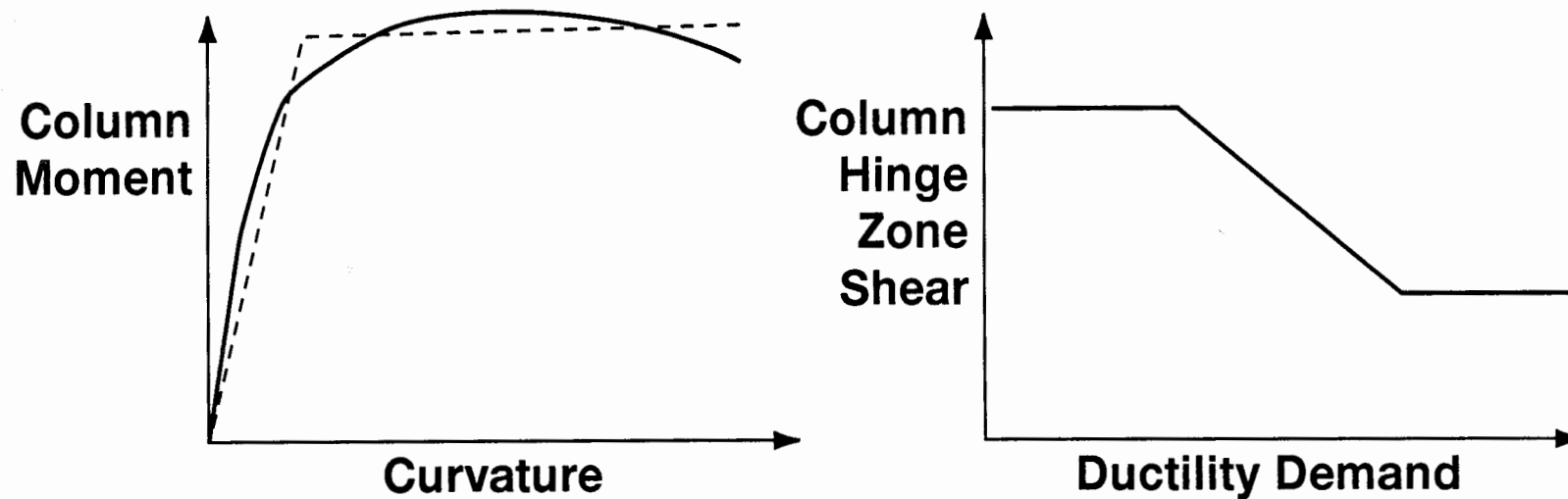
- Focus Is Entirely on Element Performance
- Cannot Account for Force Redistribution
- Does Not Account for Capacity Protection of Elements

Lateral Strength (Pushover) Method (1 of 4)

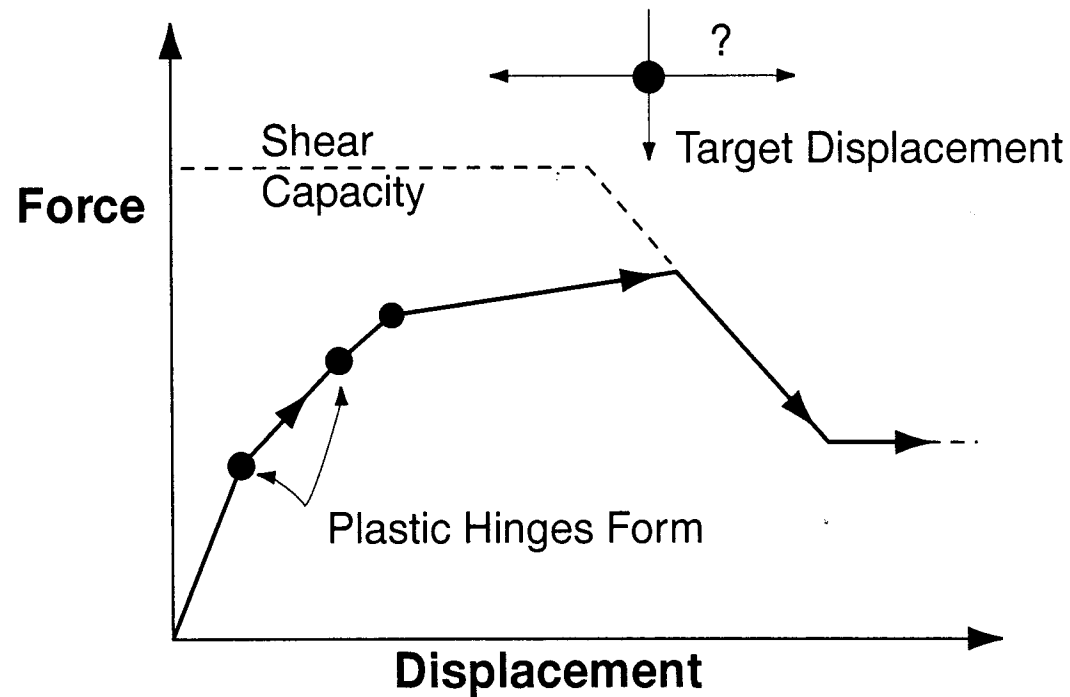
- Analyze Bridge Elastically to Obtain Target Displacements
- Develop Member Yield / Deformation / Failure Relations
- Develop Static Force / Resistance Curves (Pushover)
 - Entire Structure
 - Individual Frames
- Evaluate Behavior Up to Target Displacement

Can Elements Endure Entire Displacement Sequence?

Lateral Strength (Pushover) Method (2 of 4)



Lateral Strength (Pushover) Method (3 of 4)



Lateral Strength (Pushover) Method (4 of 4)

Advantages

- Tracks Sequence of Events (Yielding, Degradation, etc.) in Structure
- Indicates Structure (Sub-Structure) Overall Response — **System Focus**

Disadvantages

- More Effort Required (Development of Basic Member Data)
- Does Not Address Cyclic Effects Directly

New Design vs. Assessment / Retrofit

Item	New Design Provisions	Existing Bridges
• Plastic Hinging	Prescriptive Confinement	Assess Rotation Capacity Add Jacketing
• Member Shear	Design for Plastic Hinging Forces	Assess Shear Capacity and Ductility Demand Add Jacketing
• Structure Displacements	Provide Wide Seats	Probable Displacements Extend Seats Add Restrainers

New Design vs. Assessment / Retrofit

Item	New Design Provisions	Existing Bridges
• Reinforcement Splices	No Splices in High Moment Zone	Assess Ductility Demand Add Jacketing
• Footing Yielding Footing Shear	Design for Plastic Add Overlay Enlarge Footing	Assess Probable Forces Hinging Forces
• Joint Shear	Limit Average Shear Stress Protect from Force	Enlarge Joint Add Jacketing

Seismic Bridge Design Applications

Concluding Considerations

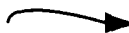

- In the Wake of the **1994 Northridge Earthquake:**

The Seismic Advisory Board Appointed to Evaluate Caltrans' Efforts Concluded:

7 Collapses

~ 4823 Total Bridges in LA Co.

“Caltrans’ design procedures and retrofit procedures are ‘technically sound.’”

- Caltrans' efforts  **AASHTO**
Division I-A
- Other's Experience (NZ, Japan, etc.) 

**Long Way
from
1971!**

Seismic Bridge Design Applications

Questions and Answers

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